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## **INVESTIGATION ON THE POTENTIAL OF A CO<sub>2</sub> CAPTURE SYSTEM, DOWNSTREAM OF THE AFTERTREATMENT SYSTEM FOR A HEAVY-DUTY ENGINE APPLICATION**

Murchana Pathak

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INVESTIGATION ON THE POTENTIAL OF A CO<sub>2</sub> CAPTURE SYSTEM,  
DOWNSTREAM OF THE AFTERTREATMENT SYSTEM FOR A HEAVY-DUTY  
ENGINE APPLICATION

By

Murchana Pathak

A THESIS

Submitted in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE

In Mechanical Engineering

MICHIGAN TECHNOLOGICAL UNIVERSITY

2018

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This thesis has been approved in partial fulfillment of the requirements for the Degree of  
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*Dedication*

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## Abstract

The transportation sector accounts for the second largest source of CO<sub>2</sub> emissions after power generation. New Corporate Average Fuel Economy (CAFE) regulations are focusing on improving energy through reduced fuel consumption and greenhouse gas emissions. This work investigates the potential of a CO<sub>2</sub> capture system downstream of an aftertreatment system for a heavy-duty engine application. Amine absorption has been described as one of the most effective ways to capture CO<sub>2</sub> from exhaust for point sources. Therefore, using thermal-swing absorption process with potassium carbonate (K<sub>2</sub>CO<sub>3</sub>) as the absorbent liquid, a process was analyzed for onboard CO<sub>2</sub> capture with a 15-liter heavy-duty truck engine. The CO<sub>2</sub> capture system comprises of a CO<sub>2</sub> absorber that separates CO<sub>2</sub> from the exhaust; a CO<sub>2</sub> stripper or regenerator that regenerates the absorbent liquid; heat exchangers and coolers for maintaining the required temperature of the system; and a compressor for compressing the CO<sub>2</sub> for storage. The operating parameters of the CO<sub>2</sub> capture system, including liquid flow rates, lean/rich loading were estimated by assuming a driving force for the mass transfer. The regenerator pressure was determined from the vapor-liquid equilibrium data as a function of temperature and lean CO<sub>2</sub> loading. The components of the system were designed and simulated individually in GT-Suite at a 60% CO<sub>2</sub> capture rate and this allowed for determination of liquid flow rates, outlet temperature and the

heat transfer across the system for a mid-speed, mid-load operating condition. The components are then integrated in GT-Suite to form a CO<sub>2</sub> capture system model downstream of the aftertreatment system. The system performance was then determined for different exhaust gas conditions representative of the Supplemental Emissions Test (SET) operating conditions from idle to full load. The CO<sub>2</sub> capture requires both heat and power for the absorption as well as the separation process which can utilize the energy extracted from waste heat recovery system (WHRS). The exhaust heat would be used to heat the solvent and desorb the CO<sub>2</sub> in the stripper. Unlike point sources, the onboard CO<sub>2</sub> capture system has challenges such as space limitations and availability of processes and cooling water. However, exhaust heat also provides a low-cost source of waste heat not typically available at stationary power plants. This work aims to determine the heat duty, cooling duty, and compression work required for capturing CO<sub>2</sub> at different engine operating conditions.



# **Chapter 1**

## **Introduction**

The phenomenon of global warming, one of the direct results of climate change has raised concerns over the emission of greenhouse gases such as carbon dioxide (CO<sub>2</sub>). As the world energy demand is increasing, greenhouse gas emissions are increasing, and this would require challenging efforts for reduction of CO<sub>2</sub> and other greenhouse gases in mitigating the climate change. A major source of CO<sub>2</sub> involves the combustion of fossil fuels. Among these various sources, coal-fired power generation is the largest contributor to CO<sub>2</sub> emission. Worldwide, the transportation sector accounts for 14% of all Greenhouse Gas (GHG) emissions and is therefore considered to be a significant source.

### **1.1.Motivation**

Over the years, the Environmental Protection Agency (EPA) regulations for vehicular CO<sub>2</sub> emissions are becoming increasingly more stringent. New Corporate Average Fuel Economy (CAFE) regulations are focusing on improving energy efficiency through reduced fuel consumption and greenhouse gas

emissions. Although more sustainable transportation options like renewable energy and alternate fuels seem to be a solution to reduce CO<sub>2</sub> emissions, the extent to which these sources can be utilized is very limited and they cannot suffice the world energy requirement in the present or in the future. Electrification is another technology to reduce tailpipe carbon emissions and improve fuel consumption, but they rely primarily on CO<sub>2</sub> generating coal and gas fired power plants to charge the batteries. Also, cost and off-road utility are two major disadvantages of electric vehicles, and range and charge time are major challenges for electrification of the heavy-duty transportation industry.

## **1.2.Sources of GHG emissions**

The worldwide greenhouse gas emissions resulting from the economic sector is shown in Figure 1.1 (EPA, 2016). Carbon dioxide emissions, being the most prominent source of greenhouse gas emissions, result from both natural and anthropogenic causes. Fossil fuel combustion is the primary source of CO<sub>2</sub> emissions which has increased steadily since the Industrial Revolution.

## 2015 Global Greenhouse Gas Emissions by Economic Sector

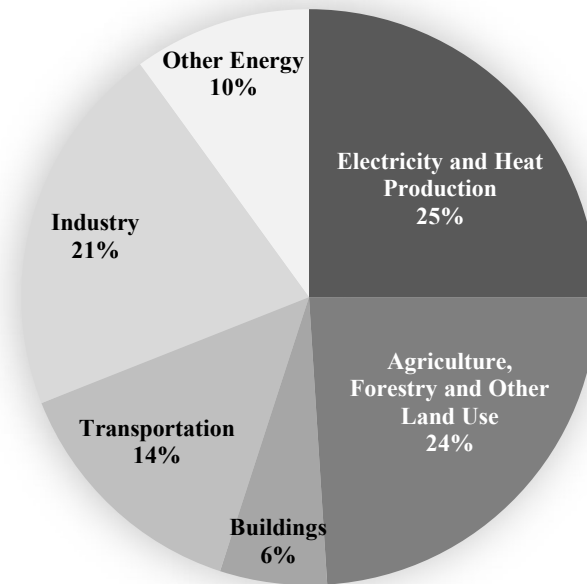


Figure 1.1. Worldwide GHG Emissions by Economic Sector in 2015, (EPA, 2016)

In 2015, fossil fuel combustion accounted for 93% of CO<sub>2</sub> emissions in the United States (EPA, 2015). The annual CO<sub>2</sub> emissions resulting from fossil fuel consumption from 1990 – 2015 are listed in Table 1.1 (EPA, 2015). From 1990 to 2015, the CO<sub>2</sub> emissions from the transportation sector in U.S. increased from 1493.8 million metric tons (MMT) CO<sub>2</sub> Eq. to 1736.4 million metric tons (MMT) CO<sub>2</sub> Eq., a 16.2 percent total increase over the twenty-six-year period.

Table 1.1. CO<sub>2</sub> Emissions from Fossil Fuel Combustion by End-Use Sector (MMT CO<sub>2</sub> Eq.)

| Gas/Source                    | 1990          | 2000          | 2010          | 2011          | 2012          | 2013          | 2014          | 2015          |
|-------------------------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|
| <b>Fossil Fuel Combustion</b> | <b>4740.3</b> | <b>5593.7</b> | <b>5359.4</b> | <b>5227.1</b> | <b>5024.6</b> | <b>5156.5</b> | <b>5202.3</b> | <b>5049.8</b> |
| Electricity Generation        | 1820.8        | 2296.9        | 2258.4        | 2157.7        | 2022.2        | 2038.1        | 2038          | 1900.7        |
| Transportation                | 1493.8        | 1805.5        | 1728.3        | 1707.6        | 1696.8        | 1713          | 1742.8        | 1736.4        |
| Industrial                    | 842.5         | 854.1         | 775.5         | 775           | 782.9         | 812.2         | 806.1         | 805.5         |
| Residential & Commercial      | 555.7         | 601.7         | 554.7         | 545.9         | 479.2         | 550.7         | 574.1         | 565.8         |

Figure 1.2 illustrates the five-major fuel consuming economic sectors contributing to CO<sub>2</sub> emissions from fossil fuel and non-fossil fuel combustion. Electricity generators produce 36% while transportation activities account for 32% of U.S. CO<sub>2</sub> emissions from fossil fuel consumption in 2015 (EPA, 2015). Medium and heavy-duty trucks account for 23% of CO<sub>2</sub> emissions, most of which consume around 2.7 million barrels of fuel, emitting a total of 530 million metric tons of CO<sub>2</sub>. Industrial emissions result from both fossil fuel consumption and electricity

generation while residential and commercial sectors rely heavily on electricity. Other sources or non-fossil fuel combustion includes CO<sub>2</sub> emissions from nuclear energy, hydroelectric energy or geothermal energy.

### 2015 U.S. Carbon Dioxide Emissions

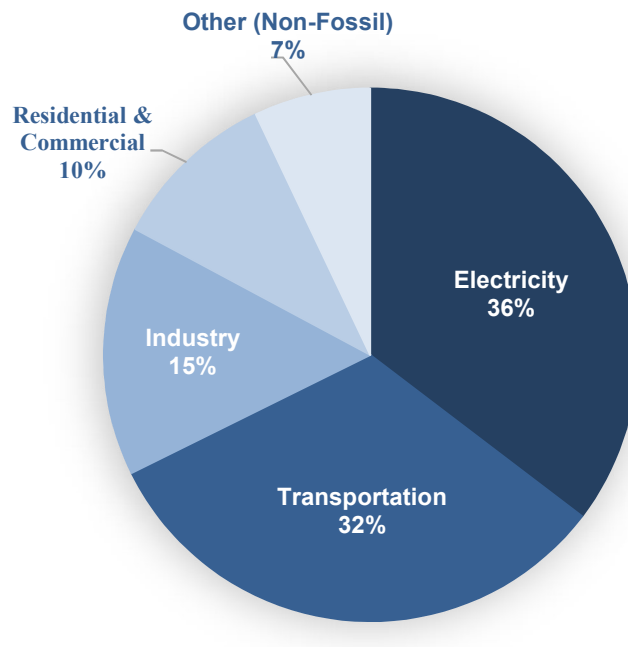


Figure 1.2. U.S. CO<sub>2</sub> Emissions from Fuel Combustion in 2015, (U.S. EPA, 2017)

#### 1.2.1. The Greenhouse Effect

The solar radiations from the sun are converted to infrared radiations or heat when they reach the earth surface. A part of these radiations or heat is absorbed by the gases in the earth's atmosphere and are re-radiated back to the earth. This phenomenon is called the greenhouse effect and the gases on earth's atmosphere responsible for this phenomenon are called greenhouse gases.

Carbon dioxide (CO<sub>2</sub>) is the most predominant greenhouse gas followed by water vapor, ozone (O<sub>3</sub>), methane (CH<sub>4</sub>), Nitrous oxide (N<sub>2</sub>O), etc. From 1990 to 2015, the total greenhouse gas emissions have increased by an overall 3.5%. In 2015, the U.S. gross greenhouse emissions were 6586.7 MMT of CO<sub>2</sub> Eq. out of which CO<sub>2</sub> emissions accounted for 5411.4 MMT of CO<sub>2</sub> Eq. Figure 1.3 shows the contribution of greenhouse gases to the total emissions in the U.S. in 2015. CO<sub>2</sub> is the primary greenhouse gas that resulted in 82% of the total emissions followed by methane (CH<sub>4</sub>) which contributes around 10%. Fossil fuel combustion was the major source of CO<sub>2</sub> emissions as well as overall greenhouse gas emissions. Nitrous Oxide (N<sub>2</sub>O) and other fluorinated gases like hydrofluorocarbon (HFC), perfluorocarbon (PFC), Sulphur hexafluoride (SF<sub>6</sub>) and Nitrogen trifluoride (NF<sub>3</sub>) contributed around 5% and 3% of the total emissions respectively.

## 2015 U.S. Greenhouse Gas Emissions

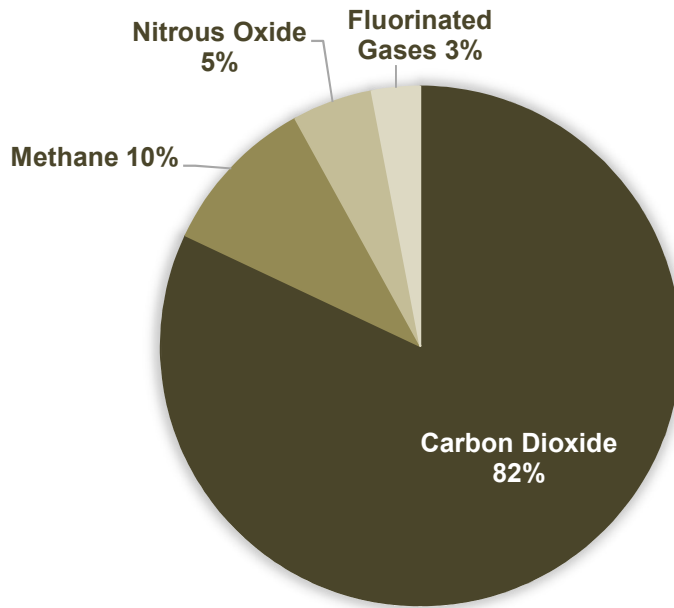


Figure 1.3. U.S. Greenhouse Gas Emissions in 2015 by gas source (U.S EPA, 2017)

### 1.2.2. Atmospheric CO<sub>2</sub> levels

Before the Industrial Revolution, the amount of CO<sub>2</sub> in the atmosphere was 280 parts per million (ppm). Since then, the rate of CO<sub>2</sub> has been increasing at an alarming rate and has reached a level of 406.56 parts per million by June 2017 according to National Oceanic and Atmospheric Administration (NOAA) researchers. Figure 1.4 depicts the monthly average atmospheric CO<sub>2</sub> levels measured at Mauna Loa Observatory in Hawaii with average seasonal cycle removed. Most of the atmospheric CO<sub>2</sub> is through a natural process. But human caused, or anthropogenic CO<sub>2</sub> makes its way into the atmosphere through different

paths. Energy-related activities are the largest anthropogenic contributor to CO<sub>2</sub> emissions, a wide majority of which accounts for combustion of fossil fuels followed by deforestation. There is a natural balance of carbon dioxide in the atmosphere and ocean as the carbon dioxide in the atmosphere is absorbed by the ocean and that in ocean rises to the atmosphere. However, the ocean is unable to absorb a large amount of carbon dioxide produced by the anthropogenic causes and this results in an increase of CO<sub>2</sub> levels in the atmosphere.

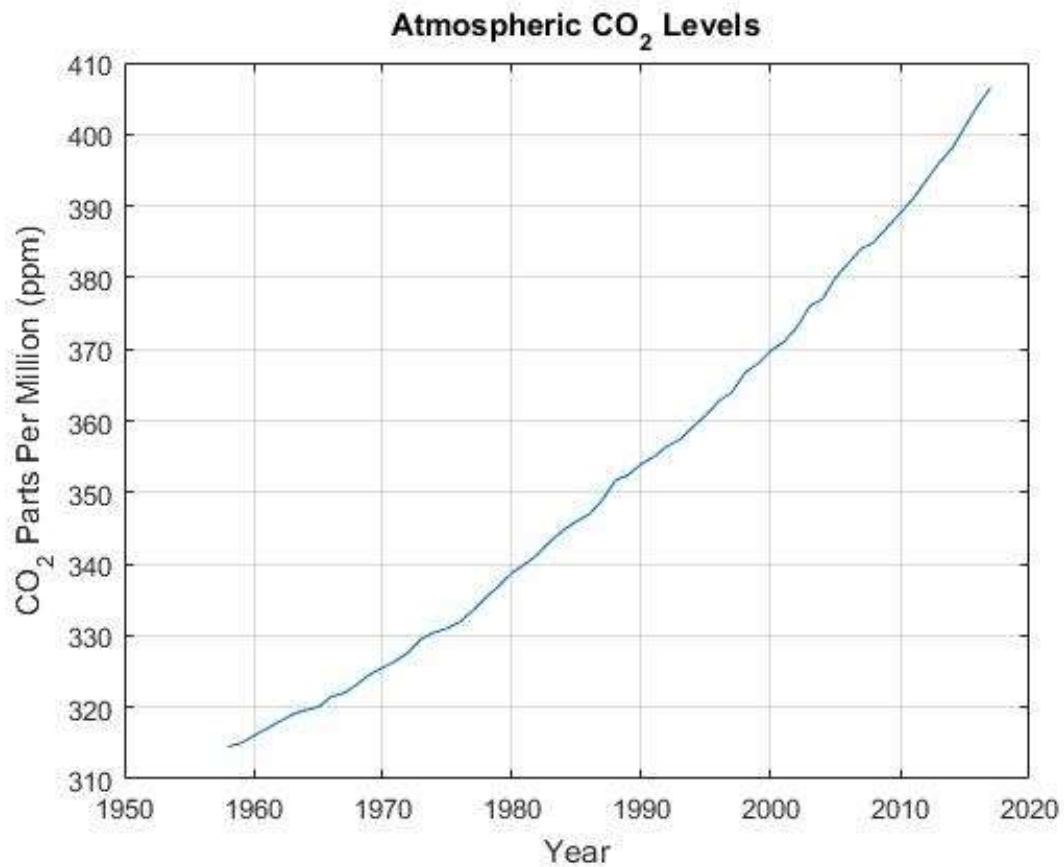


Figure 1.4. Monthly mean Atmospheric CO<sub>2</sub> levels from 1958 – 2017

(NOAA/ESRL, 2017)



### **1.3. Remediation of Carbon Dioxide**

To prevent the atmospheric CO<sub>2</sub> content from increasing at a rapid rate, the anthropogenic causes of CO<sub>2</sub> emissions must be curbed. Decreasing the rate of CO<sub>2</sub> emissions produced by burning fossil fuels is critical to that effort. Consumption of petroleum as a transportation fuel has been the largest CO<sub>2</sub> emission contributor in the post-industrial era.

### **1.4. Absorption/ Stripping Process**

Absorption is the mass transfer of a substance from the gaseous phase to the liquid phase. The substance absorbed can be bound by the liquid both physically and chemically. Amine solutions used in gas treating technology react reversibly with dissolved CO<sub>2</sub>. This has been established as one of the most effective ways to capture CO<sub>2</sub> from exhaust gas for point sources. The most common absorption process utilizes the concept of thermal swing absorption with a circulated chemical solvent. So, a process was analyzed for an onboard CO<sub>2</sub> capture system with a 15-liter heavy-duty truck engine. The exhaust gas going through the absorber is counter-currently brought in contact with an amine solvent at a low temperature. CO<sub>2</sub> from exhaust gas then reacts with the solvent with exothermal chemical reactions thereby reducing the concentration of CO<sub>2</sub> gas from the stream exiting the absorber. The solvent stream with a higher concentration or rich loading of CO<sub>2</sub> goes through a cross exchanger where it is heated up to a high temperature before it enters the stripper. The temperature of the stripper is

maintained at a high temperature so that absorption process is reversed, and the solvent stream liberates the CO<sub>2</sub>. The solvent stream with a lower concentration or lean loading of CO<sub>2</sub> passes through the cross exchanger where its temperature is reduced and is sent to the absorber to absorb more CO<sub>2</sub> from the incoming exhaust gas stream.

#### **1.4.1. Solvents**

A great variety of solvents can be used for exhaust gas treating but the most effective solvents considered for CO<sub>2</sub> removal are aqueous amines or hot potassium carbonate (K<sub>2</sub>CO<sub>3</sub>). 30% wt. 7m monoethanolamine or MEA is one of the most widely used amine solvents in CO<sub>2</sub> removal from flue gas because of its faster absorption rate but its performance is limited by its maximum operating temperature, rate of CO<sub>2</sub> absorption, cyclic CO<sub>2</sub> capacity, corrosion issues as well as oxidative and thermal degradation. Despite having poor thermodynamic properties, potassium carbonate has the advantage of being non-volatile and not subject to degradation – properties which are advantageous for onboard applications. Furthermore, its poor heat of absorption can potentially be compensated for by operating the stripper at much higher temperature using waste exhaust heat. The choice of solvent influences the energy requirements, cooling requirements, and equipment size for the CO<sub>2</sub> capture system and is, therefore, an important factor to consider for optimizing energy flow along with the absorption rate.

#### **1.4.2. Energy requirement and technical challenges**

The CO<sub>2</sub> capture system requires a considerable amount of energy for solvent regeneration and compression of CO<sub>2</sub>. In addition to that, energy is required for the heat exchanger, coolers, and condenser required to maintain the temperature of the system. For a heavy-duty engine, the integration of the CO<sub>2</sub> capture system to a waste heat recovery system following the exhaust gas recirculation (EGR) and downstream of the aftertreatment system, can reduce the energy penalty of the process. The waste heat recovery system utilizes the concept of an Organic Rankine cycle (ORC) with a working fluid to harvest energy from the engine's heat dissipating circuits. The energy recovered could be used to provide power for compression of CO<sub>2</sub> in the separation process while the remaining exhaust heat could be utilized in solvent regeneration and desorption of CO<sub>2</sub> in the stripper. Calorimetry affects the sizing of heat exchangers which in turn affects the energy requirements for solvent regeneration. The temperature of the engine's exhaust gas is very high and is required to be brought down by a considerable amount before it goes through the absorber owing to the thermal swing variation. However, exhaust heat also provides a low-cost source of waste heat not typically available at stationary power plants. The gas rate, CO<sub>2</sub> concentration, liquid rate, and lean loading all play an important role in determining the design specifications for height and diameter of the CO<sub>2</sub> absorber system. Other technical challenges involve CO<sub>2</sub> storage, collection, transportation, and disposal. The CO<sub>2</sub> collected can be stored onboard the vehicle temporarily before

being offloaded during refueling. Transportation to the disposal site can occur through existing CO<sub>2</sub> pipelines and injected into suitable deep rock geological formations underground for long term storage in depleted oil and gas reservoirs or to recover oil. Subsurface geological storage of CO<sub>2</sub> both onshore and offshore along with CO<sub>2</sub> capture can cut down emissions (IPCC, 2005).

### **1.5.Scope of work**

The focus of this work is to –

1. Determine the energy requirement for absorption and desorption of CO<sub>2</sub> for a heavy-duty engine application at a mid-speed, mid-load operating condition.
2. Study the solvent properties required for the absorption process.
3. Design a solvent regenerator model to obtain the CO<sub>2</sub> VLE data and evaluate the solvent parameters throughout the system.
4. Design a CO<sub>2</sub> capture system in GT-Suite for an on-board application to evaluate the energy requirements and solvent parameters for different operating conditions.

### **1.6.Outline of the thesis**

The thesis is organized into five chapters. Chapter 1 gives a brief overview of the objective and motivation behind the work, the fundamentals of the CO<sub>2</sub> absorption process and its challenges in an on-board system. Chapter 2 provides an overview on the theories of mass transfer with chemical reactions, equilibrium

and solvent rate behavior for a deeper understanding of the absorption process. Chapter 3 defines the CO<sub>2</sub> capture system and its components for a heavy-duty application including the assumptions, boundary conditions and steps to calculate their individual performance. A model is developed in GT-Suite® to simulate the energy transfer across the system as well as solvent parameters for all the SET operating conditions from idle to full load. Chapter 4 discusses the results obtained from the VLE data, the solvent properties and the CO<sub>2</sub> loading throughout the system as well as the heat transfer rate and flow rates for different operating conditions obtained from the GT model. Chapter 5 summarizes the overall methodology and results from this work and provides recommendations to further expand this research.

## **Chapter 2**

### **Literature Review**

This chapter presents the relevant theories and literature pertaining to the study of CO<sub>2</sub> absorption by aqueous amines and other solvents for point sources. A brief theory on the mass transfer with chemical reactions as well as equilibrium and rate behavior of solvents with an emphasis on potassium carbonate is discussed in this chapter with related assumptions and boundary conditions.

#### **2.1. Mass Transfer Theory**

The mass transfer of CO<sub>2</sub> from the exhaust gas to a liquid involves diffusion in both liquid and gas phase, physical solubility at gas-liquid interface and chemical reactions in the liquid. The role of diffusion and chemical reactions in the liquid is the most complicated part of the mass transfer process in the liquid phase. The properties of the solvent have a significant influence on the mass transfer of CO<sub>2</sub> in liquid thereby making the basics of mass transfer theories in the liquid phase a vital element for choosing the best solvent [3].

### 2.1.1. Mass Transfer Coefficients

The gas molecules diffuse in the liquid in the process of physical absorption. The flux,  $N_{CO_2}$  represents the rate of mass transfer at unit area and can be calculated at the gas-liquid interface ( $x = 0$ ) as –

$$N_{CO_2} = -D_{CO_2} \left. \frac{\partial [CO_2]}{\partial x} \right|_{x=0} \quad (2.1)$$

The flux is proportional to the concentration driving force for mass transfer across the boundary layers. In case of  $CO_2$  absorption from gas to liquid, flux can be calculated for driving force in both gas and liquid film and is same at any point within the boundary layer. The proportionality constant between flux and its corresponding driving force is the mass transfer coefficient.

$$N_{CO_2} = \begin{cases} K_G(P_{CO_2} - P_{CO_2}^*) \\ k_g(P_{CO_2} - P_{CO_2,i}) \\ k_l([CO_2]_i - [CO_2]) \\ k'_g(P_{CO_2,i} - P_{CO_2}^*) = \frac{k_l}{H_{CO_2}}(P_{CO_2,i} - P_{CO_2}^*) \end{cases} \quad (2.2)$$

Where  $K_G$  represents the overall gas phase mass transfer coefficient,  $k_g$  is the gas phase mass transfer coefficient and  $k_l$  is the liquid phase mass transfer coefficient and  $k'_g$  is the liquid phase mass transfer coefficient defined in gas phase units.  $P_{CO_2}$  indicates the bulk gas partial pressure of  $CO_2$ ,  $P_{CO_2}^*$  is the equilibrium partial pressure of  $CO_2$  in the bulk liquid and  $P_{CO_2,i}$  is the partial pressure of  $CO_2$  at gas-liquid interface.  $K_G$  corresponds to the concentration driving force between

bulk gas and bulk liquid where  $P_{CO_2}^*$  is in equilibrium with  $[CO_2]$ .  $k_g$  and  $k_l$  correspond to driving force across the gas film and liquid film respectively. Both  $k_l$  and  $k'_g$  are functions of liquid properties.  $H_{CO_2}$  is the Henry's constant of  $CO_2$  in the solvent and is used to denote the equilibrium of  $CO_2$  in the gas and liquid at the gas-liquid interface [3].

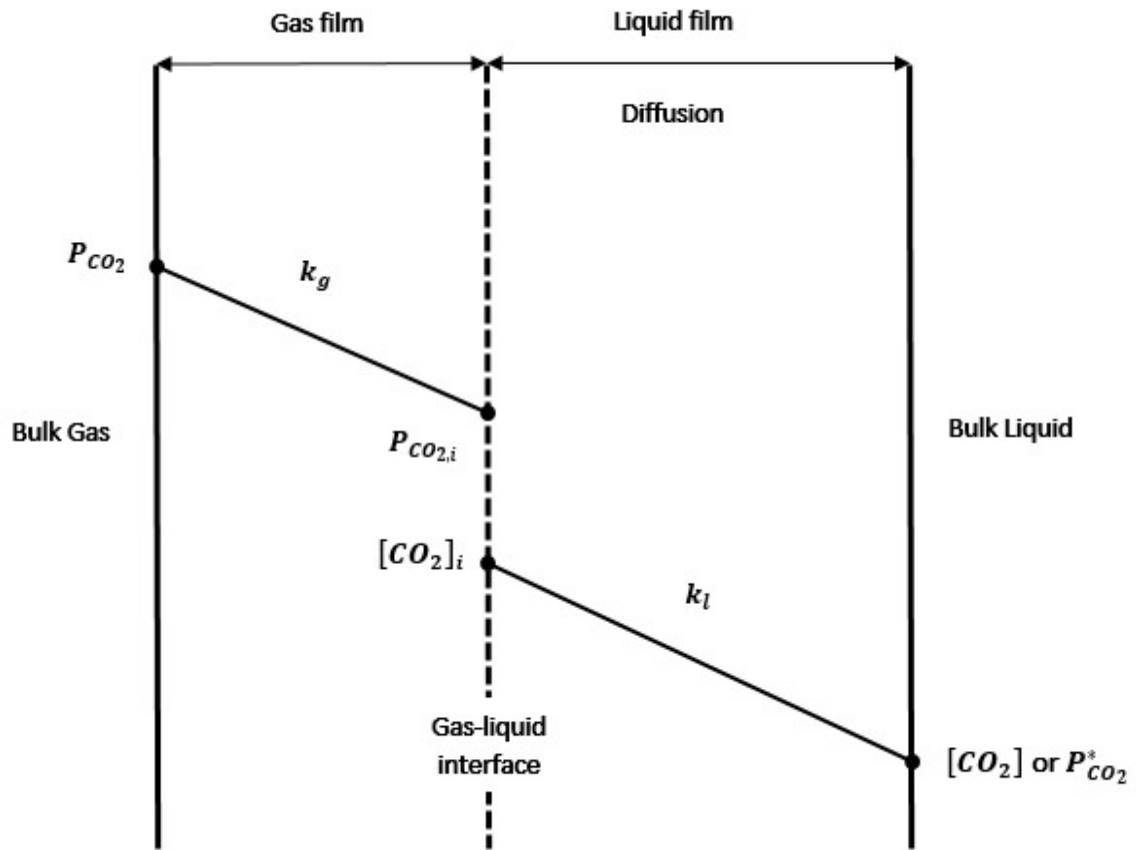


Figure 2.1. Schematic of Physical Mass Transfer of  $CO_2$  into Bulk Liquid

$CO_2$  molecules from the gas phase move to the gas-liquid interface where it dissolves. The dissolved  $CO_2$  then reacts with the solvent, diminishes from the interface and diffuses into the bulk liquid.



The flux in Equation 2.2 is constant and can be combined to represent addition of series resistances to mass transfer. The overall mass transfer coefficient in a physical absorption is same as the sum of gas film and liquid film mass transfer coefficients.

$$\frac{1}{K_G} = \frac{1}{k_g} + \frac{H_{CO_2}}{k_l} = \frac{1}{k_g} + \frac{1}{k'_g} \quad (2.3)$$

In a chemical reaction, most of the reactions occurs in the Reaction film, which is a thin layer between the gas-liquid interface and the reaction-diffusion interface as shown in Figure 2.2. The chemical reaction monitors the equilibrium at the interface and the driving force is represented by equilibrium and diffusion of CO<sub>2</sub> into the reaction film for reversible reactions. The series resistance relationship can be expressed as –

$$\frac{1}{K_G} = \frac{1}{k_g} + \frac{1}{k''_g} + \frac{1}{k_{l,PROD}} \frac{\partial P_{CO_2}^*}{\partial [CO_2]_T} \quad (2.4)$$

Since  $k_g$  comprises of both reaction and liquid diffusion films, it has both reaction and diffusion component which is shown in Equation 2.4. The term  $k''_g$  is the pseudo first order term denoting the reaction kinetics of the solvent. The third term in the Equation 2.4 represents diffusion resistance where  $\partial P_{CO_2}^* / \partial [CO_2]_T$  denotes the slope of the equilibrium line. It enables a series resistance relationship by changing the CO<sub>2</sub> concentration driving force to partial pressure driving force [8].

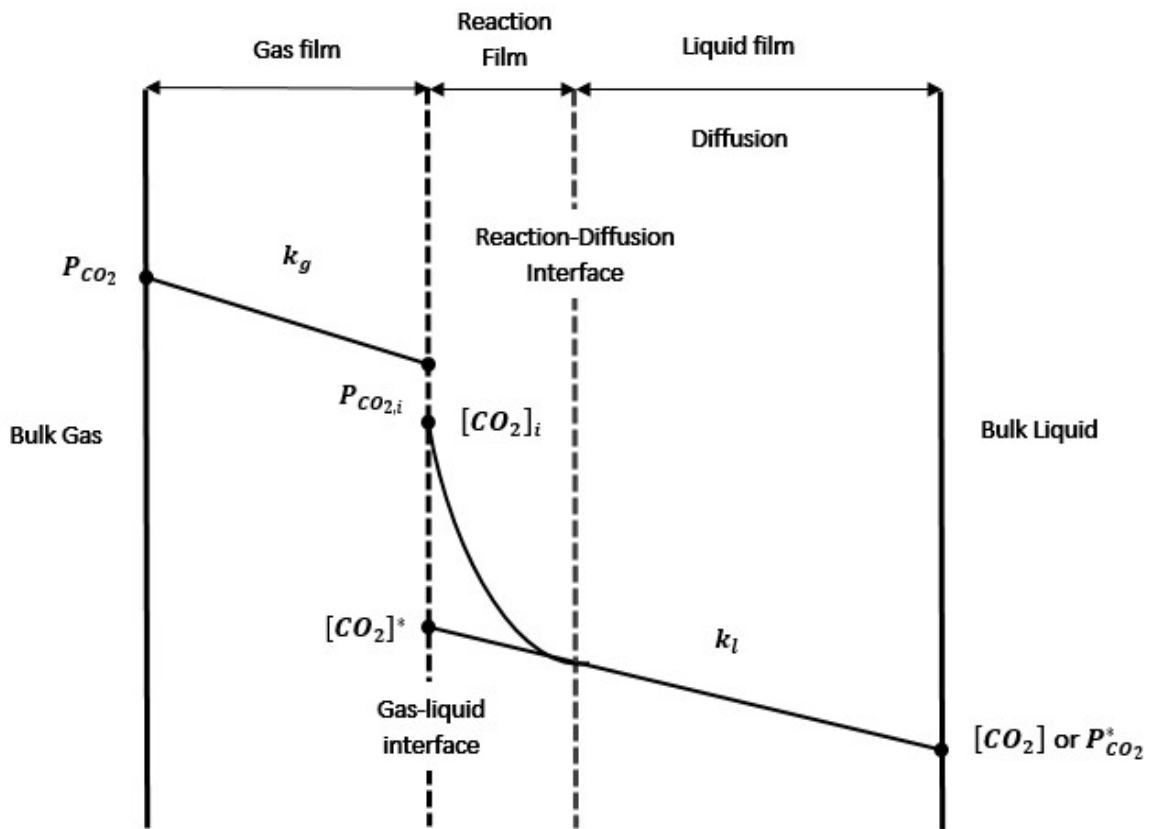


Figure 2.2. Schematic of Mass Transfer of  $\text{CO}_2$  into Bulk Liquid with Fast Chemical Reaction

As shown in Figure 2.2, the system includes resistance for gas film, reaction film and liquid diffusion film. If the reaction film resistance is predominant in a system while the liquid diffusion resistance is negligible it leads to a pseudo first order reaction. If the liquid diffusion film resistance is predominant and the reaction resistance is negligible the system leads to an instantaneous reaction condition.

## 2.2. Pseudo First Order Reaction

The pseudo first order reaction is an approximation that simplifies mass transfer with fast chemical reaction. It assumes that the concentration of amine in the solvent for reacting with CO<sub>2</sub> is higher relative to CO<sub>2</sub> flux. Applying the pseudo first order assumption, the rate of CO<sub>2</sub> reaction can be expressed as –

$$D_{CO_2} \frac{\partial^2 [CO_2]}{\partial x^2} - k_2 [Am] [CO_2] = 0 \quad (2.5)$$

Assuming both the amine concentration and the solvent concentration are same at the bulk liquid interface,

$$D_{CO_2} \frac{\partial^2 [CO_2]}{\partial x^2} - k_2 [Am]_b [CO_2] = 0 \quad (2.6)$$

where  $[Am]_b$  is the amine concentration with bulk solution composition. Using boundary conditions and neglecting the physical absorption of CO<sub>2</sub>, the flux is represented for reversible reactions as follows –

$$N_{CO_2} = \frac{\sqrt{D_{CO_2} k_2 [Am]_b}}{H_{CO_2}} (P_{CO_{2,i}} - P_{CO_2}^*) \quad (2.7)$$

From pseudo first order concentrations, the flux is expressed as –

$$k_g = \frac{\sqrt{D_{CO_2} k_2 [Am]_b}}{H_{CO_2}} \quad (2.8)$$

### 2.3. Instantaneous Reaction

The instantaneous reactions involve mass transfer with chemical reactions that are very fast or instantaneous with respect to diffusion. These reactions usually occur at high temperatures with increase in kinetics or low solvent concentrations. The mass transfer is driven by the diffusion of reactants from reaction film and the diffusion of products from the reaction film. The total solubility of CO<sub>2</sub> is represented by all dissolved forms like carbamate and bicarbonate of gas and the mass transfer rate is expressed as –

$$N_{CO_2} = k_l([CO_2]_{i,T} - [CO_2]_T^*) = k_l \left( \frac{P_g}{H_{CO_2}} - [CO_2]_T^* \right) \quad (2.9)$$

Where  $[CO_2]_{i,T}$  is the total concentration of the dissolved CO<sub>2</sub> at gas-liquid interface,  $P_g$  is the CO<sub>2</sub> partial pressure in gas phase and in equilibrium with the dissolved CO<sub>2</sub> at gas-liquid interface and  $H_{CO_2}$  is the Henry's constant of CO<sub>2</sub> in the solvent.

An instantaneous reaction case could be seen at the CO<sub>2</sub> stripper conditions. The stripper operates at a high temperature and thereby has higher driving forces of CO<sub>2</sub> partial pressure. The high partial pressure driving forces rule out the role of kinetics hence making the liquid phase diffusion coefficients the only factors contributing to the mass transfer.

## **2.4. Solvents for CO<sub>2</sub> absorption**

This discussion includes the basic thermodynamic and chemical analysis of different types of solvents used for CO<sub>2</sub> absorption.

### **2.4.1. Amines**

Amines are organic compounds containing a basic nitrogen atom. Based on their structure, amines are subdivided as primary and secondary amines, tertiary amines and hindered amines. Primary amines have one carbon atom connected to the nitrogen while secondary amines have two carbon atoms. They have open structures that enables CO<sub>2</sub> to form carbamates with the nitrogen. Tertiary amines have three carbon atoms attached to the nitrogen which makes it unstable for carbamates and forms bicarbonates instead. Hindered amines are primary and secondary amines with functional groups around the nitrogen that can hinder the formation of stable carbamates (Satori and Savage 1983). They can react with CO<sub>2</sub> to form carbamates at a lower equilibrium concentration. Hindered amines can convert CO<sub>2</sub> to bicarbonate with water like tertiary amines and have higher solvent capacity than primary and secondary amines.

A significant amount of literature data on rate studies of amines is available of which most of the studies are concerned with reactions of MEA and CO<sub>2</sub>. Previous work on amines with CO<sub>2</sub> have been done by Dugas (2009) with 7-13 m MEA; Chen (2011) with 10 m Diglycolamine (DEA), 8 m 1,2-Diaminopropane (MEDA), 8

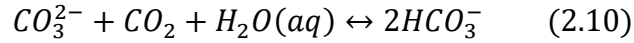
m 1 & 2 Methylpiperazine; Bishnoi (2000) with 7.6 m Methyldiethanolamine (MDEA) with Piperazine (PZ), focusing on absorption rate and capacity.

#### 2.4.2. Potassium Carbonate

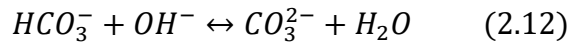
Potassium Carbonate ( $K_2CO_3$ ) has been used for  $CO_2$  absorption in natural gas treating and ammonia production for a long time. In 1954 and 1956, Benson *et al.* studied the pilot plant characterization of hot potassium carbonate and MEA, validating the use of  $K_2CO_3$  as an effective  $CO_2$  absorbent in the commercial market and utilized it for treating synthesis gas in 1959.

The absorption of  $CO_2$  into  $K_2CO_3$  is represented by the following overall reaction

—



Which can also be expressed as two parallel reversible reactions



The reaction rate is represented as a second order rate expression.

$$r_{CO_2} = k_{OH^-} [OH^-] [CO_2] \quad (2.13)$$

The reaction is usually slower than aqueous amines, but the energy required to reverse the reaction is lesser than that for amine solvents. However,

this low heat of absorption also means that at a given temperature, CO<sub>2</sub> is produced at a lower pressure, increasing the amount of water vaporized per mol of CO<sub>2</sub> as well as the compression work. Lastly, potassium carbonate is non-volatile and not prone to degradation reactions and hence there is no solvent loss due to degradation.

## 2.5. CO<sub>2</sub> Loading

The CO<sub>2</sub> loading represents the CO<sub>2</sub> concentration in a solution. It is given by the ratio of CO<sub>2</sub> molecules to the equivalent alkalinity. The CO<sub>2</sub> loading is expressed mathematically as –

$$CO_2 \text{ Loading} = \frac{n_{CO_2}}{n_{solvent}} \quad (2.14)$$

$n_{CO_2}$  and  $n_{solvent}$  represents the number of moles of CO<sub>2</sub> and the solvent respectively. In some cases, loading is expressed as per mole of basicity rather than per mole of solvent, thus the definition can depend on the solvent in question. The CO<sub>2</sub> loading for potassium carbonate solution can be represented by –

$$CO_2 \text{ Loading} = \frac{n_{CO_2}}{n_{K_2CO_3}} \quad (2.15)$$

## Chapter 3

### System Definition and Model Development

This chapter includes the development of the CO<sub>2</sub> capture system, its assumptions and thermodynamic considerations as well as the model integration for a heavy-duty truck engine.

#### 3.1. CO<sub>2</sub> Capture System

The CO<sub>2</sub> capture system utilizes the thermal swing absorption process with a circulated chemical solvent. A schematic of the CO<sub>2</sub> capture system is developed for an on-board application as shown in Figure 3.1. The exhaust gas coming out of the Selective Catalytic Reduction (SCR) of the aftertreatment system at temperature  $T_1$  is sent through an exhaust heat exchanger where its temperature reduces to  $T_2$ . The exhaust gas with low temperature  $T_2$  passes through the absorber before it exits via the tailpipe. The absorbent liquid or solvent is sent through the absorber in a counter-current direction where it absorbs the CO<sub>2</sub> from the exhaust gas at low temperature. The absorbent liquid now rich with CO<sub>2</sub> loading is sent to the absorbent-absorbent heat exchanger and the exhaust



absorbent heat exchanger where its temperature is increased to  $T_5$  before it enters the stripper. At high temperature of  $T_4$ , the  $\text{CO}_2$  molecules are released from the absorbent liquid molecules producing a  $\text{CO}_2$ -lean absorbent solution leaving the stripper. The absorbent then circulates back through the absorbent-absorbent heat exchanger and trim cooler that brings its temperature down to  $T_2$  before it returns to the absorber. The  $\text{CO}_2$  stream from the stripper is then sent through a condenser where it is condensed to  $T_6$  and the water is collected. The  $\text{CO}_2$  is then sent to the compressor where it is compressed to  $P_3$  before it goes to the storage tank.

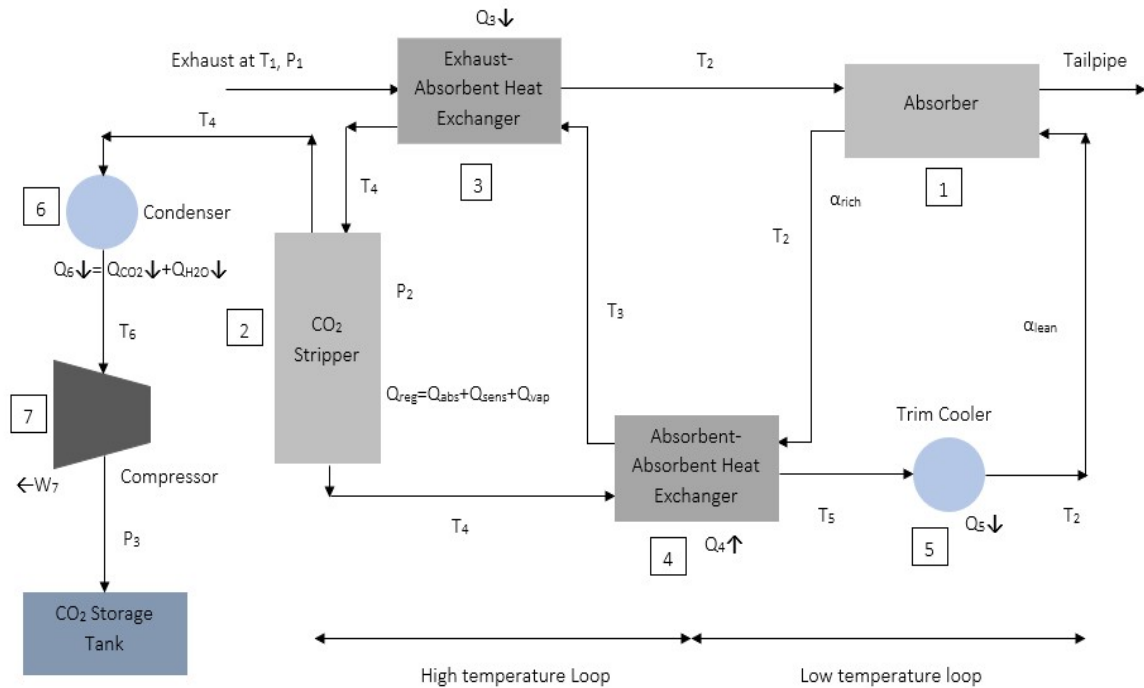


Figure 3.1. Schematic of the on-board  $\text{CO}_2$  Capture system

## 3.2. Sub-components of the system

### 3.2.1. Absorber

The absorber usually consists of one or more membrane contractors, which comprises of a bundle of narrow porous tubes encompassed by a cylindrical shell. The solvent flows through these tubes while the exhaust flows through the shell outside the tubes. The solvent absorbs the  $\text{CO}_2$  from the exhaust gas through the porous tubes before the exhaust gas leaves the tailpipe. The exhaust gas and the solvent must be brought down to a low temperature of  $40\text{-}60^\circ\text{C}$  before it is sent through the absorber. This is important, as at higher temperatures, the  $\text{CO}_2$  molecules would break away from the solvent molecules thereby making the absorption process less effective.

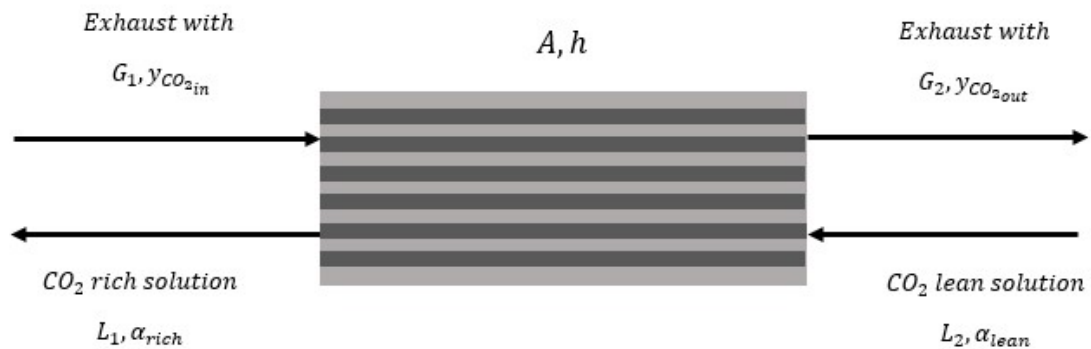


Figure 3.2. Functional diagram of an absorber

Where  $G_1$  is exhaust gas flow rate with  $CO_2$  composition  $y_{CO_2in}$  entering the absorber and  $G_2$  is exhaust gas flow rate with  $CO_2$  composition  $y_{CO_2out}$  leaving the absorber.  $L_2$  and  $L_1$  are solvent or liquid flow rates entering and leaving the absorber.  $\alpha_{lean}$  and  $\alpha_{rich}$  are the  $CO_2$  lean loading and rich loading respectively.

The mass balance in the absorber is given by the following equation

$$G_1 y_1 + L_2 x_2 = G_2 y_2 + L_1 x_1 \quad (3.1)$$

Where  $x_2$  and  $x_1$  are the moles of  $CO_2$  per mole of solvent for lean loading and rich loading.  $y_1$  and  $y_2$  are mole fraction of  $CO_2$  in the exhaust gas entering and leaving the absorber respectively.

The mole fraction of  $CO_2$  in the liquid stream is given by –

$$x_{CO_2} = \frac{\text{No. of moles of } CO_2 \text{ in the stream}}{\text{Total no. of moles in the stream}} \quad (3.2)$$

$$n_{K_2CO_3} = \frac{\text{wt}\%_{K_2CO_3} \times 100gm}{MW_{K_2CO_3}} \quad (3.3)$$

$$n_{H_2O} = \frac{\text{wt}\%_{H_2O} \times 100gm}{MW_{H_2O}} \quad (3.4)$$

$$n_{CO_2} = n_{K_2CO_3} * \text{Loading} \quad (3.5)$$

Where  $n_i$  is the no. of moles of component i,  $MW_i$  is the molecular weight of component i,  $wt.\%$  is the percent weight fraction of component i,  $x_i$  is the mole fraction of the component i and 100gm is assumed as the basis for the solution.

The  $CO_2$  absorption rate or capture rate of the absorber is represented as –

$$CO_2 \text{ Capture rate}(\%) = \frac{\text{amount of } CO_2 \text{ captured}}{\text{amount of } CO_2 \text{ entering}} 100(\%) \quad (3.6)$$

From Table 1, we can obtain the exhaust flow rate,  $G_1$  and the amount of  $CO_2$ ,  $y_1$  in the exhaust stream. Hence, the molar flow rate of  $CO_2$  entering the absorber can be calculated by the following equation.

$$n_1 = y_1 G_1 \quad (3.7)$$

Assuming a  $CO_2$  capture rate of 60%, the molar flow rate of  $CO_2$  in the exhaust stream leaving the absorber can be calculated using the following equation.

$$CO_2 \text{ Capture rate}(\%) = \frac{n_1 - n_2}{n_1} 100(\%) \quad (3.8)$$

With the newly obtained value of  $n_2$ , the exhaust flow rate leaving the absorber,  $G_2$  can be determined by using the following equation.

$$G_2 = G_1 - n_1 + n_2 \quad (3.9)$$

Hence, the  $CO_2$  composition in the exhaust stream leaving the absorber,  $y_2$  can be determined by the following equation.

$$y_2 = \frac{n_2}{G_2} \quad (3.10)$$

The amount of CO<sub>2</sub> removed from the exhaust stream in the absorber is modelled physically in GT-Suite® using an EjectorConn™ template. The EjectorConn™ extracts the calculated amount of CO<sub>2</sub> from the exhaust stream for the 13 SET operating points. The input parameters of EjectorConn™ requires the ejection rate of CO<sub>2</sub> from the exhaust stream. An absorber model using Radfrac™ template is designed in Aspen Plus with exhaust parameters of B50 operating point as the input which gives a capture efficiency of 64%. Hence, assuming a CO<sub>2</sub> capture rate of 60% for B50 point, the amount of CO<sub>2</sub> captured is calculated using equations 3.6 – 3.10 for all the SET operating points. The rate of CO<sub>2</sub> captured is then added to the solvent stream using an InjRateConn™ template. The input parameters of the InjRateConn™ are the rate of CO<sub>2</sub> captured and the temperature of the CO<sub>2</sub> stream. The temperature of the CO<sub>2</sub> stream is kept at 40°C since the absorption process is assumed to operate at 40°C.

A CO<sub>2</sub> Injector template is used in GT-Suite® to add the CO<sub>2</sub> removed from exhaust gas to the solvent stream. The CO<sub>2</sub> flow rate and the temperature at which it is injected are provided as input. The CO<sub>2</sub> flow rate can be calculated from the exhaust gas flow rate and CO<sub>2</sub> capture rate.

### 3.2.1.1. Exhaust gas parameters

The engine operating condition determines the flow rate, CO<sub>2</sub> composition, temperature and pressure of the exhaust gas. In this work, the system was designed based on the exhaust conditions at the “B50” operating point that represents a mid-load, mid-speed condition from the Supplemental Emissions Test (SET) data of a Cummins ISX15 engine with aftertreatment system. The operating points representing the exhaust parameters from idle to full-load conditions in the engine map are listed in Table 3.1.

Table 3.1. Exhaust gas parameters for the SET operating points

| <b>SET<br/>Points</b> | <b>Temperature<br/>(°C), T<sub>1</sub></b> | <b>Flow rate<br/>(kg/hr), G<sub>1</sub> or<br/><math>\dot{m}_{\text{exhaust}}</math></b> | <b>CO<sub>2</sub><br/>Composition<br/>(%), y<sub>1</sub></b> | <b>Pressure<br/>(kPa), P<sub>1</sub></b> |
|-----------------------|--|--|--|--|
| A25                   | 322.8                                      | 412.62   | 7.45   | 3.19                                     |
| A50                   | 380.4                                      | 626.28   | 9.17   | 5.73                                     |
| A75                   | 419.8                                      | 832.68   | 10.12  | 9.13                                     |
| A100                  | 429.6                                      | 1117.14  | 10.18  | 13.5                                     |
| B25                   | 337.9                                      | 496.92   | 7.46   | 3.99                                     |
| B50                   | 354.4                                      | 811.44   | 8.33   | 7.6                                      |

|      |       |         |      |       |
|------|-------|---------|------|-------|
| B75  | 378.5 | 1089.9  | 9.09 | 11.98 |
| B100 | 406.1 | 1405.5  | 9.48 | 17.83 |
| C25  | 331.8 | 586.68  | 7.05 | 4.98  |
| C50  | 336.8 | 922.8   | 7.89 | 8.95  |
| C75  | 368.8 | 1203.42 | 8.76 | 13.35 |
| C100 | 412.2 | 1477.92 | 9.36 | 19.24 |
| Idle | 193   | 154.14  | 2.35 | 0.15  |

An EndFlowInlet™ template in GT Library labelled as EndFlowInlet-Exhaust-in is used to provide the input parameters of the exhaust gas as shown in Table 3.1 in the GT model.

### 3.2.1.2. Absorbent liquid or Solvent

The absorbent liquid or solvent chosen for CO<sub>2</sub> absorption studied in this work was potassium carbonate (K<sub>2</sub>CO<sub>3</sub>) solution due to its non-volatility and negligible solvent losses associated with degradation. High potassium carbonate concentration is preferable due to increased CO<sub>2</sub> carrying capacity, however solvent viscosity and solid precipitation impose limits on the maximum practical concentration. According to the studies performed by Benson et. al. (1954) for a

K<sub>2</sub>CO<sub>3</sub> system, it was found that at 50 and 60 wt.% solution, the precipitation occurs around their respective boiling points before the bicarbonate conversion exceeds 50%. But, in case of 40 wt% solution, the precipitation doesn't occur at its boiling point until bicarbonate conversion of 90%. Hence, the solvent used in this work is 40 wt% K<sub>2</sub>CO<sub>3</sub> solution which is also the preferred expression for most gas treatments.

#### **3.2.1.3. Solvent or liquid rate selection**

The absorber performance for a given gas flow rate and CO<sub>2</sub> concentration depends on the dimensions of the absorber, the flow rate of the solvent, and the inlet CO<sub>2</sub> concentration (or lean loading) of the solvent. A solvent with a low flow rate loads up quickly decreasing the absorption rate. Although a lower lean loading can keep the CO<sub>2</sub> absorption rate constant, it requires a considerably large amount of energy to regenerate the solvent at the stripper. At a higher solvent flow rate, the amount of CO<sub>2</sub> removal can be constant with higher lean loading while reducing the energy for solvent regeneration. However, very high solvent rates lead to a higher sensible heat and increases the loading from the solvent feed to the stripper thereby affecting its vapor-liquid equilibrium. For a given exhaust CO<sub>2</sub> capture rate, an optimum solvent rate and lean loading can be determined.

#### **3.2.1.4. Vapor-Liquid Equilibrium**

The vapor-liquid equilibrium (VLE) of CO<sub>2</sub> in aqueous K<sub>2</sub>CO<sub>3</sub> is affected by the physical solubility of gaseous CO<sub>2</sub> in the solvent and the chemical equilibrium



between the CO<sub>2</sub> dissolved and the other species in the solvent. The physical solubility of gaseous CO<sub>2</sub> in the solvent is expressed using Henry's law.

$$P_{CO_2}^* = H_{CO_2-solvent} x_{CO_2} = H_{CO_2-water} x_{CO_2} y_{CO_2} \quad (3.11)$$

The dissolved CO<sub>2</sub> is in chemical equilibrium with the K<sub>2</sub>CO<sub>3</sub> products and CO<sub>2</sub> products. The total CO<sub>2</sub> in the liquid phase is the sum of the dissolved CO<sub>2</sub> and the other species containing CO<sub>2</sub> products.

$$[CO_2]_T = [CO_2] + [CO_3^{2-}] + [HCO_3^-] \quad (3.12)$$

The [CO<sub>2</sub>] in liquid phase is very low at most conditions due to the strong effect of the chemical reactions. So, in most CO<sub>2</sub> VLE representations, [CO<sub>2</sub>]<sub>T</sub> is used instead of CO<sub>2</sub>.

### 3.2.1.5. Cyclic Capacity

The CO<sub>2</sub> carrying capacity, or the cyclic capacity is the difference in CO<sub>2</sub> concentration between rich and lean CO<sub>2</sub> loading. It is expressed as the amount of CO<sub>2</sub> removed per unit mass of solvent. With a higher cyclic capacity, less amount of solvent is required for the same removal. Hence, the cyclic capacity is an important parameter in determining the sensible heat requirement, pump work, size and cost of the absorbent-absorbent heat exchanger or cross exchanger. The CO<sub>2</sub> capacity is expressed as the product of the delta loading or CO<sub>2</sub> carrying effectiveness and the concentration of the alkalinity in the solvent.

$$\Delta C_{solve} = (\alpha_{rich} - \alpha_{lean}) C_{K_2CO_3} \quad (3.13)$$

Where  $C_{K_2CO_3}$  is the concentration of  $K_2CO_3$  in the solvent. Delta loading is determined by the solvent  $CO_2$  VLE curve at  $40^\circ C$ . At a given mass concentration, the molar concentration of the absorbent is inversely proportional to its molecular weight so solvents with smaller molecular weights are preferred than that with bigger molecules, all else being equal.

### 3.2.1.6. Performance Parameters

The mass transfer driving force in the absorber is an important variable in the design of the process. The  $P_{CO_2}^*$  in the solvent must be smaller than the  $P_{CO_2}$  in the gas in the entire column to provide a positive driving force for the mass transfer. An absorber design that allows large mass transfer driving force to require less area and cost, but it can increase regeneration energy cost by producing irreversibility in the process. The overall mass transfer is given by –

$$N = K_G a (P_{CO_2} - P_{CO_2}^*) \quad (3.14)$$

Where  $N$  is the molar flux of  $CO_2$ ,  $K_G$  is the overall mass transfer coefficient,  $a$  is the effective area and  $P_{CO_2} - P_{CO_2}^*$  is the driving force. Typically, a log mean driving force, reflecting the driving force at the top and bottom of the column is used to estimate the flux if  $K_G$  and  $a$  are known.

### 3.2.2. Regenerator/ Stripper

The solvent with rich  $CO_2$  loading is sent to the stripper at a higher temperature (typically  $80-150^\circ C$ ) where the  $CO_2$  molecules are released from the

K<sub>2</sub>CO<sub>3</sub> solution. After release of the CO<sub>2</sub> from the solvent, the CO<sub>2</sub> is sent to the condenser while the solvent with lean CO<sub>2</sub> loading circulates back to the absorber to absorb more CO<sub>2</sub> from the exhaust gas.

#### **3.2.2.1. Stripper Temperature**

A higher stripper operating temperature decreases the energy requirement for the process but can increase the rate of solvent loss due to degradation. Hence, the stripper temperature selection involves a trade-off between solvent loss and energy demands. Using an assumption for the acceptable rate of degradation of the solvent, the maximum stripper temperature ( $T_{\max}$ ) can be calculated from the first order degradation rate and the activation energy of the Arrhenius equation. Being an inert salt, K<sub>2</sub>CO<sub>3</sub> is not prone to degradation. Therefore, the stripper temperature is only limited to exhaust enthalpy available at a given temperature.

#### **3.2.2.2. Stripper Pressure**

The stripper pressure will be fixed for a given temperature and loading. Higher stripper pressures reduce the amount of water vaporized per gmol of CO<sub>2</sub>, as well as the compressor work. However, at a given stripper temperature, higher stripper pressures correspond to higher lean loadings, resulting in reduced solvent capacity and greater liquid circulation rates. For two solvents with the same capacity, higher stripper pressure is more desirable as it corresponds to lower compressor and stripping heat and hence lowers overall work. The stripper pressure is the sum of the partial pressure of CO<sub>2</sub>, partial pressure of water and

the partial pressure of solvent at the stripper temperature. The partial pressure of  $\text{CO}_2$  is assumed to be in equilibrium with the lean loading of the solvent at  $T_{\max}$ .

### 3.2.2.3. Modelling the stripper

The VLE behavior of the system is estimated in Aspen Plus® Flash2™ model using an Electrolyte Non-Random Two-Liquid (ELECNRTL) method. The stripper pressure as well as the partial pressure of  $\text{CO}_2$  and water in the solvent is obtained by using a flash calculation. The flash drum separates the incoming stream into vapor and liquid stream. The input parameters of the flash drum include a solvent stream and a  $\text{CO}_2$  stream as shown in Figure 3.3. The solvent stream comprises of a solution of 40 wt%  $\text{K}_2\text{CO}_3$  and water. The  $\text{CO}_2$  stream comprises of  $\text{CO}_2$  loadings that were varied from 0 – 1.0. The temperature of both the solvent stream and  $\text{CO}_2$  stream were varied from  $80^\circ\text{C}$  –  $200^\circ\text{C}$ .

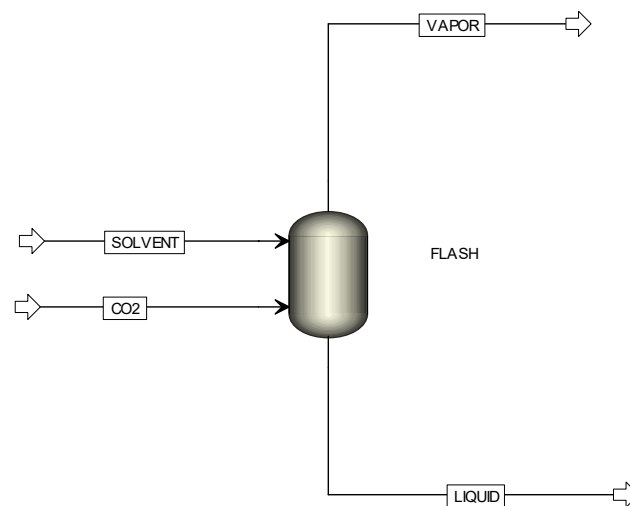


Figure 3.3. Simplified Aspen model flowsheet for Flash

The stripper or flash is represented with the help of a 2D Lookup table with XYZMap™ template in GT-Suite® labelled as Lookup flash. The X data represents the temperature of the solvent stream entering the stripper and is varied from 80-200°C while the Y data represents the CO<sub>2</sub> loading in the solvent stream entering the stripper and is varied from 0-1. The CO<sub>2</sub> loading range from 0-1 is converted to CO<sub>2</sub> mole fraction in the solvent stream before plotting it in the map. The X and Y data are the input parameters in the Lookup table. The Z data represents the total pressure generated at the stripper and is obtained from the flash calculation in Aspen Plus®. The flash generates two output streams: a vapor stream comprising of CO<sub>2</sub> and H<sub>2</sub>O that goes to the condenser and a liquid stream comprising of K<sub>2</sub>CO<sub>3</sub>, H<sub>2</sub>O and CO<sub>2</sub> that goes to the cross exchanger. An actuator is used to provide the output pressure of Lookup flash to the cross exchanger.

#### 3.2.2.4. Regeneration Energy

The total energy generated at the stripper is the sum of the desorption energy, the sensible heat and the evaporation heat and is expressed as –

$$Q_{reg} = Q_{desorption} + Q_{sensible} + Q_{vaporization} \quad (3.15)$$

$Q_{desorption}$  is the enthalpy change associated with CO<sub>2</sub> going from the gas phase to the liquid phase or vice-versa. This enthalpy change is negative (exothermic) for CO<sub>2</sub> absorption and positive for desorption and can be expressed as –

$$Q_{desorption} = -\dot{m}_{CO_2} \Delta H_{absorption} \quad (3.16)$$

The heat of absorption  $\Delta H_{\text{absorption}}$  can be estimated directly from Aspen Plus® or from the temperature dependence of the partial pressure of CO<sub>2</sub> in equilibrium. The vapor pressure data generated by the flash calculation can be used in the Clausius-Clapeyron equation given by equations 3.17 – 3.18.

$$\Delta H_{\text{absorption}} = R \left( \frac{\partial \ln P_{\text{CO}_2}^*}{\partial \frac{1}{T}} \right)_{P, x} \quad (3.17)$$

$$\ln \left( \frac{P_{\text{CO}_2, \text{lean}}^* | T_{\text{max}}}{P_{\text{CO}_2, \text{lean}}^* | 40^\circ\text{C}} \right) = \frac{-\Delta H_{\text{abs}}}{R} \left( \frac{1}{T_{\text{max}}} - \frac{1}{T_a} \right) \quad (3.18)$$

Where  $T_{\text{max}}$  is the maximum stripper temperature,  $R$  is the universal gas constant. The Clausius-Clapeyron equation assumes that molar volume of liquid is negligible relative to the molar volume of vapor and the heat of addition is independent of the temperature (Smith et. al., 1996).

$Q_{\text{sensible}}$  is the amount of energy required to heat the solvent to the stripper temperature.

$$Q_{\text{sensible}} = \frac{\text{flow rate of solvent}}{\text{flow rate of CO}_2} \quad (3.19)$$

Which can also be expressed as –

$$Q_{\text{sensible}} = m_{\text{solvent}, R} C_{p_{\text{solvent}}} \Delta T \quad (3.20)$$

Where  $C_{p_{\text{solvent}}}$  is the specific heat capacity of the solvent at the rich loading (kJ/kgK). The approach temperature  $\Delta T$  is the temperature difference of the solvent from the cross exchanger to the stripper.

$Q_{\text{vaporization}}$  is the amount of heat generated due to vaporization of water from the solvent. When the temperature of the solvent is increased on its way to the stripper, some amount of water is vaporized from the solvent.

$$Q_{\text{vaporization}} = m_{\text{CO}_2} \frac{P_{\text{H}_2\text{O}} \Delta H_{\text{vaporization}, \text{H}_2\text{O}}}{P_{\text{CO}_2}} \quad (3.21)$$

Where  $\Delta H_{\text{vaporization}, \text{H}_2\text{O}}$  is the enthalpy of vaporization of water.  $P_{\text{CO}_2}$  and  $P_{\text{H}_2\text{O}}$  are the partial pressures of  $\text{CO}_2$  and water in the solvent.

### 3.2.3. Heat exchangers

There  $\text{CO}_2$  capture system comprises of two heat exchangers that increases the temperature of the solvent before it is sent to the stripper.

#### 3.2.3.1. Exhaust-Absorbent Heat Exchanger

The exhaust-absorbent heat exchanger reduces the temperature of the exhaust gas coming from the SCR. The heat is rejected to the solvent stream with rich loading leaving the cross exchanger thereby increasing the temperature of the solvent stream to the desired operating temperature of the stripper. The amount of heat rejected also provides the sensible heat, the heat for desorption of  $\text{CO}_2$  and

the heat of vaporization of water. The heat rejected by the exhaust gas is given by

–

$$Q_{exh-abs,HR} = Q_3 = \dot{m}_{exhaust} C_{p_{exhaust}} (T_1 - T_2) \quad (3.22)$$

$Q_{exh-abs,HR}$  is the amount of heat energy rejected by the exhaust stream.  $T_1$  and  $T_2$  are the temperature of the exhaust gas entering and leaving the exhaust-absorbent heat exchanger. The exhaust gas flow rate,  $\dot{m}_{exhaust}$  and temperature,  $T_1$  are obtained from the SET data. The specific heat capacity of exhaust gas is estimated to be 1.014 kJ/kgK. The temperature of the exhaust stream should be maintained at 40-60°C for the CO<sub>2</sub> absorption process, as the carbon molecules break away from the solvent molecular bond at higher temperature. Hence, the outlet temperature of exhaust gas,  $T_2$  is assumed to be 40°C. The effectiveness of the heat exchanger is assumed as 0.85. Hence, the amount of heat rejected is estimated by putting these values in the equation 3.22.

As the heat exchange process occurs with the solvent stream with rich loading leaving the cross exchanger, the amount of heat energy gained by the solvent stream is given by the following equation.

$$Q_{exh-abs,HA} = \dot{m}_{solvent,R} C_{p_{solvent,R}} (T_4 - T_3) = \dot{m}_{solvent,R} C_{p_{solvent,R}} \Delta T_{3-4} \quad (3.23)$$

Where  $Q_{exh-abs,HA}$  is the sensible heat, or the amount of heat energy added to the solvent stream.  $\dot{m}_{solvent,R}$  is flow rate of the solvent and is calculated from the absorber mass balance equation while  $C_{p_{solvent,R}}$  is the specific heat capacity of



the solvent with rich loading, which is obtained from the ELECNRTL method in Aspen Plus®.  $T_4$  and  $T_3$  are the temperatures of the solvent stream with rich loading entering and leaving the exhaust-absorbent heat exchanger and are assumed to have a temperature difference,  $\Delta T_{3-4}$  of 10°C.

The remaining heat energy is used to provide the heat for desorption of CO<sub>2</sub> and the heat of vaporization of water and is given by –

$$Q_{exh-abs,HR} - Q_{exh-a,HA} \quad (3.24)$$

The exhaust-absorbent heat exchanger is modelled in GT-Suite® with an HXMaster™ and HXSlave™ template as shown in Figure 3.4. The rich CO<sub>2</sub> solvent stream passes through the HXMaster™ unit (Exh-Abs\_HX-1) while the exhaust stream passes through the HXSlave™ unit (Exh-Abs\_HX).

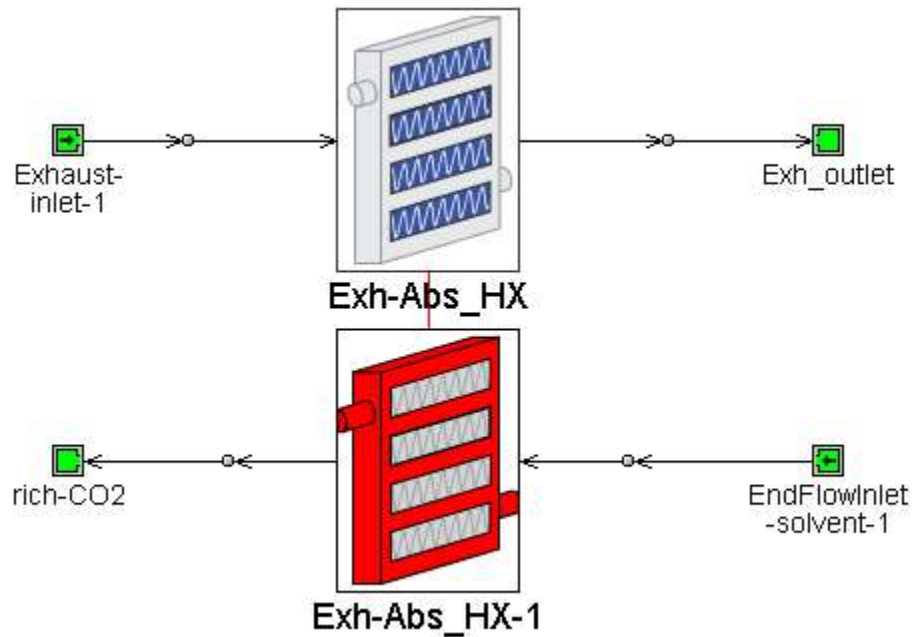


Figure 3.4. GT-Suite model of Exhaust-Absorbent heat exchanger

Table 3.2 and 3.3 shows the input parameters for HXSlave™ and HXMaster™ respectively. The input properties of the solvent such as flow rate and composition are determined from the absorber mass balance equation.

Table 3.2. Input parameters of exhaust gas for HXSlave™ (Exh-Abs\_HX)

|                              |   |
|------------------------------|---|
| Exhaust gas temperature (°C) | 354.4   |
| Pressure (bar)               | 1   |
| Composition (%)              | CO <sub>2</sub> =8.33, H <sub>2</sub> O=3.1, N <sub>2</sub> =62,<br>O <sub>2</sub> =26.57 |
| Exhaust flow rate (kg/s)     | 0.2254  |

Table 3.3. Input parameters of solvent for HXMaster™ (Exh-Abs\_HX -1)

|                                 |     |
|---------------------------------|-----|
| Solvent inlet temperature (°C)  | 110 |
| Solvent outlet temperature (°C) | 120 |

|  |   |
|--|---|
| Solvent Composition (%) and Solvent flow rate (kg/s) | Obtained from absorber mass balance results |
|--|---|

The heat exchanger design specifications are obtained from that of a TubeFin Air-Air Charge Air Cooler (CAC) for a sample truck with scaling object defined. Table 3.4 shows the design specifications of the heat exchanger.

Table 3.4. Heat exchanger design specifications

|                                    |           |
|------------------------------------|-----------|
| Heat exchanger height (mm)         | 672       |
| Heat exchanger width (mm)          | 895       |
| Heat exchanger depth (mm)          | 63        |
| Inlet connection diameter (mm)     | 55        |
| Outlet connection diameter (mm)    | 55        |
| Tube and fin material              | Aluminium |
| Mass of fin and tube material (kg) | 6         |

|                                   |            |
|-----------------------------------|------------|
| Tube wall thickness (mm)          | 1          |
| Number of channels in a tube (mm) | 35         |
| Number of passes                  | 1          |
| Number of tubes per pass          | 50         |
| Tube flow orientation             | Horizontal |

### 3.2.3.2. Absorbent-Absorbent Heat Exchanger

The absorbent-absorbent heat exchanger or cross exchanger increases the temperature of the solvent stream with rich loading coming from the absorber before it goes to the stripper. The heat exchange process occurs between the cold rich solvent stream leaving the absorber and the hot lean solvent stream coming out of the stripper. The amount of heat rejected is given by the following equation.

$$Q_{cross,HR} = Q_4 = m_{solvent,R} C_{p_{solvent,R}} (T_3 - T_2) = m_{solvent,R} C_{p_{solvent,R}} \Delta T_{2-3} \quad (3.25)$$

Where  $Q_{cross,HR}$  is the heat rejected by the solvent stream with rich loading,  $\dot{m}_{solvent,R}$  is flow rate of the solvent with rich loading and is calculated from the absorber mass balance equation and  $C_{p_{solvent,R}}$  is the specific heat capacity of the solvent

with rich loading that is obtained from the ELECNRTL method in Aspen Plus®.  $T_2$  and  $T_3$  are the temperatures of the solvent stream with rich loading entering and leaving the cross exchanger respectively.  $T_2$  is maintained at 40°C as assumed in the absorber. As we have considered an approach temperature of 10°C for the sensible heat in the regenerator,  $T_3$  is assumed to be 110°C. The heat exchanger effectiveness is assumed as 0.85.

The heat transfer occurs with the hot liquid stream or lean solvent stream leaving the stripper or flash. Hence, the amount of heat energy gained by the solvent stream with lean loading is given by the following equation.

$$Q_{cross,HA} = \dot{m}_{solvent,L} C_{p,solvent,L} (T_4 - T_5) = \dot{m}_{solvent,L} C_{p,solvent,L} \Delta T_{5-4} \quad (3.26)$$

Where  $Q_{cross,HA}$  is the amount of heat energy added to the solvent stream with lean loading.  $\dot{m}_{solvent,L}$  is flow rate of the solvent with lean loading and is calculated from the absorber mass balance equation and  $C_{p,solvent,L}$  is the specific heat capacity of the solvent with lean loading that is obtained from the ELECNRTL method in Aspen Plus®.  $T_4$  is the temperature of the solvent stream leaving the stripper and is at the same temperature as the stripper while  $T_5$  is the temperatures of the solvent stream with lean loading leaving the cross exchanger and entering the trim cooler.

The cross exchanger is modelled using an HXMaster™ and HXSlave™ template in GT-Suite® as shown in Figure 3.5, where the solvent with rich CO<sub>2</sub> loading passes through the HXMaster™ (Cross\_EX-1) and the solvent with lean CO<sub>2</sub> loading passes through the HXSlave™ unit (Cross\_EX).

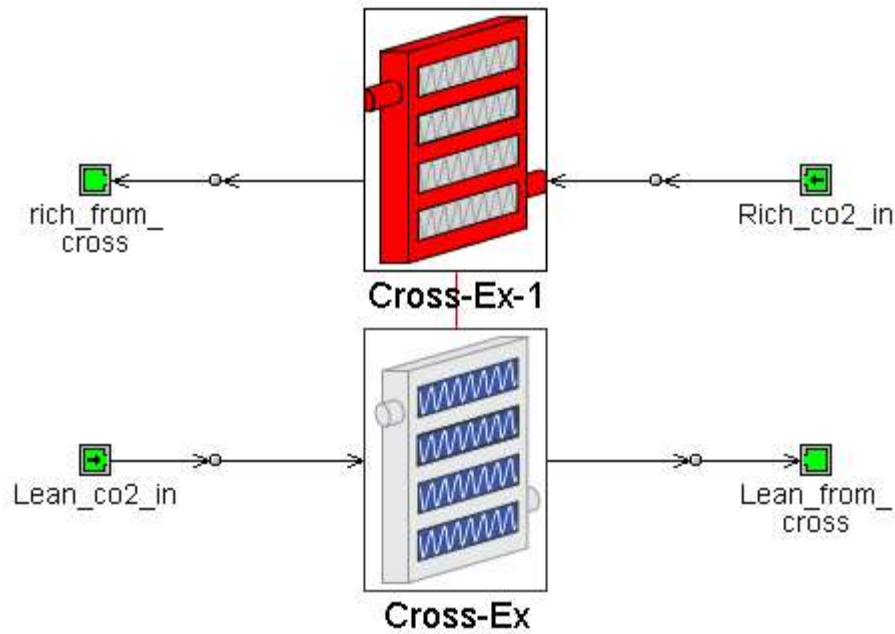


Figure 3.5. GT-Suite model of Cross exchanger

The heat exchanger specifications are kept same as that of exhaust-absorbent heat exchanger shown in Table 3.4. Table 3.5 and Table 3.6 lists the input parameters for the two units. The solvent flow rates and composition for both streams are calculated from the absorber mass balance equation.

Table 3.5. Input parameters of rich solvent for HXMaster™ (CrossEx-1)

|  |     |
|--|-----|
| Rich CO <sub>2</sub> solvent inlet temperature (°C)  | 40  |
| Rich CO <sub>2</sub> solvent outlet temperature (°C) | 110 |

|   |  |
|---|--|
| Solvent Composition (%) and Solvent<br>flow rate (kg/s) | Obtained from absorber mass<br>balance results |
|---|--|

Table 3.6. Input parameters of lean solvent for HXSlave™ (CrossEx)

|   |  |
|---|--|
| Lean CO <sub>2</sub> solvent inlet temperature (°C)     | 120  |
| Lean CO <sub>2</sub> solvent outlet temperature (°C)    | 50   |
| Solvent Composition (%) and Solvent<br>flow rate (kg/s) | Obtained from absorber mass<br>balance results |

#### 3.2.4. Cooler

The CO<sub>2</sub> capture system comprises of a trim cooler that brings down the temperature of the solvent stream coming from the stripper to the temperature required for the CO<sub>2</sub> absorption process.

### 3.2.4.1. Trim Cooler

The trim cooler maintains the temperature required for the absorber after the solvent circulates back from the high temperature stripper. The amount of heat rejected by the trim cooler is given by –

$$Q_{trim} = Q_5 = \dot{m}_{solvent,L} C_{p_{solvent,L}} (T_5 - T_2) = \dot{m}_{solvent,L} C_{p_{solvent,L}} \Delta T_{2-5} \quad (3.28)$$

Where  $\dot{m}_{solvent,L}$  is flow rate of the solvent with lean CO<sub>2</sub> and is calculated from the absorber mass balance equation and  $C_{p_{solvent,L}}$  is the specific heat capacity of the solvent with lean loading which is obtained from the ELECNRTL method in Aspen Plus®.  $T_5$  and  $T_2$  are the temperatures of the solvent stream with lean loading entering and leaving the trim cooler.  $T_2$  is assumed as 40°C in the absorber due to the low temperature requirement of the CO<sub>2</sub> absorption process. The temperature difference of the trim cooler,  $\Delta T_{2-5}$  is assumed as 10°C.

The trim cooler is modelled using an HXMaster™ and HXSlave™ template in GT-Suite® as shown in Figure 3.7. Water is passed through the HXMaster™ unit (Trim-cooler-1) while the solvent stream with lean CO<sub>2</sub> exiting the cross exchanger passes through the HXSlave™ unit (Trim-cooler).



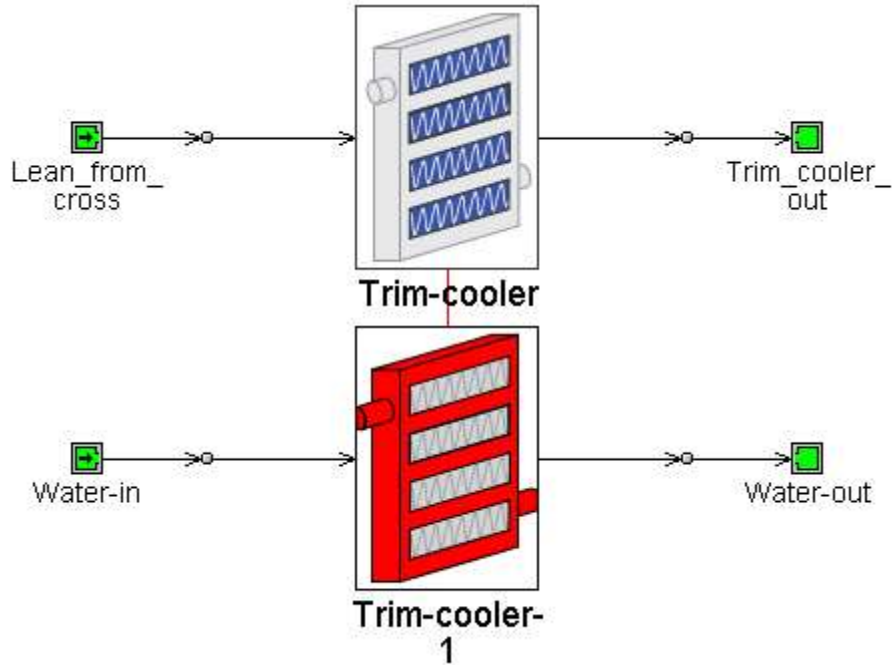


Figure 3.6. GT-Suite model of Trim cooler

The heat exchanger specifications are kept same as that of exhaust-absorbent heat exchanger as shown in Table 3.4. The input parameters of the two units are listed in Table 3.9 and 3.10.

Table 3.7. Input parameters of lean CO<sub>2</sub> solvent for HXSlave™ (TrimCooler)

|  |    |
|--|----|
| Lean CO <sub>2</sub> solvent inlet temperature (°C)  | 50 |
| Lean CO <sub>2</sub> solvent outlet temperature (°C) | 40 |

|   |  |
|---|--|
| Solvent Composition (%) and Solvent<br>flow rate (kg/s) | Obtained from absorber mass<br>balance results |
|---|--|

### 3.2.5. Condenser

The condenser condenses the vapor stream leaving the stripper or flash before it enters the compressor. The vapor stream comprises of CO<sub>2</sub> and H<sub>2</sub>O. After leaving the condenser, the water from the stream is drained and is recirculated back into the stripper. The condensed CO<sub>2</sub> stream then goes to the compressor where it is compressed for storage.

The cooling duty for steam or the amount of heat rejected due to vaporization of water is given by the following equation.

$$Q_{H_2O} = \dot{m}_{H_2O} \Delta H_{\text{vaporization}, H_2O} \quad (3.29)$$

Where  $\dot{m}_{H_2O}$  is the mass flow rate of water in the vapor stream and  $\Delta H_{\text{vaporization}, H_2O}$  is the latent heat of vaporization of water. The latent heat of vaporization of water is 2257 kJ/kgK.

The amount of heat rejected in condensing CO<sub>2</sub> is given by equation 3.30.

$$Q_{CO_2} = \dot{m}_{CO_2} C_{p_{CO_2}} (T_4 - T_6) \quad (3.30)$$

Where  $\dot{m}_{CO_2}$  is the mass flow rate of CO<sub>2</sub> in the vapor stream and  $C_{pCO_2}$  is the specific heat capacity of CO<sub>2</sub>.  $T_4$  is the temperature of the vapor stream leaving the stripper while  $T_6$  is the outlet temperature of the stream leaving the condenser, which we have assumed as 40°C.

The flash calculation in Aspen Plus® provides the total pressure at the stripper,  $P_{total}$  and the mole fraction of CO<sub>2</sub>,  $y_{CO_2}$  and mole fraction of H<sub>2</sub>O,  $y_{H_2O}$  in the vapor stream for a temperature of 80-200°C and a CO<sub>2</sub> loading of 0-1. Using the Dalton's law of partial pressure, we can calculate the mole fraction of CO<sub>2</sub> and H<sub>2</sub>O using the following equations.

$$P_{CO_2} = y_{CO_2} P_{total} \quad (3.31)$$

$$P_{H_2O} = y_{H_2O} P_{total} \quad (3.32)$$

Using equations 3.31 and 3.32, we can obtain the partial pressure of CO<sub>2</sub> and H<sub>2</sub>O for a temperature range of 80-200°C and a CO<sub>2</sub> loading of 0-1. The data obtained for both partial pressure of CO<sub>2</sub> and H<sub>2</sub>O are plotted in 2D Lookup tables using XYZMap™ template in GT-Suite®. The lookup table for partial pressure of CO<sub>2</sub> is labelled as Lookup\_flash-CO<sub>2</sub> and the lookup table for partial pressure of H<sub>2</sub>O is labelled as Lookup\_flash-H<sub>2</sub>O. The input parameters for both tables comprises of the flash output temperature of 80-200°C as X data and CO<sub>2</sub> loading of 0-1 converted to mole fractions of CO<sub>2</sub> in the solvent stream as Y data. The Z data gives the partial pressure of CO<sub>2</sub> and the partial pressure of H<sub>2</sub>O as the output. The output pressure from both the lookup tables is sensed by an actuator and is

provided as an input to the condenser. Using the temperature and the partial pressure of  $\text{CO}_2$  and  $\text{H}_2\text{O}$  as inputs, we can calculate the cooling duty for steam and  $\text{CO}_2$  in the condenser.

The condenser is modelled in GT-Suite® with an HXMaster™ and HXSlave™ template as shown in Figure 3.8. Water is passed through the HXMaster™ unit (Condenser-1). The  $\text{CO}_2$  vapor stream from lookup table for partial pressure of  $\text{CO}_2$  (Lookup\_flash- $\text{CO}_2$ ) and the  $\text{H}_2\text{O}$  vapor stream from lookup table for partial pressure of  $\text{H}_2\text{O}$  (Lookup\_flash- $\text{H}_2\text{O}$ ) passes through the HXSlave™ unit (Condenser-2).

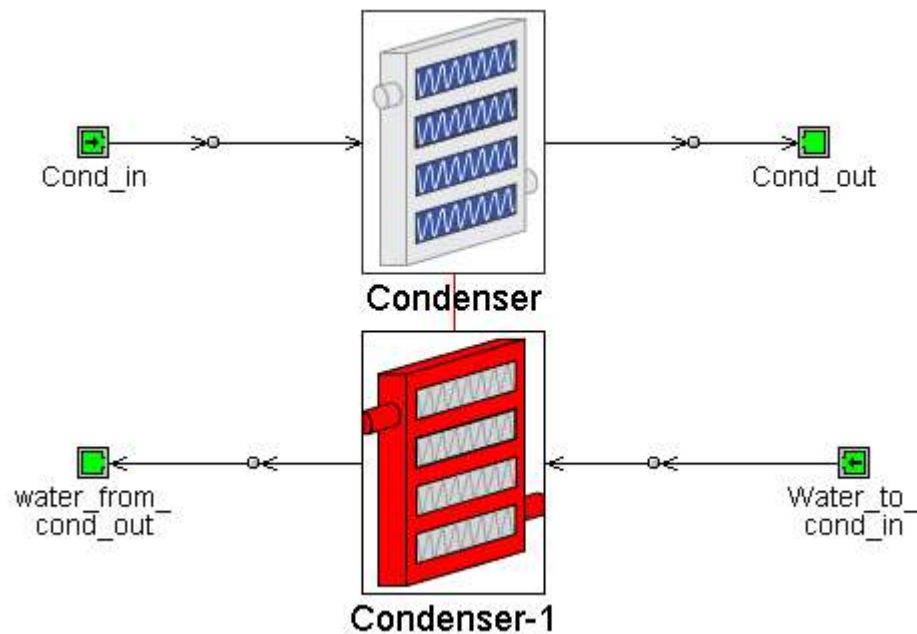


Figure 3.7. GT-Suite model of Condenser

The condenser specifications are kept same as that of exhaust-absorbent heat exchanger as shown in Table 3.4. The input parameters for HXMaster™ and HXSlave™ for the condenser at B50 operating point are listed below.

Table 3.8. Input parameters of vapor stream from flash for HXSlave™  
(Condenser)

|                                     |                                   |
|-------------------------------------|-----------------------------------|
| Vapor stream inlet temperature (°C) | 120                               |
| Outlet temperature (°C)             | 40                                |
| Composition                         | H <sub>2</sub> O, CO <sub>2</sub> |
| CO <sub>2</sub> flow rate (kg/s)    | 0.01                              |
| H <sub>2</sub> O flow rate (kg/s)   | 0.068                             |

### 3.2.6. Compressor

The compressor compresses the incoming stream of CO<sub>2</sub> from the stripper through the condenser for storing it in the tank. The CO<sub>2</sub> stream remains in the vapor form when it enters the compressor. Assuming isentropic compression, the compressor work is calculated using an empirical correlation developed by Van Wagner (2011), given by –

$$W_{comp} = \frac{4.572 * \ln\left(\frac{P_{out}}{P_{in}}\right) - 4.096}{\eta_{comp}} \quad (3.33)$$

Where  $P_{out}$  is the pressure at which the  $CO_2$  would be compressed before storage and  $P_{in}$  is the pressure of the vapor stream coming out of the stripper.  $\eta_{comp}$  is the efficiency of the compressor.

A PumpFlow™ template is used to model the compressor in GT-Suite® that determines the work required to compress the  $CO_2$  stream exiting the condenser.

The input parameters for the compressor are shown in Table 3.13.

Table 3.9. Input parameters of the compressor (PumpFlow™)

|  |  |
|--|--|
| Mass flow rate of $CO_2$ stream (kg/s) | 0.01   |
| Inlet Pressure, $P_{in}$ (bar)         | Total pressure generated in stripper<br>at 120°C |
| Outlet Pressure, $P_{out}$ (bar)       | 100  |
| Isentropic efficiency (%)              | 85   |

The heat exchangers, coolers and condenser, modelled individually in GT-Suite® are then integrated along with the lookup tables for total pressure and the partial pressure of CO<sub>2</sub> and H<sub>2</sub>O to form the CO<sub>2</sub> capture system as shown in Figure 3.9.



55

increases the solvent temperature to the desired temperature of the stripper. The green lines from the exhaust-absorbent heat exchanger senses the temperature input while the pink lines from the cross exchanger senses the CO<sub>2</sub> loading which is converted to CO<sub>2</sub> mole fraction. Three lookup tables are generated for total pressure (Lookup-flash), partial pressure of CO<sub>2</sub> (Lookup-CO<sub>2</sub>) and partial pressure of H<sub>2</sub>O (Lookup-H<sub>2</sub>O) at the stripper as a function of temperature and CO<sub>2</sub> loading or CO<sub>2</sub> mole fraction. The vapor stream from the stripper is sent to the condenser while the liquid stream is sent to the cross exchanger and the trim cooler where more CO<sub>2</sub> is injected from exhaust gas. The output from the Lookup-CO<sub>2</sub> and the Lookup-H<sub>2</sub>O is actuated to the vapor stream entering the condenser. A switch is provided to send the pressure output for either CO<sub>2</sub> stream or H<sub>2</sub>O stream at one time, to the condenser. The One-1 senses the temperature input to the condenser and the cross-exchanger. The compressor is connected to the condenser to compress the CO<sub>2</sub> to the desired pressure.



## Chapter 4

### Results and Discussion

This chapter discusses the results obtained from the VLE behavior of the system and the heat rate for different operating points along with the thermodynamic and chemical calculations in the CO<sub>2</sub> capture system and its subcomponents.

#### 4.1. Results from Aspen Plus® Flash

The flash drum is maintained at a temperature of 120°C and comprises of two input streams: one stream had 40 wt.% K<sub>2</sub>CO<sub>3</sub> and water while the other stream had CO<sub>2</sub> loading. Using sensitivity analysis, the temperature of the two input streams are varied from 80°C – 200°C. The CO<sub>2</sub> loading was varied from 0 – 1.0 which was converted to mole fraction of CO<sub>2</sub> in the solvent stream. The flash drum generates two output streams: a vapor stream and a liquid stream. The vapor stream comprises of CO<sub>2</sub> and H<sub>2</sub>O and is sent to the condenser while the liquid stream circulates back as the solvent to absorb more CO<sub>2</sub> from the absorber. The total pressure generated in the stripper is represented as a function of the

temperature of the solvent stream exiting the exhaust-absorbent heat exchanger and the CO<sub>2</sub> loading in the same. Figure 4.1 shows the plot of total pressure generated in the stripper for a temperature range of 80°C – 200°C and a CO<sub>2</sub> loading of 0 – 1.0 in the solvent stream.

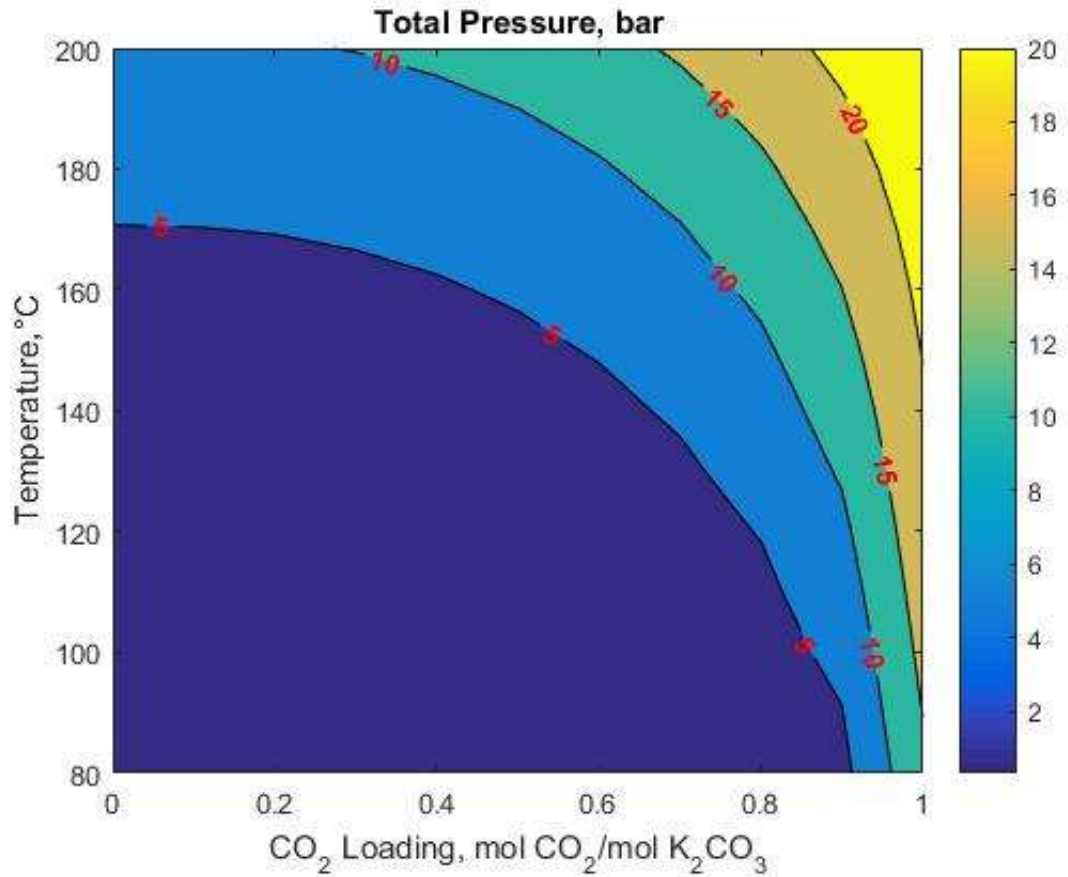


Figure 4.1. Total pressure at the stripper at a temperature of 80 – 200°C and CO<sub>2</sub> loading from 0 – 1.0.

#### **4.1.1. Calculation of partial pressure of CO<sub>2</sub> and H<sub>2</sub>O**

The total pressure generated at the stripper can be expressed as the sum of the partial pressures of CO<sub>2</sub>, H<sub>2</sub>O and K<sub>2</sub>CO<sub>3</sub>. Using sensitivity analysis for the flash drum, the composition of the individual components were calculated for both vapor and liquid stream. Using the Dalton's law of partial pressure, the partial pressure of CO<sub>2</sub> and H<sub>2</sub>O in the stripper were calculated as a function of the temperature and CO<sub>2</sub> loading of the solvent inlet stream and are shown in Figure 4.2 and 4.3 respectively. The partial pressure of CO<sub>2</sub> and H<sub>2</sub>O obtained from the results are then used to determine the heat of vaporization of water at the stripper to calculate the total regeneration energy required for the CO<sub>2</sub> desorption process.

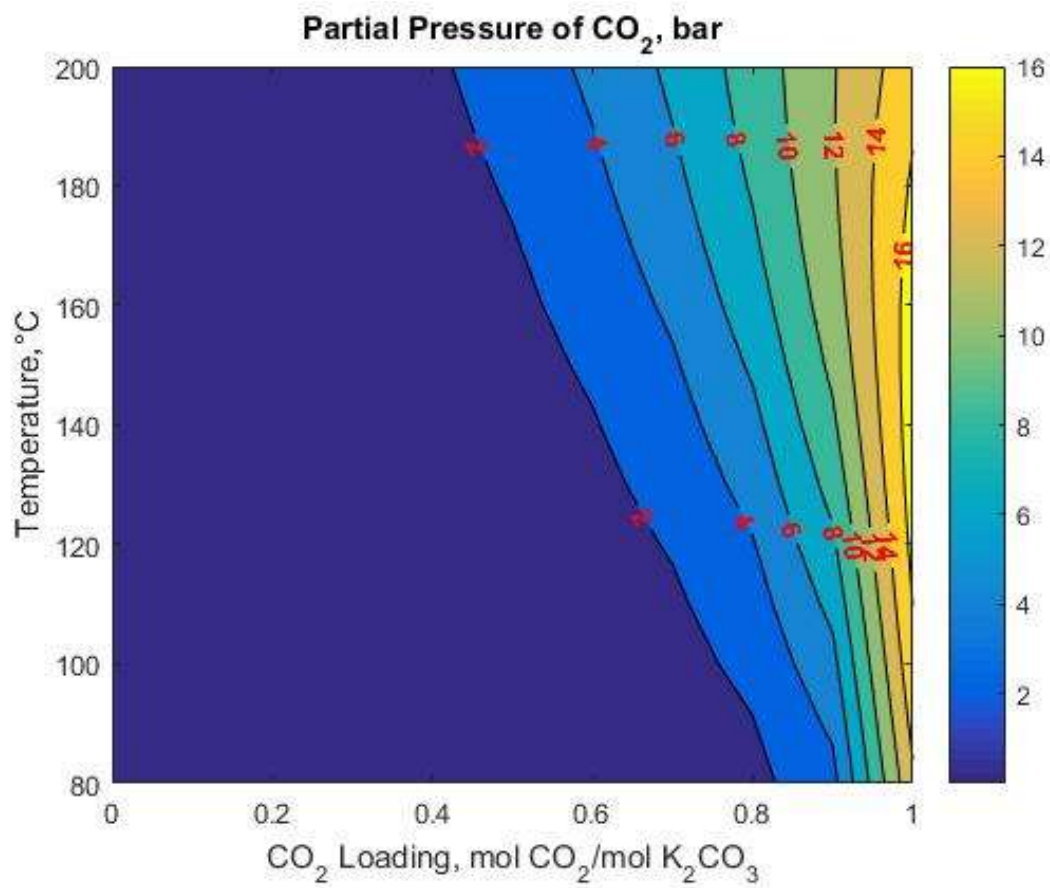


Figure 4.2. Partial pressure of CO<sub>2</sub> at a temperature of 80 – 200°C and CO<sub>2</sub> loading from 0 – 1.0.

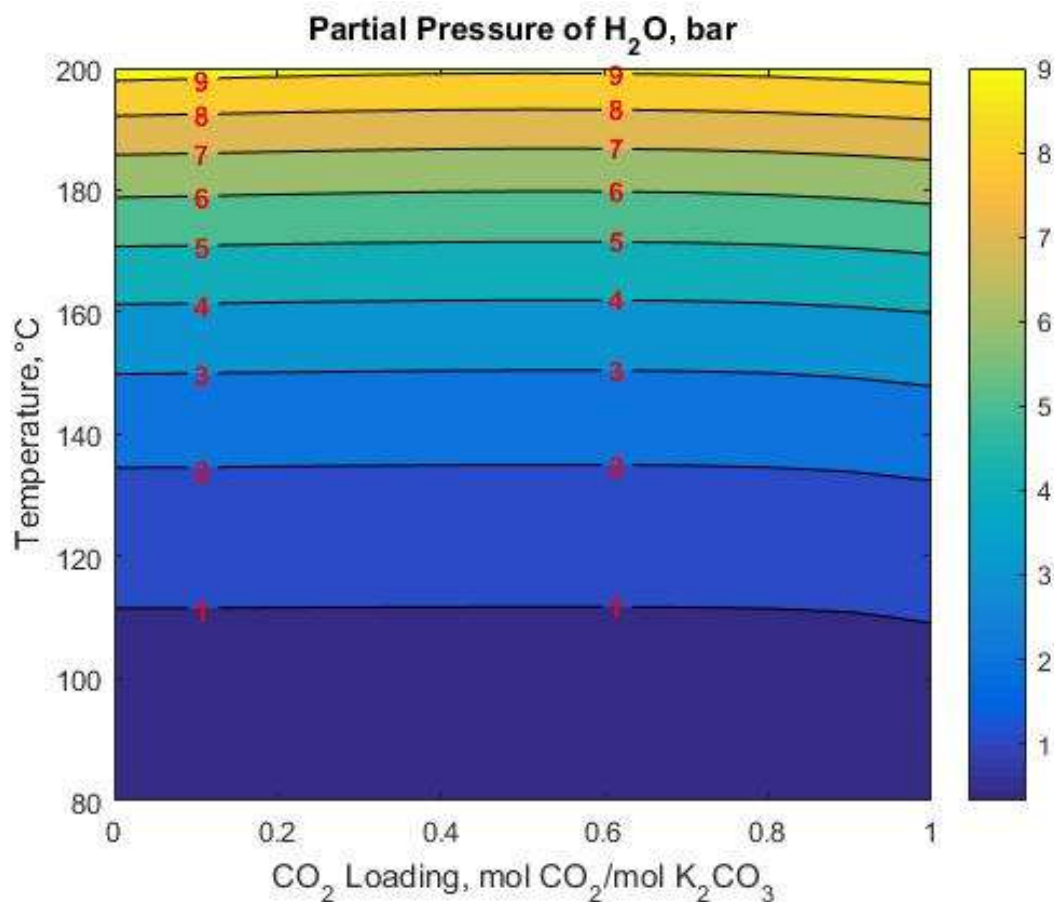


Figure 4.3. Partial pressure of H<sub>2</sub>O at a temperature of 80 – 200°C and CO<sub>2</sub> loading from 0 – 1.0.

#### 4.1.2. Vapor Liquid Equilibrium in 40 wt.% K<sub>2</sub>CO<sub>3</sub> system

In 1959, Tosh et. al conducted equilibrium studies in a rocking autoclave unit and determined the equilibrium behavior of K<sub>2</sub>CO<sub>3</sub>-KHCO<sub>3</sub>-CO<sub>2</sub>-H<sub>2</sub>O system with 40 wt.% K<sub>2</sub>CO<sub>3</sub> for a temperature range of 343 – 413 K. The VLE results are obtained for 40 wt.% K<sub>2</sub>CO<sub>3</sub> by using flash calculations in Aspen Plus® for a temperature range of 80 – 200°C. Figure 4.4 shows a comparison of the

experimental results from Tosh and Aspen results from flash for a temperature of 110°C and 130°C. There is a slight deviation of the Aspen values from those of the experimental values. The deviation is significant especially in case of higher temperature and loadings. The solution would remain close to a temperature around 110°C which is the boiling point of the solvent with 40 wt.%  $K_2CO_3$ .

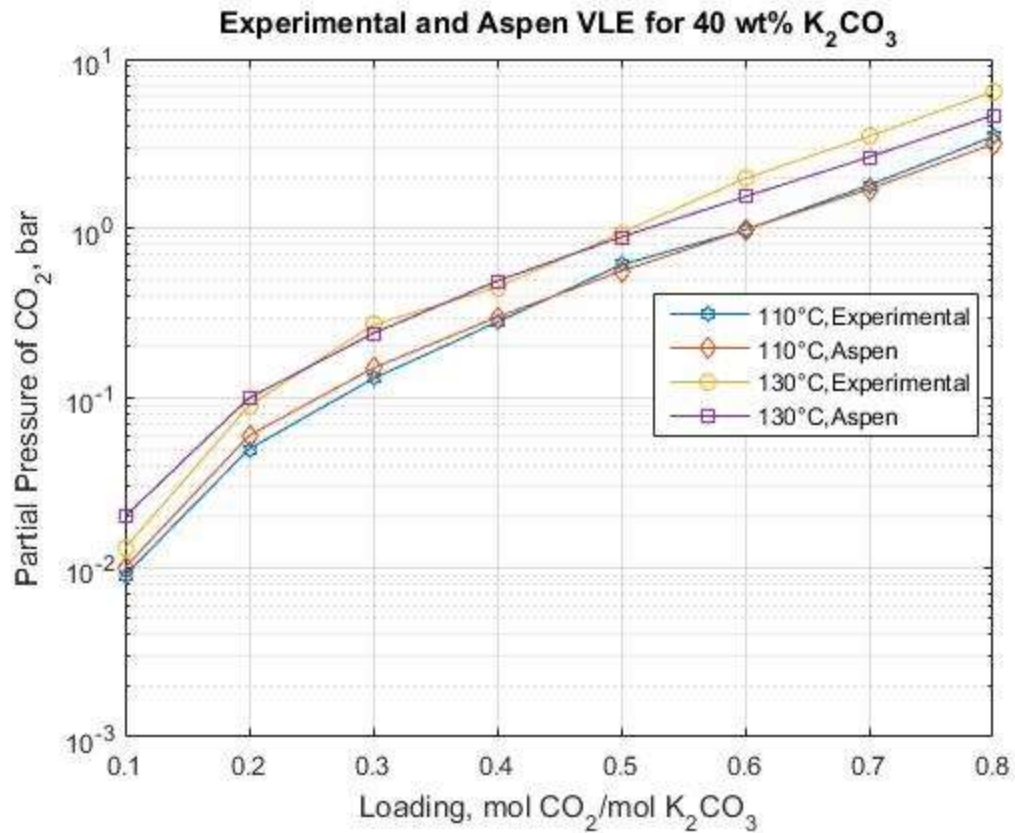


Figure 4.4. Comparison of the experimental behavior from Tosh et. al (1959) and Aspen VLE at a temperature of 110°C and 130°C

## 4.2. Calculation of Absorber parameters

For the operating point B50, the gas flow rate leaving the absorber,  $G_2$  and the  $\text{CO}_2$  composition of the exhaust stream leaving the absorber,  $y_2$  can be calculated using equations 3.6 – 3.10. From Table 3.1 and using equation 3.7, the molar flow rate of  $\text{CO}_2$  entering the absorber can be estimated.

$$n_1 = y_1 G_1$$

$$n_1 = 0.0833 \left( \frac{\text{mol}}{\text{mol}} \right) * \frac{811.44 \left( \frac{\text{kg}}{\text{hr}} \right)}{29 \left( \frac{\text{g}}{\text{mol}} \right)}$$

$$n_1 = 0.647 \frac{\text{mol}}{\text{s}}$$

With a  $\text{CO}_2$  capture rate of 60%, the molar flow rate of  $\text{CO}_2$  in the exhaust stream leaving the absorber can be calculated using the following equation.

$$\text{CO}_2 \text{ Capture rate}(\%) = \frac{n_1 - n_2}{n_1} 100(\%)$$

$$60 = \frac{n_1 - n_2}{n_1} 100(\%)$$

$$60 = \frac{0.647 - n_2}{0.647} 100(\%)$$

$$n_2 = 0.258 \frac{\text{mol}}{\text{s}}$$

With the newly obtained value of  $n_2$ , the exhaust flow rate leaving the absorber,  $G_2$  can be determined by using the following equation.

$$G_2 = G_1 - n_1 + n_2$$

$$G_2 = 7.77 \frac{\text{mol}}{\text{s}} - 0.647 \frac{\text{mol}}{\text{s}} + 0.258 \frac{\text{mol}}{\text{s}}$$

$$G_2 = 7.38 \frac{\text{mol}}{\text{s}}$$

$$G_2 = 7.38 \frac{\text{mol}}{\text{s}} * 29 \frac{\text{g}}{\text{mol}}$$

$$G_2 = 770.82 \frac{\text{kg}}{\text{hr}}$$

Hence, the  $\text{CO}_2$  composition in the exhaust stream leaving the absorber,  $y_2$  can be determined by the following equation.

$$y_2 = \frac{n_2}{G_2}$$

$$y_2 = \frac{0.258 \frac{\text{mol}}{\text{s}}}{7.38 \frac{\text{mol}}{\text{s}}}$$

$$y_2 = 0.035 \frac{\text{mol}}{\text{mol}}$$



#### 4.2.1. Loading calculation and optimization

The exhaust gas parameters can be obtained from Table 3.1. For the operating point B50, the partial pressure of CO<sub>2</sub> of the exhaust stream entering and leaving the absorber can be calculated from total pressure and CO<sub>2</sub> composition using Dalton's law of partial pressure. For the exhaust stream entering the absorber,

$$P_{CO_2, 1g} = Py_1$$

$$P_{CO_2, 1g} = 1 \text{ bar} * 0.0833 \frac{\text{mol}}{\text{mol}}$$

$$P_{CO_2, 1g} = 0.0833 \text{ bar}$$

For the exhaust stream leaving the absorber, the partial pressure of CO<sub>2</sub> in the gas is given by –

$$P_{CO_2, 2g} = Py_2$$

$$P_{CO_2, 2g} = 1 \text{ bar} * 0.035 \frac{\text{mol}}{\text{mol}}$$

$$P_{CO_2, 2g} = 0.035 \text{ bar}$$

In the above calculations,  $P_{CO_2, 1}$  and  $P_{CO_2, 2}$  are the partial pressure of CO<sub>2</sub> in the gas. The difference between the partial pressure of CO<sub>2</sub> in gas and the equilibrium partial pressure of CO<sub>2</sub> in liquid represents the driving force for the mass transfer

of absorber. Assuming the driving force for mass transfer as a factor of 2, the partial pressure of CO<sub>2</sub> in the liquid leaving and entering the absorber can be obtained by the following equations.

$$P_{CO_2, 1l} = \frac{P_{CO_2, 1g}}{2} = 0.0416 \text{ bar}$$

$$P_{CO_2, 2l} = \frac{P_{CO_2, 2g}}{2} = 0.0175 \text{ bar}$$

Figure 4.5 shows the plot of partial pressure of CO<sub>2</sub> with respect to the CO<sub>2</sub> loading at 40°C as obtained from the Aspen results. The partial pressure of CO<sub>2</sub> obtained from the above equations can be compared to the plot to obtain the corresponding CO<sub>2</sub> loading in the solvent entering and leaving the absorber. From Figure 4.5, at  $P_{CO_2, 1L} = 0.0416$  bar, the corresponding CO<sub>2</sub> loading or rich loading is 0.44 mol CO<sub>2</sub>/mol K<sub>2</sub>CO<sub>3</sub> and at  $P_{CO_2, 2L} = 0.0175$  bar, the CO<sub>2</sub> loading or lean loading is 0.31 mol CO<sub>2</sub>/mol K<sub>2</sub>CO<sub>3</sub>.

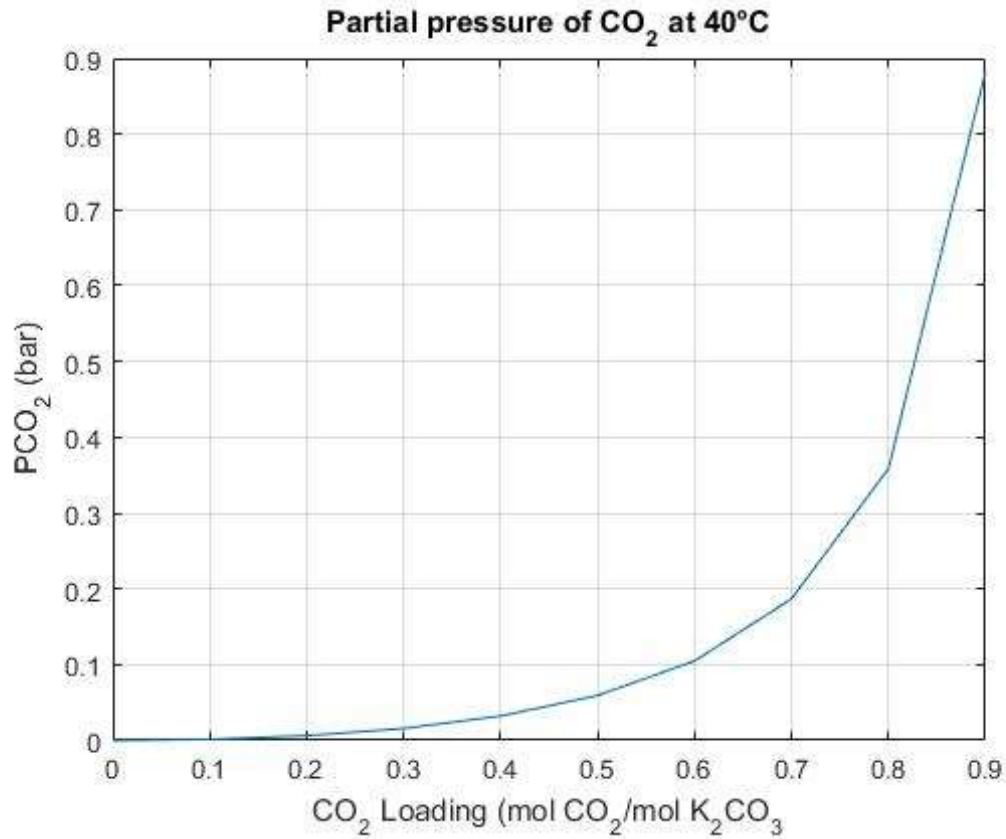


Figure 4.5. Partial pressure of CO<sub>2</sub> with respect to CO<sub>2</sub> loading at 40°C for a 40 wt.% K<sub>2</sub>CO<sub>3</sub> system solvent as obtained from Aspen results

#### 4.2.2. Calculation of solvent flow rate

Using equations 3.2 – 3.5, we can calculate the number of moles of K<sub>2</sub>CO<sub>3</sub>, CO<sub>2</sub> and H<sub>2</sub>O in the solvent stream entering the absorber.

$$n_{K_2CO_3} = \frac{40 \times 100gm}{138.205g/mol} = 28.94 \text{ mol}$$

$$n_{H_2O} = \frac{60 \times 100gm}{18.01g/mol} = 333.14 \text{ mol}$$

Moles of CO<sub>2</sub> in the absorber inlet stream,

$$n_{CO_2, 2} = 28.94 \text{ mol} * 0.31 = 8.97 \text{ mol}$$

Mole fraction of CO<sub>2</sub> in the solvent entering absorber,

$$x_{CO_2, 2} = \frac{8.97}{28.94 + 333.14 + 8.97} = 0.024 \frac{\text{mol}}{\text{mol}}$$

Moles of CO<sub>2</sub> in absorber outlet stream,

$$n_{CO_2, 1} = 28.94 \text{ mol} * 0.44 = 12.73 \text{ mol}$$

Mole fraction of CO<sub>2</sub> in the solvent leaving absorber,

$$x_{CO_2, 1} = \frac{12.73}{28.94 + 333.14 + 12.73} = 0.035 \frac{\text{mol}}{\text{mol}}$$

Hence, solvent flow rate entering absorber = L<sub>2</sub>

Mol flow rate of CO<sub>2</sub> entering absorber,

$$m_2 = L_2 * x_{CO_2, 2} = L_2 * 0.024 \frac{\text{mol}}{\text{mol}}$$

Mol flow rate of CO<sub>2</sub> leaving absorber,

$$m_1 = L_1 * x_{CO_2, 1} = L_1 * 0.035 \frac{\text{mol}}{\text{mol}}$$

Solvent flow rate leaving absorber,

$$L_1 = L_2 - m_2 + m_1$$

$$L_1 = L_2 - (L_2 * 0.024) + (L_1 * 0.035)$$

$$L_1 = L_2 * \frac{1 - 0.024}{1 - 0.035} = L_2 * 1.01$$

From absorber mass balance equation or equation 3.1,

$$L_1 * 0.035 \frac{mol}{mol} + 7.6 \frac{mol}{s} * 0.034 \frac{mol}{mol} = L_2 * 0.024 \frac{mol}{mol} + 8 \frac{mol}{s} * 0.0833 \frac{mol}{mol}$$

$$\begin{aligned} (L_2 * 1.011) * 0.035 \frac{mol}{mol} + 7.6 \frac{kg}{hr} * 0.034 \frac{mol}{mol} \\ = L_2 * 0.024 \frac{mol}{mol} + 8 \frac{mol}{s} * 0.0833 \frac{mol}{mol} \end{aligned}$$

$$L_2 = 3647.82 \frac{kg}{hr} = 1.12 \frac{kg}{s}$$

$$L_1 = 3720.68 \frac{kg}{hr} = 1.14 \frac{kg}{s}$$

$$\frac{L_1}{G_1} = 4.4 \text{ and } \frac{L_2}{G_2} = 4.6$$

Using the same procedure, the CO<sub>2</sub> lean and rich loadings as well as the liquid flow rates entering and leaving the absorber can be evaluated for all the SET points as shown in Table 4.1.

Table 4.1. CO<sub>2</sub> loadings and solvent flow rates entering and leaving the absorber  
for SET points A25-C100

| SET<br>Points | Lean Loading<br>(mol CO <sub>2</sub> /mol K <sub>2</sub> CO <sub>3</sub> ) | Rich Loading<br>(mol CO <sub>2</sub> /mol K <sub>2</sub> CO <sub>3</sub> ) | Liquid flow rate<br>entering<br>absorber, L <sub>2</sub><br>(kg/s) | Liquid flow<br>rate leaving<br>absorber, L <sub>1</sub><br>(kg/s) |
|---------------|--|--|--|---|
| A25           | 0.30   | 0.42   | 0.53   | 0.54  |
| A50           | 0.32   | 0.45   | 0.93   | 0.94  |
| A75           | 0.34   | 0.47   | 1.32   | 1.34  |
| A100          | 0.34   | 0.47   | 1.77   | 1.80  |
| B25           | 0.30   | 0.42   | 0.64   | 0.65  |
| B50           | 0.31   | 0.44   | 1.12   | 1.14  |
| B75           | 0.32   | 0.45   | 1.60   | 1.63  |
| B100          | 0.33   | 0.46   | 2.13   | 2.16  |
| C25           | 0.29   | 0.41   | 0.72   | 0.73  |
| C50           | 0.31   | 0.43   | 1.23   | 1.25  |

|      |      |      |      |      |
|------|------|------|------|------|
| C75  | 0.32 | 0.44 | 1.73 | 1.75 |
| C100 | 0.33 | 0.45 | 2.22 | 2.25 |

### 4.3. Calculation of regeneration energy

#### 4.3.1. Heat of Absorption calculation

The heat of absorption of 40 wt.% K<sub>2</sub>CO<sub>3</sub> can be estimated from Aspen Plus® for the given temperature and CO<sub>2</sub> loading. Figure 4.6 shows the heat of absorption of the solvent for a temperature range of 80 – 200°C.

The heat of absorption can also be calculated using Equations 3.17 – 3.18 as discussed in Section 3.2.2.4 with the input parameters of vapor pressure obtained from the flash calculation results.

$$Q_{desorption} = -m_{CO_2} \Delta H_{absorption}$$

$$T_{max} = 120^{\circ}C$$

$$P_{CO_2,lean}|_{T_{max}} = 19 \text{ kPa}$$

$$P_{CO_2,lean}|_{40^{\circ}C} = 1.6 \text{ kPa}$$

$$R = 8.314 * 10^{-3} \text{ kJ K}^{-1} \text{ mol}^{-1}$$

$$\Delta H_{absorption} = 31.6 \frac{\text{kJ}}{\text{mol CO}_2}$$

Mass flow rate of CO<sub>2</sub> in the absorber,

$$\dot{m}_{CO_2} = G_1 (y_1 - y_2)$$

$$\dot{m}_{CO_2} = 7.77 \frac{mol}{s} (0.0833 - 0.035) \frac{mol}{mol}$$

$$\dot{m}_{CO_2} = 0.37 \frac{mol}{s} = 0.011 \frac{kg}{s}$$

$$Q_{desorption} = 0.37 \frac{mol}{s} * 31.6 \frac{kJ}{mol CO_2} = 11.66 kW$$

#### 4.3.2. Sensible heat calculation

The specific heat of the solvent can be calculated from Aspen Plus® using a CPMX template in the NRTL method. At a rich CO<sub>2</sub> loading of 0.44 mol CO<sub>2</sub>/mol K<sub>2</sub>CO<sub>3</sub>, the specific heat of solvent at 110°C is calculated as –

$$C_{p_{solvent,R}} = 3.02 \frac{kJ}{kg K}$$

The sensible heat in the regenerator can be calculated using equation 3.20.

$$Q_{sensible} = \dot{m}_{solvent,R} C_{p_{solvent,R}} \Delta T$$

$$Q_{sensible} = 1.14 \frac{kg}{s} * 3.02 \frac{kJ}{kg K} * 10^\circ C$$

$$Q_{sensible} = 33.22 kW$$



#### 4.3.3. Calculation of heat of vaporization

From equation 3.21, we can calculate the heat of vaporization in the stripper. The partial pressure of CO<sub>2</sub> and H<sub>2</sub>O can be estimated from the plot shown in Figure 4.2 and Figure 4.3 respectively.

$$Q_{vaporization} = m_{CO_2} \frac{P_{H_2O} \Delta H_{vaporization, H_2O}}{P_{CO_2}}$$

$$Q_{vaporization} = 0.011 \frac{kg}{s} \frac{129 \text{ kPa} * 2257 \frac{kJ}{kg}}{19 \text{ kPa}}$$

$$Q_{vaporization} = 168.56 \text{ kW}$$

#### 4.3.4. Total Regeneration Energy

The total regeneration energy required in the stripper is given by –

$$Q_{reg} = Q_{desorption} + Q_{sensible} + Q_{vaporization}$$

$$Q_{reg} = 11.66 + 33.22 + 168.56 = 213.44 \text{ kW}$$

As shown in the above calculations, the regeneration energy required for the CO<sub>2</sub> desorption process in the stripper is 213.44 kW at B50 operating point. This energy is dominated by the heat of vaporization of water in the stripper, therefore performance could be substantially improved by using a solvent with a higher heat of absorption and operating the system at higher temperature (both of which increase the ratio of water to CO<sub>2</sub> in the stripper). Similarly, we can calculate

the total regeneration energy required in the stripper for all the SET points from the flow rates of solvent obtained from the absorber calculations and the VLE behavior of the system. Table 4.2 shows the total regeneration energy in the stripper along with the mass flow rate of CO<sub>2</sub> for the SET points A25-C100.

Table 4.2. Total regeneration energy required for SET points A25-C100

| SET Points | CO <sub>2</sub> (absorbed) Flow rate (kg/s) | Total Regeneration Energy (kW) |
|------------|---|--------------------------------|
| A25        | 0.005                                       | 98.41                          |
| A50        | 0.01  | 192.1                          |
| A75        | 0.014                                       | 270.25                         |
| A100       | 0.019                                       | 366.25                         |
| B25        | 0.006                                       | 118.21                         |
| B50        | 0.011                                       | 213.44                         |
| B75        | 0.016                                       | 312.34                         |
| B100       | 0.022                                       | 426.57                         |
| C25        | 0.007                                       | 137                            |
| C50        | 0.012                                       | 234.85                         |

|      |       |        |
|------|-------|--------|
| C75  | 0.017 | 332.51 |
| C100 | 0.023 | 445.6  |

#### **4.4. Results from GT-Suite® CO<sub>2</sub> Capture model**

The heat exchangers, coolers and the condenser are modelled individually in GT-Suite® and are simulated before integrating these individual models to the CO<sub>2</sub> capture system model. In all the components, the heat exchanger specifications are kept same as that of a core air-air CAC for a large truck, shown in Table 3.4.

##### **4.4.1. Results of Exhaust-absorbent heat exchanger**

As illustrated in Section 3.2.3.1, the input parameters for the exhaust absorbent heat exchanger can be found in Table 3.2 and 3.3. The rich CO<sub>2</sub> solvent flow rate as well as the solvent composition is calculated in Section 4.2.2. From the theoretical calculations of the mass balance equation, the rich CO<sub>2</sub> solvent flow rate is estimated to be 1.14 kg/s. The heat rate obtained for the exhaust-absorbent heat exchanger for B50 operating point are shown in Table 4.3.

Table 4.3. GT-Post® results of exhaust-absorbent heat exchanger

|                                   |      |
|-----------------------------------|------|
| Heat rejected by exhaust gas (kW) | 73.1 |
| Heat added to solvent (kW)        | 29.6 |

From Table 4.3, we see that at an outlet temperature of 40°C, 51.33 kW of heat is removed from the exhaust gas while 24.07 kW of heat is gained by the solvent at an outlet temperature of 120°C.

#### 4.4.2. Results of Cross exchanger

The input parameters of the cross-exchanger model are shown in Table 3.5 and Table 3.6. The cross-exchanger transfers heat between the rich CO<sub>2</sub> solvent coming from the absorber and the lean CO<sub>2</sub> solvent coming from the stripper. The solvent flow rates with rich and lean CO<sub>2</sub> along with solvent composition is calculated. From the theoretical calculations of the mass balance equation, the solvent flow rate with lean CO<sub>2</sub> is estimated to be 1.12 kg/s. The results for the cross-exchanger are shown in Table 4.4.

Table 4.4. GT-Post® results of cross-exchanger

|   |       |
|---|-------|
| Heat gained by solvent stream with rich<br>CO <sub>2</sub> loading (kW)   | 209.2 |
| Heat rejected by solvent stream with lean<br>CO <sub>2</sub> loading (kW) | 163.3 |

#### 4.4.3. Results of Trim cooler

Table 3.9 and 3.10 shows the input parameters of the trim cooler. The lean CO<sub>2</sub> solvent coming from the cross exchanger is cooled by water to maintain the desired temperature in the absorber. The lean CO<sub>2</sub> solvent flow rate and composition is calculated from absorber mass balance equation as shown in Section 4.2.2. The results for the trim cooler are shown in Table 4.5.

Table 4.5. GT-Post® results of trim cooler

|  |      |
|--|------|
| Heat rejected by lean CO <sub>2</sub> solvent (kW) | 31.2 |
| Heat gained by water stream (kW)                   | 19.6 |

#### 4.4.4. Results obtained from condenser

The input parameters for the condenser can be obtained from Table 3.11 and Table 3.12. The vapor stream from the stripper/ flash comprising of CO<sub>2</sub> and H<sub>2</sub>O is cooled by water at an initial temperature of 10°C. The water is drained, and the CO<sub>2</sub> is sent to the compressor. The CO<sub>2</sub> flow rate is calculated from the exhaust flow rate and CO<sub>2</sub> capture rate. The results obtained for the condenser with CO<sub>2</sub> stream is shown in Table 4.6.

Table 4.6. GT-Post® results of condenser with CO<sub>2</sub> stream

|  |      |
|--|------|
| Heat rejected by CO <sub>2</sub> stream (kW) | 1.02 |
| Heat gained by water stream (kW)             | 2.6  |

The steam duty in the condenser or amount of heat rejected due to vaporization of water is calculated using equation 3.29.

$$Q_{H_2O} = m_{H_2O} \Delta H_{\text{vaporization}, H_2O}$$

$$Q_{H_2O} = 0.068 \frac{kg}{s} * 2257 \frac{kJ}{kg K} = 153.5 kW$$

#### **4.4.5. Work done by the compressor**

The compressor work is calculated in GT-Suite® at a temperature of 120°C and an isentropic efficiency of 85% for a mid-speed, mid-load operating condition. To compress the CO<sub>2</sub> obtained from stripper to a desired pressure of 100 bar, the amount of work required is estimated as –

$$W_{compressor} = 19.5 \text{ kW}$$

#### **4.4.6. Energy Transfer across the system for SET points A25–C100.**

The individual model of the heat exchangers, cooler and the condenser are then integrated into the CO<sub>2</sub> capture system model. The design specifications as well as the inlet and outlet temperatures are specified in the system. The solvent flow rates for rich and lean loading and their compositions are obtained from Table 4.1. Using a case setup, the exhaust gas parameters are varied accordingly for different operating conditions, from low-load to full-load along with their respective solvent flow rates and compositions, to obtain the energy transfer across the system. The model is then simulated for all the cases. Tables 4.7 and 4.8 shows the heat rate generated across the system while Table 4.9 shows the compressor work for different operating conditions from SET A25 (low-load) to C100 (full load).

Table 4.7. Heat rate generated in the exhaust-absorbent heat exchanger and trim cooler for SET operating points from A25 – C100.

| SET data | Heat rejected by<br>exhaust stream<br>(kW) | Heat gained by<br>solvent stream<br>(kW) | Heat rejected by<br>trim cooler (kW) |
|----------|--|--|--------------------------------------|
| A25      | 36.3                                       | 16.3                                     | 11.7                                 |
| A50      | 65.7                                       | 28.4                                     | 20                                   |
| A75      | 97.5                                       | 40.3                                     | 29.2                                 |
| A100     | 134.1                                      | 57.2                                     | 39                                   |
| B25      | 45.6                                       | 19.6                                     | 17.5                                 |
| B50      | 78.7                                       | 37.8                                     | 24.7                                 |
| B75      | 113.7                                      | 49.1                                     | 36.1                                 |
| B100     | 158.5                                      | 65.1                                     | 45.7                                 |
| C25      | 52.1                                       | 22.2                                     | 15.9                                 |
| C50      | 84.8                                       | 37.8                                     | 27.6                                 |
| C75      | 122.2                                      | 52.9                                     | 38.1                                 |



|      |       |      |      |
|------|-------|------|------|
| C100 | 169.4 | 69.3 | 48.4 |
|------|-------|------|------|

Table 4.8. Heat rate generated in the cross exchanger and condenser for SET operating points from A25 – C100.

| SET data | Heat rejected by solvent with lean loading (kW) | Heat gained by solvent with rich loading (kW) | Work done in condenser (kW) |
|----------|---|---|-----------------------------|
| A25      | 81.6  | 113.5   | 0.3                         |
| A50      | 143.8   | 197.6   | 0.8                         |
| A75      | 206.1   | 272.2   | 1.3                         |
| A100     | 272.6   | 364.5   | 2.1                         |
| B25      | 98.6  | 138   | 0.4                         |
| B50      | 181.3   | 231.4   | 0.9                         |
| B75      | 246.4   | 331.1   | 1.6                         |
| B100     | 328   | 435.4   | 2.6                         |
| C25      | 111.9   | 154.7   | 0.5                         |

|      |       |       |     |
|------|-------|-------|-----|
| C50  | 194.3 | 255.7 | 1.0 |
| C75  | 267.6 | 354.3 | 1.7 |
| C100 | 342.8 | 452.8 | 2.8 |

Table 4.9. Work done by the compressor for SET operating points from A25 – C100.

| SET data | Work done by compressor (kW) |
|----------|------------------------------|
| A25      | 4.23                         |
| A50      | 15.78                        |
| A75      | 28.18                        |
| A100     | 46.36                        |
| B25      | 5.27                         |
| B50      | 19.5                         |
| B75      | 36.56                        |
| B100     | 64.87                        |

|      |       |
|------|-------|
| C25  | 7.65  |
| C50  | 21.3  |
| C75  | 41.45 |
| C100 | 69.81 |

The total amount of work in the system is obtained by deducting the compressor work from engine power output as the power required for compressor is provided by other form of exhaust energy or waste heat recovery system. The engine output is obtained from the engine SET data. Table 4.10 shows the comparative analysis of the amount of CO<sub>2</sub> in the tailpipe after passing through the CO<sub>2</sub> absorber with 60% capture rate, per kW-hr with respect to net work for SET points A25-C100.

Table 4.10. Amount of CO<sub>2</sub> in tailpipe after 60% CO<sub>2</sub> absorption per kW-hr from the CO<sub>2</sub> capture system with respect to net work for SET points A25-C100.

| SET Points | Tailpipe CO <sub>2</sub> Flow rate (kg/s) | Engine power output (kW) | Work done by compressor (kW) | Net work (kW) | Tailpipe CO <sub>2</sub> emissions (gCO <sub>2</sub> /kW-hr) |
|------------|---|--------------------------|------------------------------|---------------|--|
| A25        | 0.003                                     | 71.16                    | 4.23                         | 66.93         | 183.72   |
| A50        | 0.006                                     | 142.51                   | 15.78                        | 126.73        | 181.27   |
| A75        | 0.009                                     | 213.62                   | 28.18                        | 185.44        | 181.77   |
| A100       | 0.013                                     | 284.98                   | 46.36                        | 238.62        | 190.64   |
| B25        | 0.004                                     | 82.93                    | 5.27                         | 77.66         | 190.94   |
| B50        | 0.008                                     | 166.01                   | 19.5                         | 146.51        | 184.54   |
| B75        | 0.011                                     | 248.9                    | 36.56                        | 212.34        | 186.63   |
| B100       | 0.015                                     | 331.85                   | 64.87                        | 266.98        | 199.63   |
| C25        | 0.005                                     | 85.97                    | 7.65                         | 78.32         | 211.24   |
| C50        | 0.008                                     | 171.98                   | 21.3                         | 150.68        | 193.28   |

|      |       |        |       |        |        |
|------|-------|--------|-------|--------|--------|
| C75  | 0.012 | 258.84 | 41.45 | 217.39 | 193.97 |
| C100 | 0.015 | 341.76 | 69.81 | 271.95 | 203.47 |

According to EPA standards regulated under the GHG/CAFE vehicle regulations (2016), the CO<sub>2</sub> emissions standard for medium-duty engines are 772 g/kW-hr in 2017 and 731 g/kW-hr by 2021. For heavy-duty engines, the CO<sub>2</sub> emissions standard are 744 g/kW-hr in 2017 and 688 g/kW-hr by 2021.

## Chapter 5

### Conclusion and Recommendations

#### 5.1. Conclusion

A CO<sub>2</sub> capture system is developed for a heavy-duty engine application. The system follows a thermal swing absorption process for CO<sub>2</sub> absorption at low temperature and desorption at high temperature. A series of heat exchangers and coolers are used to maintain the temperature requirement of the system.

A 40 wt.% K<sub>2</sub>CO<sub>3</sub> solution is used as a solvent for the system due to its stability and non-volatile nature. The solvent regenerator is modelled using a flash drum in Aspen Plus which provides the CO<sub>2</sub> VLE data that helps determine the solvent flow rates, composition and other properties throughout the system by assuming a driving force for the mass transfer.

For a mid-speed, mid-load operating condition, the energy flow throughout the system involving heat rejected by exhaust gas, heat gained by the solvent stream and the regeneration energy produced due to CO<sub>2</sub> desorption is determined for a CO<sub>2</sub> absorption rate of 60% from the exhaust gas.

A model is developed in GT-Suite for the CO<sub>2</sub> capture system using HXMaster/Slave templates for heat exchangers and coolers and a 2D lookup table for the CO<sub>2</sub> stripper, with temperature and CO<sub>2</sub> loading as input and pressure as output. The heat exchangers, coolers and the condenser are modeled separately and sized for a mid-speed, mid-load operating condition and the solvent flow rates, water flow rates, outlet temperature and heat rate are determined. The outlet temperature and flow rate generated from results are set in the individual models before integrating it to the system model. The exhaust parameters such as temperature, pressure and composition are provided as input to the model for the mid-speed, mid-load operating condition. Assuming a 60% capture rate, the CO<sub>2</sub> flow rate is specified in the model. By keeping the design specifications, solvent flow rates and outlet temperature for the model constant, a case setup can be developed to calculate the heat transfer rate for the different SET operating conditions from idle to full load throughout the system.

## **5.2. Recommendations for future work**

Future work on the CO<sub>2</sub> capture system can involve integrating the system to a waste heat recovery arrangement to fulfill the energy demand of the CO<sub>2</sub> capture system to a certain extent. The compressor in the CO<sub>2</sub> capture system can be coupled to the expander of an Organic Rankine Cycle (ORC), to provide the maximum cycle power output with a suitable refrigerant.

Experimental analysis of a CO<sub>2</sub> absorber and stripper can be performed to explore the tradeoffs and benefits of various solvents relative to K<sub>2</sub>CO<sub>3</sub>. Challenges involved like sizing the system for a heavy-duty engine can also be addressed.

Validating the model with experimental data from heat exchangers, coolers and condenser should also be performed.



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## Appendix A

Table A.1. Total pressure from flash calculation in Aspen Plus as a function of Temperature and CO<sub>2</sub> loading

| Total Pressure (bar)  |       |       |       |       |       |       |       |       |       |       |       |       |       |  |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--|
| Temp(°C)  | 80    | 90    | 100   | 110   | 120   | 130   | 140   | 150   | 160   | 170   | 180   | 190   | 200   |  |
| Loading<br>(mol CO <sub>2</sub><br>/mol<br>(K <sub>2</sub> CO <sub>3</sub> )) |       |       |       |       |       |       |       |       |       |       |       |       |       |  |
| 0   | 0.33  | 0.47  | 0.68  | 0.95  | 1.30  | 1.74  | 2.31  | 3.01  | 3.87  | 4.91  | 6.16  | 7.64  | 9.39  |  |
| 0.1   | 0.33  | 0.48  | 0.69  | 0.96  | 1.31  | 1.76  | 2.33  | 3.04  | 3.90  | 4.95  | 6.20  | 7.69  | 9.44  |  |
| 0.2   | 0.35  | 0.51  | 0.72  | 1.00  | 1.37  | 1.83  | 2.41  | 3.14  | 4.02  | 5.09  | 6.37  | 7.88  | 9.67  |  |
| 0.3   | 0.39  | 0.56  | 0.79  | 1.09  | 1.48  | 1.97  | 2.58  | 3.34  | 4.27  | 5.38  | 6.71  | 8.28  | 10.13 |  |
| 0.4   | 0.46  | 0.65  | 0.91  | 1.24  | 1.67  | 2.21  | 2.88  | 3.70  | 4.70  | 5.89  | 7.30  | 8.96  | 10.88 |  |
| 0.5   | 0.57  | 0.80  | 1.11  | 1.50  | 1.99  | 2.61  | 3.37  | 4.29  | 5.39  | 6.69  | 8.22  | 9.98  | 12.00 |  |
| 0.6   | 0.76  | 1.05  | 1.43  | 1.92  | 2.52  | 3.26  | 4.16  | 5.22  | 6.48  | 7.92  | 9.58  | 11.45 | 13.55 |  |
| 0.7   | 1.09  | 1.50  | 2.01  | 2.65  | 3.43  | 4.37  | 5.47  | 6.74  | 8.18  | 9.78  | 11.54 | 13.47 | 15.58 |  |
| 0.8   | 1.78  | 2.40  | 3.17  | 4.10  | 5.18  | 6.41  | 7.77  | 9.26  | 10.84 | 12.52 | 14.28 | 16.14 | 18.12 |  |
| 0.9   | 3.71  | 4.84  | 6.11  | 7.51  | 8.97  | 10.48 | 11.98 | 13.47 | 14.95 | 16.43 | 17.94 | 19.50 | 21.18 |  |
| 1   | 14.00 | 15.10 | 16.12 | 17.05 | 17.91 | 18.71 | 19.45 | 20.18 | 20.92 | 21.70 | 22.56 | 23.54 | 24.70 |  |

Table A.2. Partial Pressure of CO<sub>2</sub> from flash calculation in Aspen Plus as a function of Temperature and CO<sub>2</sub> loading

| Partial Pressure of CO <sub>2</sub> (bar)                                     |       |       |       |       |       |       |       |       |       |       |       |       |       |  |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--|
| Temp(°C)  | 80    | 90    | 100   | 110   | 120   | 130   | 140   | 150   | 160   | 170   | 180   | 190   | 200   |  |
| Loading<br>(mol CO <sub>2</sub><br>/mol<br>(K <sub>2</sub> CO <sub>3</sub> )) |       |       |       |       |       |       |       |       |       |       |       |       |       |  |
| 0   | 0.00  | 0.00  | 0.00  | 0.00  | 0.00  | 0.00  | 0.00  | 0.00  | 0.00  | 0.01  | 0.01  | 0.02  | 0.03  |  |
| 0.1   | 0.01  | 0.01  | 0.01  | 0.01  | 0.02  | 0.02  | 0.03  | 0.04  | 0.05  | 0.06  | 0.08  | 0.11  | 0.14  |  |
| 0.2   | 0.03  | 0.03  | 0.05  | 0.06  | 0.08  | 0.10  | 0.12  | 0.15  | 0.19  | 0.23  | 0.28  | 0.34  | 0.42  |  |
| 0.3   | 0.07  | 0.09  | 0.12  | 0.15  | 0.19  | 0.24  | 0.30  | 0.37  | 0.45  | 0.55  | 0.66  | 0.78  | 0.93  |  |
| 0.4   | 0.13  | 0.18  | 0.23  | 0.30  | 0.39  | 0.49  | 0.60  | 0.74  | 0.89  | 1.07  | 1.27  | 1.49  | 1.72  |  |
| 0.5   | 0.24  | 0.33  | 0.43  | 0.56  | 0.71  | 0.89  | 1.09  | 1.33  | 1.59  | 1.88  | 2.20  | 2.52  | 2.86  |  |
| 0.6   | 0.43  | 0.58  | 0.76  | 0.98  | 1.24  | 1.54  | 1.88  | 2.26  | 2.68  | 3.11  | 3.56  | 3.99  | 4.40  |  |
| 0.7   | 0.77  | 1.02  | 1.34  | 1.71  | 2.15  | 2.64  | 3.19  | 3.77  | 4.36  | 4.95  | 5.50  | 5.99  | 6.40  |  |
| 0.8   | 1.45  | 1.93  | 2.49  | 3.15  | 3.88  | 4.66  | 5.47  | 6.26  | 7.00  | 7.65  | 8.19  | 8.60  | 8.88  |  |
| 0.9   | 3.38  | 4.35  | 5.42  | 6.54  | 7.65  | 8.70  | 9.63  | 10.42 | 11.05 | 11.49 | 11.77 | 11.88 | 11.85 |  |
| 1   | 13.64 | 14.58 | 15.38 | 16.03 | 16.52 | 16.85 | 17.02 | 17.03 | 16.90 | 16.65 | 16.28 | 15.81 | 15.26 |  |

Table A.3. Partial Pressure of H<sub>2</sub>O from flash calculation in Aspen Plus as a function of Temperature and CO<sub>2</sub> loading

| Partial Pressure of H <sub>2</sub> O (bar)                                    |      |      |      |      |      |      |      |      |      |      |      |      |      |  |
|---|------|------|------|------|------|------|------|------|------|------|------|------|------|--|
| Temp(°C)  | 80   | 90   | 100  | 110  | 120  | 130  | 140  | 150  | 160  | 170  | 180  | 190  | 200  |  |
| Loading<br>(mol CO <sub>2</sub><br>/mol<br>(K <sub>2</sub> CO <sub>3</sub> )) |      |      |      |      |      |      |      |      |      |      |      |      |      |  |
| 0   | 0.33 | 0.47 | 0.68 | 0.95 | 1.30 | 1.74 | 2.31 | 3.01 | 3.86 | 4.90 | 6.15 | 7.63 | 9.36 |  |
| 0.1   | 0.33 | 0.47 | 0.68 | 0.95 | 1.29 | 1.74 | 2.30 | 3.00 | 3.85 | 4.89 | 6.12 | 7.58 | 9.30 |  |
| 0.2   | 0.33 | 0.47 | 0.68 | 0.94 | 1.29 | 1.73 | 2.29 | 2.99 | 3.83 | 4.86 | 6.09 | 7.54 | 9.24 |  |
| 0.3   | 0.33 | 0.47 | 0.68 | 0.94 | 1.29 | 1.73 | 2.29 | 2.97 | 3.82 | 4.84 | 6.06 | 7.50 | 9.19 |  |
| 0.4   | 0.33 | 0.47 | 0.67 | 0.94 | 1.28 | 1.73 | 2.28 | 2.97 | 3.80 | 4.82 | 6.03 | 7.47 | 9.16 |  |
| 0.5   | 0.33 | 0.47 | 0.67 | 0.94 | 1.28 | 1.72 | 2.27 | 2.96 | 3.80 | 4.81 | 6.02 | 7.46 | 9.14 |  |
| 0.6   | 0.33 | 0.47 | 0.67 | 0.94 | 1.28 | 1.72 | 2.27 | 2.96 | 3.80 | 4.81 | 6.02 | 7.46 | 9.15 |  |
| 0.7   | 0.33 | 0.48 | 0.68 | 0.94 | 1.29 | 1.73 | 2.28 | 2.97 | 3.81 | 4.83 | 6.05 | 7.49 | 9.18 |  |
| 0.8   | 0.33 | 0.48 | 0.68 | 0.95 | 1.30 | 1.74 | 2.30 | 3.00 | 3.84 | 4.87 | 6.09 | 7.54 | 9.24 |  |
| 0.9   | 0.33 | 0.49 | 0.69 | 0.97 | 1.32 | 1.78 | 2.35 | 3.05 | 3.91 | 4.94 | 6.17 | 7.62 | 9.32 |  |
| 1   | 0.36 | 0.52 | 0.74 | 1.03 | 1.39 | 1.86 | 2.44 | 3.15 | 4.01 | 5.05 | 6.28 | 7.73 | 9.44 |  |