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# BEAUTIFUL FORMS AND COMPOSITIONS ARE NOT MADE BY CHANCE: EXPLORING THE EFFICACY OF PORTABLE X-RAY FLUORESCENCE TO SORT AND SOURCE ENGLISH LEAD GLAZED CERAMICS

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#### BEAUTIFUL FORMS AND COMPOSITIONS ARE NOT MADE BY CHANCE: EXPLORING THE EFFICACY OF PORTABLE X-RAY FLUORESCENCE TO SORT AND SOURCE ENGLISH LEAD GLAZED CERAMICS

By

Steven J. Sarich

#### A THESIS

Submitted in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE

In Industrial Archaeology

#### MICHIGAN TECHNOLOGICAL UNIVERSITY

2015

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This thesis has been approved in partial fulfillment of the requirements for the Degree of MASTER OF SCIENCE in Industrial Archaeology

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#### Abstract

Advances in portable X-ray fluorescence (pXRF) technology have made it a viable option for the non-destructive exploration of the underlying chemical composition of ceramic artifacts for the purposes of classification. However, because the literature regarding the use of this instrument on historic artifacts is limited, it is necessary to begin with a broad scale exploratory assessment that might act as a jumping off point for future studies on this topic. Toward that end, this research uses a collection of British and Continental European ceramics ranging from 1650-1920, owned and curated by the Chipstone Foundation in Fox Point, WI, to explore the efficacy of using pXRF to sort and source those materials. The chemical patterns in the data are tested against the known provenance of these artifacts which has been pre-determined by ceramic experts and material culture analysts.

Of the 102 samples that have been tested, primary focus is given to items crafted in London and Staffordshire which account for the largest portion of artifacts in the dataset. Principle component analysis is used to better understand the underlying structure of the entire dataset to ultimately reduce the number of chemical variables to those that best distinguish each group. Using those particular chemical variables, a separate dataset of London and Staffordshire mean intensity readings is subjected to factor analysis which resulted in two components being identified. The calculated factor scores are incorporated into a binary logistic regression model to determine if the samples can be correctly sorted into their pre-established provenance categories. A second model that incorporates the year of production is also presented which shows an improved ability to classify those samples. These results are ultimately situated within the historic context of the pottery making industry in England which was highly influenced by the Industrial Revolution and developments in ceramic technology.

## Chapter 1: Introduction to Archaeological Classification and Portable X-Ray Fluorescence

The characterization and classification of artifacts is a cornerstone of archaeological analysis that entails the detailed examination and description of an object or assemblage. Classification draws on an array of external and internal details of the artifacts. The confluence of that information leads the researcher to conclusions regarding the archaeological record and the groups of people that took part in its creation (Prown 1982). That ancillary or external information is often lacking for historical artifacts, however, or non-existent in prehistoric contexts. Throughout the history of the discipline, this has lead archaeologists to develop means of extracting relevant and valuable information purely from the artifacts themselves. Scholars developed typologies and classification schemes as systems of thought. In other words, these systems became tools for formulating questions by comparing and contrasting the characteristics of artifacts. Subsequent research then answers those questions.

Culture historians, in the early years of archaeology, developed pragmatic and regional systems for making artifact comparisons. Chronologies of cultural and technological developments and diffusion developed as a result. Early examples include Gladwin and Gladwin's (1930) regional chronological classification of southwestern pottery or the Midwestern Taxonomic System used to find confluences of traits that characterized the past cultures in North America (McKern 1939). Later, processual archaeologists endeavored to discover the exact role of artifacts in cultural systems and in the surrounding environment. Archaeologists began to favor models of cross-cultural human behavior based on the archaeological and ethnoarchaeological record over the recreation of "unique events in all their idiosyncratic detail" (Trigger 2006, 401).

An interest in human agency in the conceptualization and production of things, however, led archaeologists to a post-processual school of thought. An artifact in an historic or prehistoric context was seen as "an active element" within the society where it was produced (Trigger 2006, 453). Post-processual archaeologists emphasize artifacts as symbols and identify traits reflective of an individual's role in society. The classification of artifacts therefore became a tool to gain insight into race, class, and gender in a given society or to reveal the minds of the makers. The artifacts themselves are not of central importance necessarily, but rather the primary focus is on the individual who is crafting them.

These elements, along with particular tenets of preceding paradigms, are being incorporated into the contemporary archaeological toolkit. The classification of artifacts in modern archaeology has taken on a more pragmatically minded processual-plus flavor. This approach views material culture from multiple theoretical perspectives to achieve a holistic understanding of past cultures and human behavior. This framework also incorporates a multitude of methods that are most productive for answering a given research question.

Any artifact research, no matter the theoretical framework for classifying artifacts, must ultimately confront the practical realities of archaeology. Archaeologists draw their conclusions from things. This necessitates developing tools for examining and organizing those material remains. For much of the history of the discipline there has been a reliance

on diagnostic characteristics of artifacts that can be seen with the naked eye or through an optical microscope. Material science techniques in archaeology have gained a great deal of traction over the last few decades and are useful lines of research. Systems of classification based on the chemical fingerprint of artifacts can serve to reinforce existing systems or uncover variation that would otherwise go unnoticed.

#### The Benefits of Material Science and Portable X-Ray Fluorescence

Techniques in material science allow archaeologists and material culture analysts to understand artifacts at a mineralogical and elemental level. This is most useful in the absence of macroscopic diagnostic features which would typically be used for identifying and classifying artifacts. Several of these techniques, including pXRF, involve concentrating x-rays into a fine beam which interacts with the material under analysis. Given enough energy, an electron is dislodged from an M, L, or K electron orbital. To maintain neutrality, a higher shell electron drops into the gap. The binding energy of electrons increases the further they are from the nucleus. The difference in energy as a higher shell electron drops into a lower shell, determined by the distances between the M, L, and K shells, leads to the emission of radiation in the form of photons which are detected by the instrument (Figure 1.1) (Piorek 1997; Rice 1987). As the atomic structure of each element is different, the energy emitted will be characteristic of that element and result in M, L, and K spectral peaks. The instrument and software also calculates counts, or net intensities of an elemental which act as a measure of the amount of that element in the artifact. This information factors into a patterned "fingerprint" that can be linked with artifacts or raw material of similar composition.



Figure 1.1 Basic diagram of X-ray fluorescence. A) Emitted X-rays eject an inner shell electron. B) A higher shell electron fills the gap to maintain electrical neutrality which causes the emission of characteristic radiation.

This approach to artifact analysis operates under the assumption that objects or groups of objects made by people can be distinguished based on their elemental fingerprint. This distinction is based on alternative approaches to the production of items even though the same basic end may be achieved. In other words, one potter may produce a similarly shaped vessel or another, however each may be utilizing different raw materials for both fabric and glaze as well as using varying amounts of those raw materials in their recipes. This divergence in approaches to production is shown to manifest itself in differing chemical signatures allowing archaeologists to sort and "source" objects to particular individuals, pottery shops, or ceramic producing regions (Forster and Grave 2013; Hou et al. 2004). The development of these types of technologies for analyzing materials marks a sizeable expansion of the archaeologist's toolkit for understanding the archaeological record.

An array of features characterize field portable X-ray fluorescence (pXRF), shown in Figure 1.2, that are highly attractive to material culture analysts and archaeologists. As the name suggests, the device can be transported to a location such as



Figure 1.2 Basic instrument setup with complete software package, vacuum pump, and instrument stand.

a museum or into the field to perform *in situ*, non-destructive artifact characterization. In cases of delicate, highly valuable, or non-transportable items this is of great benefit as they do not have to be handled or moved apart from positioning the object for analysis or transitioning from one reading location to another. The pXRF instrument is also capable of performing an analysis non-destructively by reading the surface characteristics of objects, however, homogenized or powdered samples can be used as well to randomize the distribution of constituents. Furthermore, this technology has evolved in recent years to achieve greater accuracy and detect a wider array of constituent elements relative to its earlier incarnations while still maintaining its portability (Potts 2008). Given these features coupled with its lower operating costs and short reading times relative to most bench instruments it is worthwhile to assess its ability to chemically classify artifacts. Through the use of a curated collection of intact British and Continental European ceramics, attributed to manufacture dates from approximately 1650 to 1915, this study tests the efficacy of the pXRF instrument for archaeological analysis. This is meant to be a proof-of-concept study that will demonstrate the use of pXRF and factor analysis to sort ceramic artifacts by provenance using the chemical signature of the surrounding tinopacified lead-oxide glaze of each artifact.

#### **A Brief Overview of Glaze Constituents**

Many British ceramics from the seventeenth to the nineteenth century feature earthenware fabrics fired at a lower temperature with a relatively high degree of porosity. The permeable fabric necessitates the application of a non-permeable glaze in order to hold liquid and for aesthetic effect. There are several types of ceramic glazes, but the artifacts at the heart of this study were coated with a lead based tin-opacified glaze. Lead oxide acts as a flux to lower the melting point of the clay to encourage the formation of a smooth glassy surface. Aluminum and silicon are also fundamental constituents which help to stabilize the surface. That is to say keep the glassy surface from running or cracking and help the glaze adhere to the fabric surface (Rice 1987).

Potters from the Netherlands introduced tin-glazing to England in the middle of the sixteenth century (Black 2001). It is a variation on the primarily lead based glazes which have a long history in pottery production. This became a popular glazing strategy as the tin, when fired, interacts with the other glaze constituents to form tiny air bubbles in the glaze which scatter light and thus create a glossy, white surface that imitated fine imported porcelain finishes. The basic combination of lead, aluminum, and silicon along with tin was applied to the vessels and fired in a glost kiln. Colorants would subsequently be dusted or painted depending on the desired outcome. Common colorants include cobalt, iron, copper, nickel, or manganese. Table 1.1 lists common stabilizers, fluxes, opacifiers, and colorants. The use of colorants as well as the underlying, fundamental lead or tin-glazed coating was subject to experimentation over the years in Britain and Continental Europe to achieve an aesthetically pleasing and white product. An extensive number of these artifacts can be found among the collections at the Chipstone Foundation.

Stabilizers	Fluxes	Opacifiers	Colorants
Silicon	Lead	Tin	Copper
Aluminium	Calcium	Titanium	Cobalt
	Potassium		Manganese
	Sodium		Iron
	Magnesium		Nickel
	Zinc		

Table <u>1.1 List of common stabilizers</u>, fluxes, opacifiers, and colorants.

#### The Benefits and Limitations of the Chipstone Ceramic Collection

In the middle of the twentieth century, Stanley and Polly Stone started collecting seventeenth and eighteenth century British and European ceramics. In the 1980s the Chipstone Foundation was formed to manage this collection and educate people about the importance of these items. Approximately 505 ceramic objects are curated by the Chipstone Foundation. The artifacts chosen for this analysis have known provenance information assessed by experts in the field of historic British and Continental European ceramics (Hume 2001, Martin 1999). This information is catalogued in an online database managed by the University of Wisconsin-Madison, a permanent record of which resides at the Chipstone headquarters. The valuable nature of artifacts held in this collection make pXRF ideal for extracting elemental data without damaging any of the items. The volume of objects curated by the foundation allows for the examination of a substantial number of samples in a single location without significantly disturbing artifacts or transporting them great distances. The Archaeological Research Laboratory at the University of Wisconsin-Milwaukee very kindly agreed to lend the instrument for the purposes of carrying out this study.

This study is meant to demonstrate the viability of using the pXRF instrument, i.e. act as a proof-of-concept study, to sort ceramic artifacts based on their respective chemical signatures. This study comes with certain limitations however. Because the initial collector, Stanley Stone, was interested in a certain subset of ceramic artifacts, it is open to question whether they are truly representative of the population of tin-opacified and lead glazed wares made in these ceramic producing regions. Additional concerns include differential preservation of ceramic vessel types. Furthermore, this study itself focused on a particular subset of the collection. Nevertheless, the research strategy employed here was deemed acceptable as a useful starting point to gain some insight into the effectiveness of the instrument to characterize these artifacts.

#### **Document Structure**

The five subsequent chapters of this thesis build on one another and culminate in a synthesized assessment that situates this work among the archaeological systematics and ceramic classification literature. Chapter 2 entails a retrospective review of systematics and classification over the course of the archaeological discipline. This is meant to provide some context on those topics as well as emphasize the absolute importance of artifact, and more specifically, ceramic classification in the archaeological realm. This is also meant to highlight the need for a constant re-examination of the toolkit available to the archaeological researcher for organizing and describing material culture as it is the foundation for all subsequent research into the archaeological record. This chapter will also feature a discussion of the use of material science techniques, with a

focus on portable X-ray fluorescence, in contemporary archaeology. However, theoretical concepts regarding pragmatism in classification and having an understanding of the mind of the maker are essential in sorting artifacts effectively regardless of the technique for so doing.

Having established the usefulness of pXRF for material culture analysis, Chapter 3 introduces the methodological elements of the study of the Chipstone collection. This includes a review of the instrument specifications, the samples and the sample size, the process of data collection, and the data analysis procedure and protocols set down by the University of Wisconsin-Milwaukee Archaeological Research Lab. Chapter 4 will detail the results of that data analysis including the trends shown in the principle component analysis, the subsequent ANOVA and post-hoc tests linking the clusters of data to their provenance designations., and the focused factor analysis and regression models for the Staffordshire and London artifacts. With these results in hand, Chapter 5 explores the implications of the findings and situates them within the literature on glaze raw materials and chemical analysis. Finally in Chapter 6, a reflexive examination of the gleaned results leads to new questions manifested as a results of the experiments and features closing remarks on the benefits of arcaeometric analysis.

#### **Chapter 2: The Disciplinary Evolution of Systematics and Classification**

Approaches to artifact classification have taken on many iterations over the years as new paradigms and frameworks are introduced into the archaeological discipline. In all these instances the classification of artifacts was meant to better understand the movements, behaviors, and habits of people and the changing nature of the culture or cultures engaged in the production of particular items by viewing the often subtle variations in form or decoration of artifacts. Classification helps to make sense out of the vast amounts of materials in the world. Once sorted, archaeologists can start to ask questions about the past. Despite this common goal, the means by which these phenomena are understood has been open to much debate, largely between processually minded archaeologists with defined types which become the primary units of analysis (Dunnell 1971; 1986), cognitive scholars who see the mind of the maker among variations in artifacts (Renfrew 2005) and post-processual thinkers who view the changing meanings of artifacts over time and utilize more relativistic vernacular labels or folk taxonomic systems to better understand the emic values imbued in objects (Shanks 1998).

In recent years, these debates have subsided to a certain extent, having been reconciled in the minds of many scholars who see value in pragmatically driven research designs to classify and interpret artifacts in the archaeological record (Read 2009). Not only are interpretive frameworks being developed to unpack the meanings surrounding particular formal or stylistic choices, but there appears be a resurgence in the application

of natural science techniques to the study of artifacts influenced in large part by advancements in technology. Material science and archaeometric techniques have been introduced into the realm of systematics and artifact classification that bring into the fold an alternate means of differentiating cultural items through the use of chemical data (Kingery 1996; Orton and Hughes 2013). This does not eliminate the need for macroscopic diagnostic information of, in the case of the research presented here, whole or partial ceramic artifacts. The chemical classifications are meant to supplement those other systems or provide contrast to them.

Archaeologists organize artifacts in an iterative process. New technology or alternate thinking forces necessary reconceptualization of relationships among objects. New groupings of objects, or awareness of new traits, alters archaeologist's understanding of the people that made or used them. It is worthwhile to chart the trajectory of intellectual thought related to this topic to assess the established toolkit available to the contemporary archaeologist. This continual reconceptualization of artifact classification gave rise to this pragmatic paradigm that utilizes macroscopic as well as elemental information. It is useful to keep this context in mind when determining where the research presented here might fit within the larger realm of systematics and classification.

This discussion is organized by paradigmatic shifts in the archaeological discipline which influenced not only the organization of objects, but also the types of questions archaeologist's asked of the archaeological record. This discussion necessarily begins within the realm of culture-historical archaeology, a period which laid the foundation for typological debates subsequently brought about by the processual and

post-processual turn in archaeology. The many complexities archaeologist's uncovered as a result of those debates went a long way toward influencing the current state of archaeology. In a sense, the discipline has returned to the central tenet of the anthropological field as a holistic pursuit which brings to bear systematic, interpretive, and material science approaches to the study of past human behavior.

#### Culture-Historical Archaeology and the Development of Classificatory Systems

The central goal of the culture-historical paradigm has been to "trace historical relations through time and space. Such historical findings are the necessary prerequisites for evolutionary generalizations about the process of change" (Trigger 2006, 313). Concepts like acculturation, assimilation based on the degree of contact, and the organization of cultures across space and over time were developed based on the similarities and differences of styles and forms. However, the application of these ideas was largely focused on prehistoric and contact period contexts with less regard for historic sites. For example, Quimby and Spoehr (1951) looked at the regular changes in form of native-made objects over time among museum collections during the contact period in North America to see the steady assimilation of Western ideas into the material culture of Native groups. The tenets of culture-historical archaeology are reflected also in Culture and Acculturation of the Delware Indians by William Newcomb (1956) which narrowed the scope to changes among a particular group of Native Americans. These authors traced steady cultural changes based on the materials being produced. In other words, it was thought that one culture would transition into another form based on the degree of contact, though with a certain disregard for the complexities of these changes. For example, an article by Jörgen Meldgaard (1960) featured a straightforward and

simple model that showed a temporally broad and steady progression, based on tool materials and house forms, from Late Archaic groups in the Eastern Arctic to Early Woodland who then became the Dorset people. Over time, however, scholars began to recognize the complexities inherent in the archaeological record and this led to both cladistic and reticulation models to trace evolving artifact features and therefore demonstrate cultural transitions over time (O'Brien et al. 2012; Tëmkin and Eldredge 2007). At its core, the cladistic model argues that a single population over time begins to branch out to produce multiple new populations, languages, cultural values, etc. This allows archaeologists to trace representative artifacts in the archaeological record back to a common ancestral culture (Tehrani and Collard 2002). On the other hand the reticulation model puts forth the idea that multiple groups or populations are responsible for the rise of multiple modern populations, languages and cultural values and can be seen as a more convoluted "braided stream" (Moore 1994; O'Brien et al. 2002). These later years of culture-historical archaeology set the stage for a more systematic approach to the study of artifacts; one that would more accurately depict the observed changes in the archaeological record taking place over time.

As a result of these disciplinary developments, archaeologists created classification systems for an array of artifact classes including ceramics. One early example is Gladwin and Gladwin's (1930; 1931; 1933) classificatory system of pottery of the southwest that was "based on relative degrees of trait similarities, its dendritic pattern involved geographical considerations and it was implicitly chronological; roots formed before stems and stems before branches" (Trigger 2006, 284). Will C. McKern (1939) created an alternate system called the Midwestern Taxonomic Method. This system

divided units of occupation into components then foci which, in turn, were further subdivided. At the time of their inception, these systems separated cultures into a rough chronological framework or situated them in approximate geographic space. Ford's (1962) seriation method required careful observations of stratigraphy and detailed artifact descriptions, and this led scholars to a continual re-examination of classification systems.

Issues surrounding classification erupted with the Ford-Spaulding debate. Albert Spaulding (1953) argued that types were discovered and thus real to makers. Classification should, therefore, fit the cultural context. James Ford (1954), on the other hand, saw types as being constructed by the archaeologist as a practical solution to the sometimes chaotic nature of culture change. Charles Ewen (2003, 70) noted that Ford and Spaulding's approaches "were designed to answer different questions…One could argue that Ford was promoting paleoethnology…while Spaulding championed paleoethnography." Because of these discussions culture-historical archaeologists were able to give a firm description and history to particular groups or past cultures.

A number of classificatory systems in historical archaeology were also devised, applied, and refined. These include the type-variety system (Dunnell 1971; Gifford 1960; Sabloff and Smith 1969), the SHA typological systems that establish date of manufacture based on technology history (Lindsey 2015), and more focused systems addressing a particular region such as the Potomac Typological System (Beaudry et al. 1983). Furthermore, industrial archaeology still maintains a firm foothold in the regional nutsand-bolts approach to classification. Becher and Becher (2004) developed a typology of industrial structures based on formal changes over time. Bayley and Rehren (2007) offer a classification of crucibles based largely on differences in function.

In the realm of ceramics, the type-variety system was developed and is a popular way of describing an assemblage of pottery. It is designed to deconstruct ceramic artifacts into ware, type, variety, and group and analyze the interrelationship between these variables to establish ceramic complexes and chronologies (Sabloff and Smith 1969). The type-variety system has been criticized for being too rigid in its definition of types which often times have a great deal of overlap. Hammond (1972, 452) noted that,

This loss of effectiveness may perhaps be partly resolved by treating the Ceramic Group as a polythetic set of attributes...within which the possession of any one attribute is neither sufficient nor necessary for membership. Thus neither a common vessel form, nor the color, nor even the presence of slip, nor the absence, presence, or variety of ornament matter provided that the specimen possesses a certain number of the defined attributes which encapsulate the group.

This debate speaks to the core concern of archaeologists at this time which centered on making sense of the material world. Classification in the culture-historical realm is focused largely on description and identifying certain patterns. New intellectual developments in anthropology and archaeology would challenge the straightforward narratives presented by the culture-historian, approaches that acknowledged a number of other cultural and ecological factors that influenced the nature of the archaeological record as well as the form and function of artifacts.

#### A Systematic Approach to Artifact Classification

Moving forward to the middle decades of the 20<sup>th</sup> century, culture-historical archaeology dominated the study of material culture and the archaeological record. However an alternate approach was taking shape in the form of the processualist paradigm (Binford 1989). Scientific practice was incorporated into archaeological research and patterns in the archaeological record were being studied using computers and multivariate statistics. This technological and methodological change mirrors the current evolution in contemporary archaeological practice influenced by material science studies.

This paradigm is discussed in several articles by Binford (see Binford 1983; Binford and Quincy 1972), but his 1962 article "Archaeology as Anthropology" is notable for a number of reasons, one of which is his deconstruction of material culture into the technomic, socio-technic, and ideotechnic. According to Binford (1962, 217) "change in the total cultural system must be viewed in an adaptive context both social and environmental, not whimsically viewed as the result of 'influences,' 'stimuli,' or even 'migrations' between and among geographically defined units." The cultural system is revealed through the study of the three classes of material culture stated above. This new framework resulted in a more systematic and process oriented approach to culture change and the study of the archaeological record. This developing framework was explored, again, by Binford (1965) who advocated for the use of particular artifacts, ceramics among them, to reveal the workings of given subsystems of a culture and basing classification on formal, decorative and primary and secondary functional elements.

Robert Dunnell's (1971; 1986) work exemplified these intellectual trends and outlined a strategy for utilizing artifact types as the basic unit of analysis. This approach also used etic classifications that would be universal to the assemblage of items made by individuals in a given culture. In the words of Dunnell (1971):

If several objects hold features in common, and those features are of human origin, there is but a single plausible account. Intentionally or unintentionally, consciously or unconsciously, the objects were made to look alike by people who can be treated as possessing similar ideas about them and who have the same categories of features and ways of articulating the features into whole artifacts. In short, the objects can be treated as expressions of the same mental template (132).

In this sense, the individual is exchanged for culturally guided groups and focus is placed on common classes of traits rather than particular details of a given artifact (Read 2009). The concept of commonalities between material objects is central to the approach of this research. The sorting of artifacts chemically operates under the assumption that particular groups of potters utilized like glaze recipes that are independent of those developed in another pottery producing region. However, questions regarding the exact nature and cause of those shared features are addressed in greater detail by cognitive and postprocessual scholars who seek to understand the mind of the maker and the evolution of the sequence of operations to achieve a desired outcome in the creation of objects.

#### **Cognitive and Post-Processual Approaches to Artifact Types**

Cognitive approaches to the archaeological record were influenced by developments in the broader discipline of cognitive anthropology and related fields. The paradigm endeavored to utilize material culture to better understand the mental processes at work as people crafted objects which would subsequently make their way into the archaeological record (Abramiuk 2012; Renfrew 1993, 1998). Cognitive archaeology borrows many of the theoretical underpinnings of cognitive anthropology and psychology. A goal of cognitive archaeology is to craft networks of typologies often based on the vernacular terminology of makers and craftspeople to see how ideas regarding the production of objects might develop and be transferred. In other words, the idea is to "develop a secure methodology by which we [cognitive archaeologists] can hope to learn how the minds of the ancient communities in question worked and the manner in which that working shaped their actions" (Renfrew 2005,41).

Often cognitive interpretations take on a dialectical flavor with back and forth interaction between the mental conceptualization of the maker and real world practice. The strengths and limitations of the material strongly influences the form as the final outcome is re-conceptualized as skill and technology develops (Bleed 2001; Keller and Keller 1996; Schlanger 1996). In this sense, individual action plays a role in the construction of forms and styles, all of which are factored into the organization of the artifacts. James Deetz (1977) saw these slight style differences as variations on a theme, however, and returned to the concept of shared ideas of material culture. Deetz considered artifacts as "reflections of the mental templates of the makers" though this normative framework has been criticized as too formulaic (Neuwirth et al. 2002, 113). Certain concepts, though, overlap with the central dictates of the post-processual paradigm in archaeology which, at its core, attempts to account for human agency and individuals as major influencing factor in the variation found in the archaeological record (Johnson 2010, 108).

As noted above, throughout the 1960s and 70s the archaeological discipline was rich with processual concepts including Binford's (1965; Binford 1968) middle range theory and framing culture as consisting of multiple interacting systems all of which factor into the interpretation of the archaeological record. In the 1980s and 1990s, however, a paradigm shift took place (Kuhn 1962) primarily led by archaeologists influenced by the postmodern turn in the social sciences (Hodder 1982; 1985), who raised a number of questions regarding processual thought in archaeology. The idea of cultures

as systems was considered particularly problematic, or as Matthew Johnson (2010, 102) stated, "in particular, they pointed to the need to address cognitive factors, the difficulties of positivist epistemology, and the problems with developing middle-range theory..." Ian Hodder, for example, was a processualist, and believed that processes in modern cultures could be associated with the processes of the past as reflected in the archaeological record (Hodder and Orton 1976; Johnson 2010, 102). Over the course of his research in Africa, however, he came to several conclusions that led him to believe that processual concepts were no longer adequate in explaining patterns in the archaeological record and past human behavior (Johnson 2010, 103). Hodder (1991) explained that:

From a hermeneutic point of view, the failure of the processual archaeology of the 1970s and early 1980s was that it too often took a cavalier, externally based approach where the data were simply examples for the testing of universal schemes, with too little attention paid to context and to understanding the data in their own terms. The possibility that radically different processes might be encountered was thus difficult to entertain. From the point of view of critique, the failure of processual archaeology was its blindness to its own ideologies (12).

Post-processualism began to focus, to a much greater extent, on the context of material culture and considers the social factors embedded within a past culture.

Processual thinkers argued that the archaeological record is a reflection of systems operating within a society, and can give insight into the interaction between these systems that were part of a particular culture. Lewis Binford (1983, 25) stated, "the archaeological record is a static contemporary phenomenon. It is structured matter motionless and noninteractive in terms of the properties of historical interest to the archaeologists" (Binford 1983, 25). Material remains offer a snapshot of the systems functioning with one another and any changes that may be perceived are extrasomatic in

nature (Binford 1962). In contrast, one of the emphases of post-processualism is that cognitive processes as well as a number of other non-behavioral factors influence material culture, and objects are imbued with certain meanings and, over time, these meanings change. Where processualism narrows the focus to certain extrasomatic means of adaptation, a number of distinct frameworks within the post-processualist paradigm attempt to understand the beliefs and symbols that may give insight into the social structure or interaction between groups and individuals. Ultimately, the physical objects found in the archaeological record embody the beliefs and values of people. This adds a level of complexity to the organization of objects which may fill a particular cultural or societal role among one group of individuals, but not another.

The debates in historical archaeology have largely centered on topics well within the post-processual realm that typically involve research into race, class, gender, symbolic interpretation, and power relations (Shackel and Little 1992). However, in recent years there appears to be a reemergence of interest in the creation of typological systems facilitated in large part by a desire for flexibility in design and the utilization of alternate methods and technology which offer an alternate perspective on the organization of artifacts (See Fluzin et al. 2012; Smith et al. 2014).

On the topic of classifying artifacts, Michael Shanks and Ian Hodder (2007) explain that,

Classification operates under a 'rule of the same.' Taxa are characterized by relative *homogeneity*. This is a legitimate strategy for coping with the immense empirical variety and particularity that archaeologists have to deal with. However, we should be clear that classification does not give the *general* picture; it gives the *average*. It is not a general picture because there is no provision in classification for assessing the norm, the taxa..., not the variation within a class, nor the variability of variability. Classification is less interested in coping with particularity...Why are the members of a class of pots all in fact slightly different? (150).

This assertion is worthwhile to keep in mind when approaching the topic of classifying artifacts and does indeed factor into the broad epistemological framework of the research presented here. Particularities, to a degree, are not the end goal for the study of chemical data in the case of this exploratory examination of historic ceramic glazes. Rather the trends that manifest themselves are of central importance as they will inevitably lead to more focused questioning and a readjustment of the current lens of inquiry. Determining the reason for commonalities and divergence in glaze chemistry requires further research into the societal, economic, technological, and cognitive factors at play during the time these historic ceramic materials were being produced.

#### **Potentials of Material Science and Archaeometry**

Because particular constituent materials were chosen for a given end, material science techniques investigate the structure of assemblages. Formal, stylistic, spatial, chemical as well as other forms of evidence can be used to understand the association, context, and meaning of objects. Various techniques have been developed to analyze the constituent elements of an artifact to source those materials or understand the microstructure and begin to understand the processes involved in its creation (Henderson 2000; Rice 1987). A researcher can also undertake a detailed phase analysis to understand the properties and interactions of the material and thereby enter the mind of the maker who was forming educated decisions based on their ever-developing principled knowledge. However, in the words of Kingery (1996, 196), "there is always tacit knowledge embodied in artifacts, and it is not easy to interpret the function and use of a

complex construction without culture-specific knowledge or specific instruction." This means that the approach to the study of material culture always entails a confluence of evidence drawn from both the artifact itself in the form of chemical data as well as anthropological and historical information.

Nevertheless, there is an ever growing body of archaeological projects and scholarly literature using material science technology and techniques to characterize or "fingerprint" artifacts from the archaeological record including ceramic artifacts and assemblages (Maggetti 2012; Maggetti et al. 2014; Papadopoulou et al. 2007). Though the literature on historic fabric and glaze analysis is not as extensive as that involving prehistoric artifacts, several studies using French faience, i.e. French tin-glazed earthenware, have been undertaken. Work by Marino Maggetti, for example, contains a great deal of contextual and chemical information regarding French samples collected from several pottery shops. Maggetti analyzed these faience sherds to develop chemical reference groups which researchers can use to determine the provenance of archaeological samples by comparing the chemical signature of the artifact in question to the reference group (Maggetti 2012; Maggetti et al. 2014). In an effort to distinguish between pottery workshops, Maggetti, Rosen and Serneels (2014 utilized both X-ray fluorescence and X-ray diffractometric techniques to the study of French faience samples of sherds. While these techniques have certain advantages in terms of their abilities to provide high quality chemical and mineralogical information, both are destructive techniques that require that lab staff mill the samples to a fine powder.

Other archaeometrists have established non-destructive alternatives that do not require damage to artifacts and offer other useful features. Recent literature addressed

issues of reliability as it relates to portable instruments like pXRF analyzers. These articles emphasize the need for quality standards to check the instrument is operating consistently, performing multiple runs at appropriate reading locations on the artifact, and taking precautions to reduce attenuation, i.e., loss of x-ray intensity by absorption, during analysis (Craig et al. 2007; Shackley 2010; Speakman et al. 2011; Speakman 2012). This research was mindful of these necessary standards, and analytical practice followed the protocols established by the University of Wisconsin-Milwaukee Archaeological Research Lab.

Archaeologists are now utilizing field portable X-ray fluorescence instruments heavily in prehistoric contexts and in analysis driven by research designs from Art History. Hand-held pXRF analyzers provide data to sort and source materials beyond their macroscopic diagnostic characteristics at a level of accuracy that is adequate for the purposes of the archaeologist who is interested in the averaged patterns, as Shanks and Hodder (2007) would state, that are present in the data (Liritzis and Zacharias 2011; Shugar and Mass 2012). Researchers have used pXRF devices on a wide range of ceramic artifacts including Neolithic Grecian pottery (Papadopoulou et al. 2007), glazed stonewares from north-east Asia (Mitchell et al. 2012), cuneiform tablets from the Near East (Goren et al. 2011), and pre-colonial pottery from Sao Luis, Brazil (Ikeoka et al. 2011). Each of these studies has achieved some level of success for "sourcing" artifacts, at least at the regional level, usually in conjunction with neutron activation or mass spectroscopic techniques used for comparative purposes. Nicola Forster and Peter Graves (2013) undertook a pilot study of lead glazed Byzantine vessels from Cyprus and noted that some of the compositional groups matched well with particular pottery

manufacturers, though this was not the case for all groups. Nevertheless, these results encouraged the authors to pursue a larger characterization study of Cypriot ceramics (2013, 485). These studies have shown field portable XRF has a great deal of potential for non-destructive, in-situ analysis of ceramic materials, though the literature is sparse with regards to the application of this technique to the study of historic artifacts in general and ceramics in particular. The research presented here is intended to add to the literature on classification and pXRF with a focus on historic rather than prehistoric materials.

#### **Chapter 3: Methods for Assigning Provenance Using Glaze Constituents**

This proof-of-concept study uses portable X-Ray fluorescence (pXRF) to source historic ceramic materials through the use of a body of data with known production location information. This case study focuses on lead-glazed and tin-opacified wares housed in the Chipstone Foundation collection of British and European ceramics. As stated earlier, the premise is to gain elemental net intensity data both non-destructively and *in situ*. In other words, the entirety of the pXRF instrument readings are performed at the facility where all the samples are currently curated with little sample preparation. This is meant to demonstrate to the archaeological community that useful, reliable, and meaningful information can be obtained quickly, cost effectively, and without affecting the integrity of these valuable cultural resources.

Speakman and Shackley (2013) have recently commented on pXRF studies that they characterize as examples of "silo science" due to the use of uncalibrated data. Speakman and Shackley argue that the result is not good science as these studies lack reproducibility and inter-laboratory comparability. Because my study relies upon uncalibrated net intensity values, it might be argued that the result is an example of this genre. Certainly, my results would be more broadly comparable if my data represented calibrated values for analyzed elements. However, the instrument available to me lacked that capability, as the appropriate calibrations had not been loaded at the time I collected and analyzed the data. Consequently, this work must be seen as a preliminary "proof of concept" study valid only at the level of the Chipstone collection. However, if one assumes: 1) that the analyzed sample is representative of Staffordshire and London wares in general and; 2) that the net intensity values are a reasonable proxy for the elemental concentrations in the samples, results suggest a statistically valid separation between London and Staffordshire wares based on the variation in tin content. While this result cannot be generalized to other collections (i.e, recorded net intensity values cannot be used to suggest the real range of difference because a different instrument will likely return different net intensity values), other researchers can attempt to replicate my basic finding that tin concentrations vary significantly. This variation is further supported by observed shifts in production, distribution, and social vogues during the time the pottery in the Chipstone sample was produced and used. Thus, the results presented here should have analytical utility beyond the Chipstone collection and the present study.

Toward that end, I analyzed the readings using R Statistical Software to establish the chemical fingerprint of the samples and used factor analysis to link those signatures to the known provenance designations. Clusters, on the one hand, need to be identified among the intensity readings which act as an indirect measure of the variation in glaze production strategies utilized by the various production centers. I can then compare the extracted factors and samples designated as coming from the Staffordshire region and London region, two major pottery manufacturing areas with the former located in the north of England and the latter in the South (shown in Figure 3.1). The geographical separation, the development of independent pottery manufacturing techniques, and the tin glazed industry's waning in London should produce distinguishable chemical signatures. In SPSS, I used factor analysis to study a reduced dataset of only London and



# *Figure 3.1 Map showing major pottery manufacturing sites in the 17th and 18th centuries.* Staffordshire materials with averaged net intensities of stabilizers and fluxes to determine differences in glaze production strategies. Two binary logistic regression models, utilizing the factor scores, determined the probability of samples being correctly assigned to either Staffordshire or London. Other researchers can test this model in future studies using similar lead and tin-glazed ceramic artifacts held by Chipstone and other facilities.
## An Initial Exploration of the Chipstone Data

Prior to determining the relationship between the Staffordshire and London materials this research aims to utilize the entire dataset of analyzed samples from Britain and Continental Europe. Analysis of the complete dataset seemed a natural starting point for getting a sense of the data and the interaction between chemical variables before refining the approach. Though the number of Continental European artifacts is small and cannot be included in the factor analysis and regression models, their inclusion in the principle component analysis and analysis of variance is useful. Principle component scores coupled with ANOVA and Tukey post-hoc tests for determining potential differences between groups provided some sense of the divergence in compositions between the artifacts. I posit that English ceramics, broadly speaking, are not the same compositionally as Continental European ceramic artifacts in the Chipstone dataset. The major influencing variables that help to capture the greatest trends in the data were retained while removing redundant or unnecessary variables to further distinguish the English and Continental European artifacts from one another.

With this broad geographical understanding that English ceramics are unique from those in Europe, the question then turns to whether the two major sets of artifacts from Staffordshire and London have unique compositional characteristics determined through factor analysis and logistic regression. This allowed for an appraisal of the level of geographical focus that can be achieved with the instrument starting with a broad assessment of all the data and moving toward a narrower regional assessment. A reduced dataset with all representative samples, but using only data of elements uses as glaze stabilizers and fluxes, was examined using PCA and ANOVA. I was able to determine the appropriateness of using those fundamental glaze constituents for the final regression model that focuses on distinguishing London and Staffordshire made materials. The reason for retaining the stabilizers and flux components in the second principle component analysis and subsequent factor analysis of the London and Staffordshire materials is based on the assumption that the glaze manufacturing process became more standardized over time. The fundamental constituents of the lead based glazes were retained, but variability in decorative colorants will be present even in a single pottery shop (Hale 2008; Owen and Sutherland 1901). I offer further discussion of this topic in the subsequent chapters.

## A Note Regarding the Relationship between Glaze Chemistry Readings

Glaze is a vitreous, non-permeable coating in which elements are not represented randomly. Particular elements will correlate because of the nature of glaze production. Silicon and aluminum, for example, are fundamental constituents of the glaze composition which act as stabilizers to keep the glaze from running or from cracking. Lead and tin also likely correlate as an increase in the percent of lead will require a decrease in tin or vice versa depending on the level of opacity or translucence that the potter would like to achieve. Despite these correlations between elements, other forms of analysis are required to make a determination if particular production factors have an effect on the classification of artifacts into one category or another. It is highly useful, nevertheless, to analyze the chemical variables using principle component analysis to understand the exact underlying structure of the chemical data which can be taken into consideration when determining which variables to include in the regression models.

#### The Instrument and Instrument Specifications

The University of Wisconsin-Milwaukee Archaeological Research Lab (ARL) loaned the pXRF instrument for the purposes of this experiment. ARL's instrument is a Bruker AXS Tracer IIIv +with a Si pin detector, and an X-ray tube featuring a Rh target. As such, the analysis followed the UW-Milwaukee pXRF protocols. I chose not to use a filter in order to gain a wide spectrum of chemical information, and after consultation with UW-Milwaukee ARL staff and consultants at Bruker Corporation, determined that the instrument should be set at 15 KeV and 25  $\mu$ A. Depending on the amount of lead, a 15 KeV beam under vacuum could penetrate up to 5 mm, so this protocol was meant to minimize depth of penetration. Readings were taken under vacuum and without a beam filter to reduce the amount of atmospheric attenuation and a voltage regulator was put in place to maintain a steady power output allowing the instrument to operate consistently. The voltage regulator stopped functioning midway through the experiment, so power levels were checked regularly to ensure that fluctuations were not occurring.

Three flat or approximately flat areas were chosen on each vessel to accommodate the collimated 3x4mm X-ray beam. Furthermore, plain white areas or low colorant areas were targeted. All vessel locations were scanned for three continuous runs at 180 seconds per run totaling nine minute scans for each location (180s x 3 = 540s). The scan time for a single sample, therefore, was 1,620 seconds or 27 minutes yielding 9 cases of net intensity readings to gain a representative overview of the glaze surface. Before and after each analysis session a kaolinite clay standard (Kaolin KGa-2) was used to be certain that

the instrument was running consistently. Precise chemical compositional data for this standard has been published in the *Data Handbook for Clay Materials and Other Non-metallic Minerals* (Van Olphen and Fripiat 1979) and is shown below in Table 3.1.

 Table 3.1 Characteristics of the kaolin clay standard used to check consistent instrument performance.

 Kaolin Kga-2 (high-defect)

	Kaolin Kga-2, (ngn-defect)
Origin:	Probably lower tertiary (stratigraphic sequence uncertain)
	County of Warren, State of Georgia, USA
Location:	33019' N-82028' W approximately, topographic map Bowdens Pond, Georgia
	N 3315-W 8222.5/7.5, Collected from face of Purvis pit, October 4, 1972.
Chemical Composition(%):	SiO2: 43.9, Al2O3: 38.5, TiO2: 2.08, Fe2O3: 0.98, FeO: 0.15, MnO: n.d.,
	MgO: 0.03, CaO: n.d., Na2O: <0.005, K2O: 0.065, P2O5: 0.045, S: 0.02,
	Loss on heating: -550oC: 12.6; 550-1000oC: 1.17, F:0.02.
Cation Exchange Capacity:	3.3 meq/100g
Surface Area:	N2 area: 23.50 +/- 0.06 m2/g
Thermal Analysis:	DTA: endotherm at 625oC, exotherm at 1005oC, TG: dehydroxylationweight loss
	13.14% (theory 14%) indicating less than 7% impurities.
Infrared Spectroscopy:	Typical spectrum for less crystallized kaolinite, however the mineral
	is not extremely disordered since the band at 3669 cm-1 is still present in the spectrum.
Structure:	(Catr Ktr)[Al3.66 Fe(III).07 Mntr Mgtr Ti.16][Si4.00]O10(OH)8, Octahedral charge: .16,
	Tetrahedral charge: 0.00, Interlayer charge: .16, Unbalanced charge: .15, Extra Si: .04

## **The Chipstone Ceramic Samples**

The Chipstone Foundation owns and curates all the objects used in this study. The foundation began in the 1980s with an endowment from the Stone family dedicated to maintaining the large ceramic, furniture, and print collections accumulated by Stanley and Polly Stone or purchased during the years since they created their foundation. The Chipstone Foundation now owns and curates approximately 505 ceramic objects. The ceramic materials are primarily seventeenth, eighteenth, and nineteenth century English lead and tin-opacified wares with comparable earthenware fabrics. Through the eighteenth and nineteenth centuries a transition to cream-colored wares and whiter improved earthenwares occurred, and these types are dominant in the Chipstone collection. Of the many vessels in the collection, I analyzed 102 (N=102) using the Bruker pXRF instrument. Table 3.2 lists the Chipstone vessel types and the number of

each analyzed. For more detail regarding individual vessels and vessel images see Appendix A and B.

Table 3.2 Chipstone vessels types and the number analyzed using the pXRF instrument.

	Chipstone Vessel Types										
Chargers	Chargers Plates Bottle/Jugs Cups/Tankards Pots/Teapots Jars Bowls Figurines Wall Pockets Fruit Stands Handwarmers Total									Total	
21	21     17     9     14     18     8     4     6     2     2     1     102										102

The analyzed samples can be subdivided into English and Continental European made artifacts with 32 (n=32) attributed to London based potteries, 41 (n=41) produced in Staffordshire, and 7 (n=7) from Bristol. Experts attributed objects to Kent (n=2), Essex (n=1), Liverpool (n=1), the general Midlands area (n=2), Stoke-on-Trent (n=4), Derbyshire (n=1), England generally (n=2), and Glasgow (n=1). Ceramicists have also identified samples from European pottery shops including the Netherlands (n=4), France (n=2), Italy (n=2), Portugal (n=1), and Czechoslovakia (n=1). One vessel has been traced to Massachusetts (n=1) and one is unknown (n=1).

#### **Net Intensity Readings and Initial R Preparation**

Once analyzed, I imported the resulting spectra into the Bruker Artax software to begin the Bayesian deconvolution process which helps to identify the most probable compositional components of the historic glazes and their associated net intensities. The Artax software can only analyze 100 spectra at one time resulting in several project files that were combined in Microsoft Excel. I created a new characterization method using the software by identifying components in a random selection of spectra to craft a preset list of elements. This was an iterative process that entailed selecting a spectrum, identifying the elements, and testing the updated method on a subsequent spectrum to determine if additional elements should be included. The final method was used to analyze all the remaining spectra in each project set. Net intensities were extracted for 18 elements including: Al, Co, Cr, Cu, Fe, Ga, K, Mn, Ni, Pb L, Pb M, Rh, Rh L, Si, Sn, Sn L, Ti, Zn. A majority of identified elements and their associated net intensities come from K shell readings unless otherwise labeled. The instrument detected only the L and M shell spectral peaks for lead as greater power levels are needed to detect K shell lead readings. This analysis uses the lead L shell counts as a measure of lead in the artifacts. Because of the Rh target, this element will always appear in the list of identifiable components and therefore subsequent analyses did not use either the K shell or. A qualitative scan of the data also lead to the removal of certain other elements from the analysis including Cr, K, Pb M, and Sn K because they appeared at negligible levels or presented as 0 or negative values which are essentially noise in the spectrum requiring correction. This left a total of 12 remaining major glaze elements that were used in the initial principle component analysis and tests of significance.

I removed particular artifacts in the dataset due to the ambiguity of their assigned provenance designations and low sample sizes. Those items included the England (general) materials and the samples from Liverpool, Essex, Kent, Derbyshire, the Midlands, Massachusetts, Czechoslovakia, and the unknown sample. The sample from Glasgow was retained due to the suggested relationship between London and Glasgow pottery shops which entailed the occasional movement of potters between those two locations. The dataset now featured 90 samples. Subsequent to this qualitative culling, a letter designation was assigned to the remaining British and Continental European samples (presented in Table 3.2), included in a new field in the R prepared dataset. A unique artifact identifier was assigned to each item that consisted of the artifact

Provenance	<b>R</b> Designation	# of Samples
London	L	32
Staffordshire	S	41
Bristol	В	7
Glasgow	G	1
Italy	Ι	2
France (Rouen)	FR	1
France (Nevers)	FN	1
Portugal	Р	1
Netherlands	Ν	4

Table 3.3 List of provenance designations and number of samples.

designation, the reading number, and the reading location. After converting the spreadsheet to a .txt file, I uploaded the data into the R Statistical Software.

## **Removing Anomalous Readings with R**

The Mahalanobis distance metric was applied in order to remove extreme or anomalous chemical readings from the dataset. According to Hulit (2012:32) "the Mahalanobis distance is a robust metric designed to measure the distance of each reading from the center of all the readings for the artifact. It differs from Euclidean distance metrics in that it takes into account the nature of chemical data to tend towards elliptical shapes when projected in two dimensions." In this case, I analyzed the three measurements that comprise a single case (i.e. a single reading location) to check for consistency among those measurements. The software removed cases from the dataset that deviated greatly from other measurements leaving readings that represent the net intensities of the glaze components across the surface of the ceramic object. As a result of the Mahalanobis distance metric analysis, the software identified and removed 63 readings in this initial broad analysis. Furthermore, a software function identified any cases that included net intensity values less than or equal to zero and removed those as well. As a result 750 readings remained after applying the distance metric and 721 after removing zero or negative net intensities for all 102 samples. Having culled any outliers from the dataset, the remaining cases were ready to be examined using principle component analysis.

## **R** Statistical Software Analysis

I used principle component analysis (PCA) to analyze relationships among elements to see if they are indicative of variations in the glaze production process or some other latent variable(s) linked to particular sites of manufacture. PCA allows a researcher to see correlations among multiple variables and identify compositional differences between artifacts based on its position in multidimensional space. A principle component is essentially a line that fits the greatest spread among data points in a cloud. The line is a representation of variation among two or more variables. Within the R software, I applied the GrayILRv2 function contained within the Hulit Source for clustering and compositional analysis (Hulit 2012). As a result, the function produced a biplot "which aims to represent both the observations and variables of a matrix of multivariate data on the same plot" (Hulit 2012, 48). Rather than thinking in so many dimensions, the plot provides a more intuitive two dimensional representation. The number of dimensions is equivalent to the number of elemental variables and with each component more of the variation in the data is explained, i.e. particular trends in the data are being captured. The first principle component explains the highest percentage of variation. The elements (i.e. variables) in the first principle component with high loading values have the greatest influence on the distribution of the data. Subsequent principle components capture the remaining variation characterized by alternative sets of variables

that influence the respective components. The amount of variation captured by each component is represented visually in the form of a screeplot. Focus is given to those components up to the point of a horizontal leveling as these components represent a majority of the variation among the artifacts.

Furthermore, the correlation between elements is representative of a latent variable that cannot be measured directly. Ultimately, those elemental variables with the highest loading values, i.e. those elements with the highest level of interaction and explanatory power, can be looked at in greater detail while ignoring others in an effort to reduce the dimensionality of the overall dataset. Archaeometric convention states that explaining 50-60% of the variation is adequate and follows UW-Milwaukee ARL standards.

# Chapter 4: Results of Dimension Reduction and the Development of a Glaze Chemistry Regression Model

The following section provides the results of the statistical analysis of the Chipstone ceramic data and presents two logistic regression models used to predict the provenance of London and Staffordshire materials. Prior to principle component analysis the Mahalanobis distance metric function removed anomalous readings from the dataset. After running the distance metric function, 750 readings remained for subsequent culling. Another function in the Hulit (2012) package that identified zero or negative intensity readings removed them from the dataset. Upon running this package 721 cases remained for use in the principle component analysis that included all remaining readings and utilized all of the relevant, identified elements. I created a subset of net intensity measures and the GrayILRv2 command, developed by Dr. J. Patrick Gray (Hulit 2012), provided the loading values, individual reading scores or standing on each component, and the percent of variation explained by each component. It also automatically generated a biplot and a screeplot for the data.

The screeplot in Figure 4.1 shows four principle components that account for a majority of the variance, however the first three components are adequate per ARL standards. Analyzing the percent of variation explained by each of the four components, I determined that Component 1 accounts for ~29%. Each additional component explains an increasing amount of variation with all four major principle components accounting for a cumulative sum of 70% of the variation (Table 4.1). In studying the PCA biplot, the data appears to

Screeplot of Chipstone Ceramic Data



Figure 4.1 Screeplot of entire Chipstone dataset. This plot indicates four major principle components.

Table 4.1 Percentage of the variation for each principle component and the associated cumulative sum for the entire Chipstone dataset.

Percent Variation of Chipstone Ceramic Data										
Comp.1	Comp.2	Comp.3	Comp.4	Comp.5	Comp.6	Comp.7	Comp.8	Comp.9	Comp.10	Comp.11
29.429362	18.514763	12.673716	9.466257	7.761725	6.438849	5.317259	3.905716	3.467725	1.994504	1.030124
Cumulative Sum of Percent Variation Chipstone Ceramic Data										
		Cum	ulative Sun	n of Percent	t Variation	Chipstone (	Ceramic Da	ta		
Comp.1	Comp.2	Comp.3	Comp.4	Comp.5	Comp.6	Chipstone Comp.7	Comp.8	ta Comp.9	Comp.10	Comp.11

be elliptical in shape with several possible clusters being apparent (Figure 4.2). The loading values indicate the explanatory weight of particular variables on the distribution of the data. This information factors into the decision to retain certain variables or remove them to reduce dimensionality when conducting subsequent tests. The analysis focused on the loadings of the four major components identified which are listed in Table 4.2 with notable values highlighted. Viewing the loading measures, overall the higher values are often associated with fundamental glaze constituents, i.e. stabilizers such as aluminum and silicon, along with fluxes such as lead, particularly in the first principle component. It is possible then to say that the principle components with these variables



Figure 4.2 PCA biplot showing multiple clustering indicating possible compositional differences.

	PCA Loadings for All Data										
	Comp. 1	Comp. 2	Comp. 3	Comp. 4							
Al	-0.59803652	-0.41256175	-0.16168662	0.03282603							
Co	-0.12710500	-0.03273245	-0.12366019	-0.30431481							
Cu	-0.03810563	0.24323265	0.16036956	-0.47004273							
Fe	0.14959512	0.14602156	-0.29178832	-0.20848093							
Ga	0.19149149	-0.32045661	0.18731731	0.29321967							
Mn	-0.07252857	0.48397013	-0.19274925	0.69077076							
Ni	0.26524659	-0.06133849	0.42470556	-0.12335846							
Pb	0.37243646	-0.11802426	0.22688753	0.11601712							
Si	-0.39461537	-0.19603727	0.08444303	0.05249406							
Sn	-0.25612610	0.47226534	0.40762361	-0.02214774							
Ti	0.27781315	-0.33805390	-0.12613309	0.12187723							
Zn	0.22993438	0.13371504	-0.59532913	-0.17886021							

Table 4.2 PCA loadings for the entire Chipstone dataset with high loading values indicated.

captured the greatest amount of variation in the data. In other words, the opposition of aluminum and silicon to lead represents the greatest trend in the data.

Furthermore, aluminum and tin oppose one another in the second principle component and a correlation between tin and manganese as well as titanium and gallium. Nickel and tin cluster in the third principle component and are in opposition to zinc. Cobalt and copper cluster in the fourth component and oppose manganese. Based on these results it is difficult to conceptualize the groupings of variables apart from the loading scores on PC1 which does not feature any colorants. However, Components 2 and 3 show tin as positively correlated with particular colorants which may be some indication of a conscious decision by the pottery to create a colored opaque glaze for purely artistic reasons or to better cover the coarse earthenware fabric. This is discussed further below.

To determine if the compositions of categorical groups differ significantly from one another it is necessary to run an ANOVA test with a 95% confidence interval ( $\alpha$ =.05) on all four components. Each of the four ANOVA tests show statistically significant results (PC1: p=1.24e-13; df=8; PC2: p=<2e-16, df=8; PC3: p=<2e-16, df=8; PC4: p=<2e-16, df=8). The p-values and associated ANOVA information is shown in Table 4.3. Because the analysis concluded that at least one significant grouping is present in

I able 4.	Table 4.5 ANOVA results of the entire Chipstone dataset.									
ANC	ANOVA Results for Chipstone Ceramic Data									
	Df Sum Sq Mean Sq F value Pr(>F)									
ANOVA PC1	8	196.1	24.51	10.26	1.24e-13 ***					
Residuals	712	1701.3	2.39							
	Df	Sum Sq	Mean Sq	F value	Pr(>F)					
ANOVA PC2	8	267.8	33.47	15.82	<2e-16 ***					
Residuals	712	1506.3	2.12							
	Df	Sum Sq	Mean Sq	F value	Pr(>F)					
ANOVA PC3	8	273	34.12	12.62	<2e-16 ***					
Residuals	712	1925	2.70							
	Df	Sum Sq	Mean Sq	F value	Pr(>F)					
ANOVA PC4	8	356.5	44.56	26.36	<2e-16 ***					
Residuals	712	1203.7	1.69							

Tabl	le	4.3	ANC	)VA	results	ofi	the	entire	Ch	ipstone	e dataset.
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each principle component, I applied a Tukey post-hoc test to determine significant differences between each of the individual provenance categories. Those pairings with significant values less than  $\alpha$ =.05 have been consolidated in Table 4.4. It is particularly

Tukey Post-Hoc PC1					Tukey Post-Hoc PC2				
	diff	lwr	upr	p adj		diff	lwr	upr	p adj
S-FN	1.97278817	0.349066692	3.5965096	0.0053047	B-P	1.813355570	0.188139755	3.4385710	0.0159683
L-FN	2.29141596	0.658573747	3.9242582	0.0004912	L-P	2.362470770	0.826051102	3.8988900	0.0000728
B-FN	2.67201166	0.944800641	4.3992227	0.0000633	G-P	3.347923208	0.823702120	5.8721440	0.0013575
N-FN	3.21698113	1.365786405	5.0681759	0.0000031	L-N	1.569992631	0.651561442	2.4884240	0.0000050
FR-FN	3.28490610	0.947887320	5.6219249	0.0004763	G-N	2.555445069	0.352124268	4.7587660	0.0099232
P-FN	3.77551338	1.508272133	6.0427546	0.0000102	B-S	0.657435048	0.005971059	1.3088990	0.0459528
I-FN	4.03914575	2.056500795	6.0217907	0.0000000	L-S	1.206550248	0.827519537	1.5855810	0.0000000
I-G	2.71470229	0.267860620	5.1615440	0.0170599	G-S	2.192002687	0.153677152	4.2303280	0.0242134
B-S	0.69922349	0.006874961	1.3915720	0.0456283					
N-S	1.24419296	0.283458612	2.2049273	0.0020167					
P-S	1.80272521	0.179003729	3.4264467	0.0169227					
I-S	2.06635758	0.871799255	3.2609159	0.0000036					
I-L	1.74772979	0.540803185	2.9546564	0.0002650					
I-B	1.36713409	0.035309751	2.6989584	0.0390558					
	Т	ukey Post-Hoc	PC3				Tukey Post-H	oc PC4	
	diff	lwr	upr	p adj		diff	lwr	upr	p adj
S-P	2.28969478	0.56247461	4.016915	0.0013691	S-FR	2.294095600	0.847502700	3.740688500	0.000035200
S-FN	1.74412789	0.01690773	3.471348	0.0456880	S-FN	2.069370600	0.703600900	3.435140300	0.000101400
S-N	1.45793225	0.43595911	2.479905	0.0003573	S-B	1.652746800	1.070387900	2.235105700	0.000000000
S-L	1.19401469	0.76552051	1.622509	0.0000000	S-I	1.512758300	0.507972900	2.517543700	0.000116600
S-B	0.82512383	0.08864386	1.561604	0.0152104	S-P	1.437015000	0.071245300	2.802784700	0.030499400
					S-L	1.259264200	0.920439800	1.598088600	0.000000000
					S-N	1.156932800	0.348825100	1.965040600	0.000333100

noteworthy that compositional differences exist between British artifacts and several Continental European artifacts across all four principle components. Furthermore, in the case of the second, third, and fourth principle components there are significant differences between Staffordshire and London materials based on the associated chemical variables for those components.

P=Portugal N=Netherlands

S=Staffordshire L=London B=Bristol G=Glasgow I=Italy FR=France (Rouen) FN=France (Nevers)

These components feature several colorants and in the case of Component 2 gallium and tin load highly. The p-value=.0000 in the Tukey post-hoc test indicates there are some compositional differences between artifacts involving these variables which appear to be negatively correlated. It is curious that Staffordshire and London materials do not differ significantly in the first principle component, yet Bristol and Staffordshire materials do. Because the first component is characterized by fundamental glaze elements it is of interest to see how retaining those variables and removing particular colorant variables effects the loadings and subsequent ANOVA results. Furthermore, the presumed variability in the application of color to each item during production makes it worthwhile to investigate those constituents that are necessary to achieve a glaze that will behave appropriately when fired and therefore be more consistent throughout the production of successive items.

## **Reducing the Dataset to Fundamental Glaze Constituents**

Because of the assumed high degree of variability in the application of colorants, which are subject to the whims of the artist and the desires of the mass market, I reran the principle component analysis with a reduced number of variables based on the higher measures for stabilizing and fluxing agents particularly in the first principle component. For this subsequent analysis aluminum, copper, gallium, lead, silicon, tin, and zinc were retained as variables. I chose to retain copper, despite being a colorant, for its fluxing effect. Once again, the analysis identified four components as accounting for a majority of the variance as shown in the screeplot (Figure 4.3). The screeplot shows that these first



Figure 4.3 Screeplot of Chipstone stabilizer and flux dataset.

four principle components capture ~95% of the variation, summarized in Table 4.5.

Table 4.5 Percentage of the variation for each principle component and the associated cumulative sum for the reduced chipstone dataset.

	Percent Variation of Stabilizer and Flux Data								
Comp. 1	Comp. 2	Comp. 3	Comp. 4	Comp. 5	Comp. 6				
38.334161	24.404741	22.567737	9.815842	3.156235	1.721285				
Cumu	lative Sum of	Percent Vari	ation Stabili	izer and Flux	x Data				
Comp. 1 Comp. 2 Comp. 3 Comp. 4 Comp. 5 Comp. 6									
38.33416	62.7389	85.30664	95.12248	98.27871	100.00000				

Furthermore, the first two PCS account for  $\sim 63\%$  of the variation. Looking forward to the factor analysis, it is possible to see some overlap in how certain variables load, notably gallium in the second PC and second Factor component. The biplot shows two larger clusters, however, surrounded by smaller groupings (Figure 4.4). This is potentially



Figure 4.4 PCA biplot of the reduced dataset showing two clusters.

explained by the much larger number of Staffordshire and London samples also hinted at by the unusual shape of the screeplot that plateaus after components 1 and 2 and descends between components 3 and 4.

	PCA Loadings for Stabilizers and Fluxes								
	Comp.1 Comp.2 Comp.3 Comp.4								
AlK	0.55974571	0.26484550	-0.04283422	-0.19295304					
CuK	-0.07348023	-0.34137870	-0.35836980	-0.73550883					
GaK	-0.28498131	0.36710920	0.33793103	-0.08806853					
PbL	-0.52695423	0.18568500	0.32637015	-0.03844671					
SiK	0.51571173	0.17644760	0.16014641	0.21628085					
SnL	0.04349591	-0.77352390	0.30500527	0.33544776					
ZnK	-0.23353758	0.12081530	-0.72824884	0.50324850					

Loading measures for this reduced dataset are presented in Table 4.6 which show

Table 4.6 PCA loadings for the stabilizer and flux Chipstone data with major loading values indicated.

higher values and a positive correlation of aluminum and silicon and opposition to lead in Component 1. Copper and gallium are negatively correlated in Component 2 with a high value for tin as well. Gallium, lead, and tin correlate in Component 3, though oppose copper. There is also a high value for zinc. Component 4 features a high loading value for copper and slight clustering of tin and zinc. To determine whether this reduction helps to explain the compositional differences, I used ANOVA once more to determine compositional differences among the four principle components. All four components returned significant values indicating at least one significantly different provenance grouping based on this set of variables (PC1: p=1.73e-11, df=8; PC2: <2e-16, df=8; PC4: p=9.1e-14, df=8) detailed in Table 4.7. The Tukey post-hoc test

able 4.7 ANO	able 4.7 ANOVA results for the Chipstone stabilizer and flux data								
AN	ANOVA Results for Stabilizer and Flux Data								
Df Sum Sq Mean Sq F value Pr (>F)									
ANOVA PC1	8	120.8	15.099	8.788	1.73e-11 ***				
Residuals	6695	1194.2	1.718						
	Df	Sum Sq	Mean Sq	F value	Pr (>F)				
ANOVA PC2	8	210.8	26.344	12.56	<2e-16 ***				
Residuals	695	1457.6	2.097						
	Df	Sum Sq	Mean Sq	F value	Pr (>F)				
ANOVA PC3	8	361.5	45.19	194.8	<2e-16 ***				
Residuals	695	161.2	0.23						
	Df	Sum Sq	Mean Sq	F value	Pr (>F)				
ANOVA PC4	8	94.2	11.779	10.36	9.1e-14 ***				
Residuals	695	789.9	1.137						

Table 4.7 ANOVA results for the Chipstone stabilizer and flux data.

showed that the number of pairings which present as being significantly different increase in the case of the second, third, and fourth principle components. Significant pairings increase from eight to 14 for Component 2, five to 13 for Component 3, and seven to eight for Component 4. The number of pairings drops from 14 to 12 for Component 1. The p-value for the Staffordshire and London pairing in Principle Component 1, which together represent the greatest number of artifacts analyzed, drops from p=.2530 to p=.0731. While this is not statistically significant based on the assigned confidence interval, however it is an improvement. Table 4.8 shows these results.

Table 4.8 Tukey post-hoc results for the Chipstone stabilizer and flux datawith provenance designation key

Tukey Post-Hoc PC1				Tukey Post-Hoc PC2					
	diff	lwr	upr	p adj		diff	lwr	upr	p adj
L-P	1.53405493	0.150526231	2.9175836	0.0171851	S-G	1.74151261	0.21867571	3.2643495	0.0118574
S-P	1.86185921	0.483489979	3.2402284	0.0009907	I-G	2.04783330	0.12259049	3.9730761	0.0272292
G-P	2.07923229	0.156526712	4.0019379	0.0227888	N-G	2.67099607	0.87569789	4.4662942	0.0001512
FN-P	2.81201647	0.662366284	4.9616667	0.0017129	P-G	4.40658258	2.28235713	6.5308080	0.0000000
S-FR	1.62348528	0.245116050	3.0018545	0.0081216	N-FN	2.21372093	0.12777295	4.2996689	0.0278909
FN-FR	2.57364254	0.423992355	4.7232927	0.0065158	P-FN	3.94930744	1.57435119	6.3242637	0.0000106
L-I	1.15850726	0.038681647	2.2783329	0.0361804	S-L	0.69757914	0.31926150	1.0758968	0.0000005
S-I	1.48631153	0.372866671	2.5997564	0.0012176	N-L	1.62706260	0.60374077	2.6503844	0.0000332
FN-I	2.43646879	0.446279443	4.4266581	0.0047631	P-L	3.36264911	1.83411197	4.8911862	0.0000000
L-N	1.01654783	0.090305941	1.9427897	0.0193282	N-B	1.23163445	0.08911369	2.3741552	0.0235898
S-N	1.34435210	0.425834768	2.2628694	0.0002134	P-B	2.96722096	1.35644726	4.5779947	0.0000005
FN-N	2.29450936	0.406449967	4.1825688	0.0052899	P-S	2.66506997	1.14223308	4.1879069	0.0000026
					P-I	2.35874928	0.43350648	4.2839921	0.0047113
					P-FR	2.30324044	0.17901499	4.4274659	0.0221354
	T	ukey Post-Hoc F	PC3		Tukey Post-Hoc PC4				
	diff	lwr	upr	p adj		diff	lwr	upr	p adj
FN-S	0.84992117	0.232414080	1.4674283	0.0007069	S-I	1.08352579	0.17794459	1.9891070	0.0065712
P-S	1.02653397	0.520048006	1.5330199	0.0000000	N-I	1.52355894	0.37900022	2.6681177	0.0012777
N-S	1.08595130	0.748439319	1.4234633	0.0000000	G-I	1.54515919	0.12787687	2.9624415	0.0208296
G-S	1.32026803	0.813782067	1.8267540	0.0000000	N-P	1.33938117	0.01775859	2.6610038	0.0441655
B-S	1.34232461	1.131634869	1.5530143	0.0000000	S-B	0.75706517	0.29072780	1.2234025	0.0000198
L-S	1.47692630	1.351100238	1.6027524	0.0000000	N-B	1.19709833	0.35602287	2.0381738	0.0003746
I-S	1.54275162	1.133612919	1.9518903	0.0000000	S-L	0.59399604	0.31549460	0.8724975	0.0000000
FR-S	1.82822128	1.321735317	2.3347072	0.0000000	N-L	1.03402919	0.28070295	1.7873554	0.0007431
L-FN	0.62700513	0.007942081	1.2460682	0.0444162					
FR-FN	0.97830011	0.188404615	1.7681956	0.0040230					
FR-P	0.80168731	0.095183305	1.5081913	0.0130513					
L-N	0.39097500	0.050624601	0.7313254	0.0112112					
FR-N	0.74226997	0.145165107	1.3393748	0.0038084					

S=Staffordshire L=London B=Bristol G=Glasgow I=Italy FR=France (Rouen) FN=France (Nevers) P=Portugal N=Netherlands

Based on the outcome of this second analysis it appears that the removal of

particular colorants improves the ability to detect differences between groups of both

British and Continental European made artifacts. Furthermore, the analysis showed potential compositional distinctions between those materials made in Britain which had highly significant values, particularly in those components with higher lead, tin, gallium, zinc, and copper loadings. With this knowledge in mind regarding the relationships between fundamental glaze constituents, the focus turns to the Staffordshire and London materials in particular to determine those glaze constituents that best factor into each group and if those artifacts can be sorted into their respective provenance categories.

## Factor Analysis of Staffordshire and London Mean Net Intensity Readings

Due to the results of the principle component analysis of the overall dataset, I determined that the analysis should be re-focused to emphasize fundamental glaze elements of the Staffordshire and London made materials. Toward that end, I placed those measures into a separate dataset and averaged the multiple readings for each pot to achieve a single representative reading of each glaze constituent variable. Furthermore, I removed copper from the analysis so as to have a dataset that included only those variables which constituted the fundamental aspects of the glaze, i.e. stabilizing and fluxing agents. Within SPSS, I conducted a factor analysis to see if these observed variables hint at some broader unobserved variables such as different glaze production strategies. Variables now correlate positively or negatively with the factor, i.e. the latent variable. The factor analysis utilized the Anderson-Rubin method "in which the least squares formula is adjusted to produce factor scores that are not only uncorrelated with other factors, but also uncorrelated with each other." (DiStefano et al. 2009, 5). This aids in the elimination of multicollinearity which is understandable given that there are necessary elements in the glaze chemistry to achieve a given end. (DiStefano et al. 2009).

As a result, the factor analysis extracted two components that cumulatively

account for ~71% of the variance. Table 4.9 details these values and Table 4.10 shows

Staffordshire and London adda.						
Factor Loadings						
	Comp. 2					
Alkavg	0.892					
GaKavg		0.893				
PbLavg	-0.852	0.348				
SiKavg	0.974					
SnLavg	0.516	-0.397				
ZnKavg		-0.617				

 Table 4.9 Factor loading values for the

 Staffordshire and London data.

 Table 4.10 Factor analysis results of the Staffordshire and London mean intensities.

Factor Analysis of Staffordshire and London Mean Net Intensities								
	Initial Eigenvalues			Extraction Sums of Squared Loadings				
Component	Component Total % of Variance		Cumulative %	Total	% Variance	Cumulative %		
1 2.78 46.375		46.375	46.375	2.782	46.375	46.375		
2	2 1.5 25.022		71.396	1.501	25.022	71.396		
3	0.97	16.151	87.547					
4 0.54 8.976		96.524						
5	5 1.64 2.732		99.255					
6	0.05 0.745		100.000					

the associated factor loadings. Of particular note is the positive correlation between Factor 1 and tin. This is to say that as the Factor 1 score of an artifact increases, i.e. an artifacts standing on a factor goes up, the amount of tin will also increase. Furthermore, aluminum, lead and silicon have a strong association with the first factor.

Gallium is a major characteristic of Factor 2 and positively correlates with that factor. Gallium has a very high loading value and is a distinctive characteristic of Factor 2. A positive correlation also exists between Factor 2 and lead. Furthermore, Factor 2 is negatively correlated with tin. Those artifact glazes that have a high Factor 2 score will have greater intensities of gallium and lead though feature much less tin in their compositions resulting in a clear finish rather than an opaque one.

## **Developing a Model for Predicting Staffordshire or London Provenance**

In light of this information regarding the notable variables for Factor 1 and Factor 2, it is now possible to use the factor scores to develop a binary logistic regression model that utilizes the London and Staffordshire provenance designations as the dependent variable. Not taking into consideration any other information, the regression analysis assumed the model would correctly predict the provenance by chance alone 56.2% of the time. When including the factor scores in the model the chi-square test ( $\alpha$ =.05) of the null hypothesis shows p value=.000 indicating that the model can make some distinction between Staffordshire and London materials as a result of the inclusion of the factor scores in the analysis. However, when looking at the Cox & Snell R Square value it is low showing that only 23.2% of the variability of the data is being explained. In this instance, the model correctly predicted to be from London and 82.9% of Staffordshire samples correctly predicted to come from Staffordshire (Table 4.11).

Classification							
London Staffordshire % Corr							
London	24	8	75				
Staffordshire	7	34	82.9				
Overall			79.5				

Table 4.11 Logistic regression Model 1 showing the number of correctly predicted samples using factor scores.

Only the Factor 2 scores of the chemical variables that constitute the second factor contribute to the predictive ability of the model, as seen in Table 4.12.

In an effort to improve upon this model, I re-ran the logistic regression analysis with the variables in the previous model as well as the addition of the estimated year of production. In this case the Cox & Snell R Square value improves significantly which

Variables in the Equation								
	B S.E. Wald df Sig. Exp(B)							
Factor 1	-0.148	0.263	0.316	1	0.574	0.863		
Factor 2	1.322	0.381	12.033	1	0.001	3.751		
Constant	Constant 0.295 0.271 1.189 1 0.276 1.344							

 

 Table 4.12 Details of significant variables that contribute to the predictive ability of Model 1.

now indicates that 50.1% of the variability in the data is now being explained. The

overall percentage of correctly predicted samples also increases to 87.7% with 84.4% of

London samples correctly attributed to London and 90.2% of Staffordshire materials

correctly predicted as coming from Staffordshire (Table 4.13). Factors 1 and 2 as well the

 Table 4.13 Logistic regression Model 2 showing the number

 of correctly predicted samples using factor scores and year of production.

Classification							
London Staffordshire % Co							
London	27	5	84.4				
Staffordshire	4	37	90.2				
Overall			87.7				

estimated year of production are significant and therefore are contributors to the ability of the model to make an accurate prediction of provenance. Table 4.14 details this

All variables are significant contributors.								
Variables in the Equation								
	B S.E. Wald df Sig. Exp(B)							
Factor 1	-1.755	8.717	8.717	1	0.003	0.173		
Factor 2	0.807	3.665	3.665	1	0.056	2.242		
Est. Year	0.043	0.011	15.035	1	0.000	1.044		
Constant	-74.219	19.234	14.889	1	0.000	0.000		

 Table 4.14 Details of significant variables that contribute to the predictive ability of Model 2.

 All variables are significant contributors.

information. The results of this exploratory analysis into making provenance attributions based on the constituent chemical fingerprints of these ceramics can now be considered in the light of historical trends in the British pottery industry to gain a better understanding of why particular glaze constituents aid in distinguishing between groups.

## Chapter 5: The Evolution of the Pottery Industry in the Eighteenth and Nineteenth Centuries

It is of interest to examine the historical context of ceramic production and consumption in England to gain a deeper understanding of the results of this study. As a corollary to this, further consideration should be paid to the reasons behind the improved results when I removed the lead and tin-opacified glaze colorants from the principle component analysis, ANOVA, Tukey post-hoc tests, and the regression models. Because of the notable difference between pottery groups, particularly the distinction between Staffordshire and London artifacts, it is useful to consider industrial pottery practice in England during the eighteenth and nineteenth centuries. During this time, changes wrought by the Industrial Revolution led to alterations in pottery fabric and glazes and led to the large scale commodification of decorative ceramics.

Changing ceramic markets necessitated a higher degree of production resulting in a pervasiveness of ceramic objects during the eighteenth and nineteenth centuries. These changes go a long way toward explaining many of the observed patterns and differences in the data. Standardization of glaze processes led to regional commonalities, but technological change in pottery and glaze production resulted in national distinctions. From a disciplinary perspective these results strengthen the justification for a refined archaeological toolkit and utilizing chemical analysis to aid in sorting through these materials, in particular taking advantage of the beneficial features of the portable X-ray fluorescence instrument.

## **English Ceramic Economy in the Eighteenth and Nineteenth Centuries**

The eighteenth century marked a period of industrialization and expansion of population and wealth in England. Entrepreneurs began investing in the development of technologies to facilitate the extraction of raw materials and the creation of finished products of greater variety in order to satisfy a growing national and global market place. Very early in this period, the production of pottery was one industry among many that was influenced by these forces, though maintained a fascination with exotic goods and stylistic elements. In the early decades of the 1700s, many pottery manufacturers tried developing imitations of Chinese, Japanese, and Mediterranean designs that often featured fine porcelain fabrics and delicate aesthetic qualities that caught the eye of many consumers (Hume 2001). However, organizations attempting to encourage domestic developments in the sciences and arts such as the Royal Society of Arts, founded in 1754, advocated for a movement away from the imitation and importation of these Eastern and Mediterranean ceramic traditions toward innovative English-made styles (Berg 2002).

London based potteries at Southwark and Lambeth were producing tin-glazed wares that attempted to approximate the appearance of overseas porcelain and later production expanded to a large degree particularly in Liverpool (Ostermann 2006). Not only were these potters conducting experiments on ceramic technologies and processes of manufacture, but new styles were emerging as well. Rosemary Troy Krill (2010, 135) noted that "some obvious evidences of development include sgraffito-decorated earthenware, influenced by an ethnic tradition; various white-bodied tea and dinner wares, affected by cross-cultural influences and social practices; and the diversity of transfer-printed wares, stimulated by the desire to expand ceramic markets." Because of

the advancements made by these individuals, a flowering of styles and forms flooded into the marketplace to meet the demands and tastes of a rising middle and upper class.

Pottery production during this period of English ceramic reflects shifts in societal and consumer aesthetics and cultural and cross-cultural influences that resulted in the production of new artifact forms. In tandem with new domestic scientific and technological developments, by the late 1700s "the number of forms had been extended to include a variety of objects for the home such as rectangular flower-holders, pen-andink stands, puzzle jugs, and a full complement of tea-drinking items..." (Cooper 2000, 155). A number of factors converged in the 1700s in England that altered the ways in which people were able to purchase goods and maintain and present themselves within society. Agricultural difficulties, population shifts, and the development of factories and mass production all served to alter the landscape of Britain (Mokyr 1985). A growing urban middle class was on the rise bolstered by a strengthened entrepreneurial spirit and characterized by a strong desire to express themselves to other members of their socioeconomic rank by purchasing decorative additions to display in their homes and on their dress (Berg 2007). Bermingham and Brewer (2013, 13) explained that "of the character models available to the late eighteenth century it was the ideal of the 'bohemian' or 'romantic' that most predisposed its types to consume. The romantic creed of self-expression, Campbell believes, aligned easily with consumption's promise of hedonistic self-gratification" (citing Campbell 1987).

While the ceramic market, and the market for other luxury goods fluctuated throughout the first decades of the 1700s, by the end of the eighteenth century the marketplace had evolved to meet the tastes and demands of the middle class consumer,

whose home was "rich in material goods which signified much about the social and cultural values of its occupiers..." (Richards 1999, 71). According to Dean et al. (2004) among households in Kent the percentage of those that owned plates increased from 14% in the early 1600s to 85% by the early eighteenth century, and in Cornwall this number went from 4% to 85%. The authors note similar increases among many other ceramic consumer goods in those same areas indicating changing tastes and greater affordability (Dean et al. 2004).

The eighteenth and nineteenth centuries marked an evolution of the consumer who was now able to obtain desirable goods for display as well as engage in leisure activities that gave individuals the opportunity to demonstrate their social rank through such a display (Bermingham and Brewer 2013). These sorts of engagements were certainly a product of the time which was characterized by shifting social, cultural, and economic circumstances. This new population of consumers exhibited a growing degree of extravagance and excess reflected in conspicuous consumptive behavior. Such behavior may have been an expression of identity, or to distinguish oneself among a growing population of similarly well-to-do people. During this time elements of Georgian high style had an important influence on the goods being sought, and with each passing decade the means were being put in place to meet the whims of the buyers.

## **Standardization and Rethinking the Ceramic Production Process**

In order to meet the demands of a rising mass market, the English ceramic industry experimented with new forms of factory organization. Writing in the nineteenth century, Simon Shaw (1900[1829]) noted that by the middle of the eighteenth century the

organization of workers in Staffordshire pottery factories changed significantly and was one factor that facilitated increased production. According to Shaw:

The increase of workmen, the subdivision of labour in every process; and the dexterity and quickness consequent on separate persons confining themselves solely to one branch of the Art, with the time saved in the change of implements and articles, instead of retarding, greatly promoted the manufacture, by increasing its excellence and elegance (166).

Given this reorganization that separated workers into particular activity areas of the overall manufacturing process, it is assumed that those engaged in the glazing process would follow the dictates of the master. This individual would have extensive knowledge regarding the necessary proportions of glaze constituents most appropriate to achieve a desired appearance, and this knowledge would be passed down to their apprentice(s).

Apart from the re-organization of workers to increase productivity, it is also the case that the production process itself, i.e., the operational sequence of making ceramic items, was becoming increasingly standardized. Jessica Hale (2008) offers a condensed list of seven production tasks that are described by Malcom Graham (2000, 13[1908]), a Staffordshire Vicar who published a photo-essay of nineteenth century earthenware production. Hale's list includes clay preparation, shaping, biscuit firing, application of glaze, glost firing, application of decoration, and a final firing. The glazing process can be further subdivided, as described by Owen (1901), beginning with the dipping of wares into a glaze bath, a subsequent inspection by the ware-cleaner, and a firing in the glost oven. During each firing, saggers were used to protect the wares in both early wood-fired kilns and subsequent larger coal-fired bottle kilns (Burton 1902). The application of colorants by blowing, painting, or dusting happened subsequent to the glost firing. After the addition of color and decoration the wares were placed in the kilns for the final firing.

Despite this newly specialized workforce that engaged in the glazing process, these craftsmen were becoming increasingly disconnected from the actual experimentation with and production of the glaze. This task was increasingly being taken over by chemists or other materials specialists. Goodfellow and Booth, for example, developed an improved fluid glaze and John Greatbatch is credited with the development of so-called China Glaze for Wedgwood that further refined Goodfellow and Booth's method (Miller 1987; Shaw 1900[1829]). Looking back over the course of the nineteenth century up to the time of publication of *A Potter's Book*, Bernard Leach (1976, 134) made note of the changes that resulted from this evolution of the English pottery craft and states "industrialization of pot making has involved such a heightened degree of standardization of material that it is now no longer the universal practice for potters to know their glaze materials and to make their own glazes." With such contextual information in mind it is now possible to make linkages between English pottery making history and the information derived from the pXRF chemical analysis.

#### Situating Glaze Chemistry in its Historical Context

Affordable material substitutes for porcelain were in growing demand by English consumers during the late eighteenth century. However, these ceramics featured a coarse earthenware fabric which necessitated the heavy use of tin glazing in order to produce a porcelain-like finish. Black (2001, 8) notes "it is impossible...to estimate how much tin-glazed earthenware was produced in the seventeenth and eighteenth centuries, but Peter Francis...estimates 44 million pieces between 1723 and 1781 from factories outside London alone (citing Francis 2000). The desire of consumers for improvements to fabric and glaze alike did not fall on deaf ears, however. Josiah Wedgwood, for example, was

beginning to utilize a growing body of scientific knowledge on the production of pottery. Glenn Adamson (2007) noted a paradigm shift in the eighteenth century from secretive alchemy to modern science in several realms, including pottery production, which was to the benefit of industrialists and entrepreneurs. Scientific experimentation allowed better precision and control over the constituent elements of the clay, the firing temperature and atmosphere, and the glaze. Eventually, this would result in a product to rival expensive, imported porcelains (Musson and Robinson 1969). As the nature and behavior of materials related to pottery production became public knowledge, it was possible to refine manufacturing techniques and apply that knowledge to industrial production (Adamson 2007).

With the development of cream-colored ware in the mid-1700s, the English, and in particular the Staffordshire ceramic industry saw a massive expansion and by the later decades of the eighteenth century "Josiah Wedgwood...achieved undisputed preeminence, and became the greatest agent in the world-wide distribution of the creamcoloured earthenware of North Staffordshire" (Miller 1980; Wedgwood 1913, 85). Originally using Dorsetshire ball clay with a mixture of other local clay, the Wedgwood recipe was altered with the discovery of kaolin deposits in Cornwall. The use of kaolin clays improved the fabric even more and allowed production of a much refined ware (Wedgwood 1913, 84). This development shook the British ceramic industry at this time as "the introduction and success of industrially manufactured cream-coloured wares in the second half of the eighteenth century led to a decline in the popularity of tin-glazed ware, and by around 1800 production of it had virtually ceased" (Bagdade and Bagdade 2004; Cooper 2000, 155).

Taking this into consideration, it is possible to look at the elements that best characterize the respective factors extracted through the factor analysis. Of greatest interest are the loading values of tin on Factors 1 and 2 of the Staffordshire and London stabilizers and fluxes. The fact that tin does not characterize Factors 2 to such a high degree relative to the tin value in Factor 1 seems to reflect the historic developments of glaze production in that region. Furthermore, tin is negatively correlated with Factor 2, but positively correlated with lead indicating that London and Staffordshire can be distinguished based on separate glaze production processes. Tin, as an opacifier, was no longer needed to produce a lustrous porcelain-like appearance in Staffordshire-made wares as they transitioned from the rougher local clays to the finer kaolinite material. However, Factor 1 is noteworthy for its greater loading value for tin and the associated higher intensity measures and factor scores for the London artifacts. As pointed out above, tin-glaze production was initiated among London based pottery shops and continued for many decades afterward before production experiences a sharp decline. Thus, the difference in tin is one of the most distinguishing characteristics of ceramic objects made in Staffordshire or London. Given the use of Cornwall kaolinite deposits by Staffordshire factories, it is also worthwhile to consider the presence of gallium in the second factor of the factor analysis which is linked to the Staffordshire glaze production strategy. Gallium is relatively uncommon; however, it is found in greater concentrations in association with aluminosilicate minerals, including those that constitute kaolinite, and is found during the extraction of alumina and zinc (Gray et al. 2000). Gray et al. (2000) states that:

The early stages of weathering of primary host rocks is characterized by leaching of alkalis, alkali-earths and silicon, consequently, gallium and aluminum may remained linked in secondary minerals, typically kaolinite and gibbsite, retaining in part the originally affinity in the lateritic cover (339).

While gallium may not be an intentional component of the glaze recipe, its presence hints

at the change in raw materials used by Wedgwood and the Staffordshire potters, namely

the use of kaolin clays. Coupled with the overall intensities of the other highly loaded

elements these materials can be sorted into their respective places of manufacture.

## **Chapter 6: Future Research Using pXRF to Study Glaze Chemistry**

As a result of this analysis a number of intriguing questions remain to be considered, in particular, future testing of the exploratory model that has been presented here. The principle component analysis focused the study to the major glaze constituents. Subsequent tests indicated compositional differences that encouraged further exploration. The factor analysis refined my understanding of the glaze chemistry which allowed for the characterization of the factors as London and Staffordshire glaze production strategies. Though the first of the two logistic regression models assigned the artifacts to the correct provenance or production area to a fair degree, the inclusion of the year of production allowed the model to achieve a greater level of statistical significance and improved the pseudo-R<sup>2</sup> values. Such results encourage the use of the pXRF as one tool for gaining a deeper understanding of the Chipstone collection as well as other ceramic assemblages. While this analysis could be reproduced, it would only be useful for drawing further conclusions about this collection, however, alterations to the research design and further testing is worthwhile.

To refine the model for predicting provenance it would be beneficial to use the pXRF instrument to scan not only more of the British artifacts in the Chipstone collection, but also branch out to other repositories of historic British and Continental European ceramics to see if a greater number of readings of materials will support the conclusions drawn from this initial model. It is necessary to determine a research strategy that eliminates the sampling bias issue inherent in this study (Speakman and Shackley 2013). One possible solution is to use collections of sherds and wasters in a blind study

and subsequently compare groups to known provenance information. In addition, Hunt and Speakman (2015) discuss the issues of measuring low Z elements and propose certain protocols for the analysis of ceramics and sediments as raw materials.

A new research design would begin by calibrating the existing dataset and the analysis would be re-run using parts per million values. Sherds in Chipstone's collection would be analyzed using pXRF and destructive analytical techniques to derive detailed compositional fingerprints of the glaze. A filter might be developed, in collaboration with Bruker, to target the specific constituents of lead glazes. Furthermore, a comparative study could be conducted using the ELIO Bruker analyzer that produces an XRF map of complex design surfaces. Should this line of research prove fruitful, the analysis could expand to sherds or whole vessels that do not yet have provenance information associated with them. This would further support the portable X-Ray Fluorescence instrument as a useful tool, both in the field and the lab, for sorting historic archaeological ceramics.

Apart from refining the model, developing greater knowledge about the raw materials used for the production of glaze and how those constituents interact with one another as well as confirming the link between raw material source and the pottery shop would be a productive avenue for research. On the one hand, it would reveal the nature of the kaolinite clay deposits that Staffordshire potters used in the late eighteenth century and determine if gallium and specific isotopes of other elements are present both in the those clay sources and in the glaze being made from those sources. It is an opportunity to assess the depositional effects on glaze chemistry by comparing the raw material chemistry to the fired artifacts. This may stretch beyond the abilities of the pXRF

instrument, though it would be interesting to utilize it as one tool among many for that research.

Such research would begin to fill in the entire commodity chain from raw materials to production and ultimately distribution into the mass market. This would give some insight into the spread of goods at every stage facilitated by the influences of the Industrial Revolution and the rise of consumerism. Tracing these goods chemically and archaeologically leads to multiple avenues to assess consumer choice as well as have knowledge of production. Archaeologists could reopen the issue of modeling consumer behavior discussed by Henry (1991), Klein (1991), Spencer-Wood (1987), and Wurst (1999). Furthermore, making basic national attributions to ceramic assemblages at archaeological sites based on the chemical fingerprinting of artifacts would be worthwhile given the strictures of mercantilism in the seventeenth and eighteenth centuries. Mercantilism lead to the expansion of trade routes, but restrictions on trade itself. Many European nations, including Britain, expanded their reach by establishing colonies and footholds across the world (Ormrod 2003). Materials were extracted and produced, but trade with foreign nations restricted (Ormrod 2003). Undertaking chemical analysis at a British colonial site and finding goods produced by a foreign nation may reveal occurrences of smuggling or deviations from established foreign relation policies. Such as research strategy could be expanded to other contexts including Roman and Mayan sites to reveal the exchange of goods, illicit or otherwise.

Furthermore, having that understanding of the raw and finished materials would help in potentially recreating the glaze recipes. This would entail not only an understanding of those raw sources, but also a careful chemical analysis of the glaze. A detailed reading of the historical record is also necessary that would provide insights into the specific ratios of constituents. This would likely involve a battery of tests and the use of a calibrated pXRF instrument as well as other techniques for gaining quantitative percentages of elements in the glaze.

Having an understanding of the glaze, coupled with the knowledge gained from the study of each stage of production, leads to interesting questions regarding technology transfer and the sharing of knowledge of practice. These transferences can be attained in a variety of ways including the traditional master and apprentice relationship. It might also be accomplished through industrial espionage or the movement of skilled workers to an alternate ceramic producing factory or region. Materials based research also provides an opportunity to assess the loss of diversity in glaze production strategies and recipes as that knowledge is concentrated into a smaller group of skilled glaze chemists and material scientists.

## Concluding Remarks on Glaze Analysis using Portable X-Ray Fluorescence

This exploratory foray into determining provenance based on the chemical compositions of British and Continental European lead and tin-opacified glazes is very much reliant on an understanding of the technical and methodological material science techniques, and in particular the nature of portable X-Ray fluorescence. This is coupled with a firm grounding in the historical literature that contextualizes the presence or absence of certain glaze elements. In this particular case, the trajectory of English made ceramics and the influence of industrialization on that process offer powerful insights into the patterns this study produced as a result of the principle component analysis, the subsequent factor analysis and the final logistic regression models.

The archaeologist or material culture analyst has an opportunity to utilize pXRF and other analytical tools to gain a better understanding of materials through the study of their underlying distinctions and similarities. These studies may provide new knowledge regarding the producers and the users of items manufactured from the materials studied. It should be stated outright that the portable X-Ray Fluorescence instrument cannot be considered a magic wand that will instantly generate conclusions regarding the archaeological record. A study such as this one must draw on a multitude of tools in the archaeological toolkit to achieve a holistic understanding of the material under study. Furthermore, generating that understanding is an iterative process whereby new information leads to a reexamination of the dataset, and seemingly anomalous results may force the researcher to alter the framework through which they view events in history.

Coupled with this, the importance of collaboration, drawing on the specialized knowledge of other researchers in various fields, and linking that knowledge together to craft an effect research design should be emphasized when approaching a study such as this one. This research is, on the one hand, situated well within the discipline of archaeology, but it also draws heavily on the material science of ceramics. There are elements of the industrial historical past and a solid understanding of the disciplinary history of archaeology regarding systematics and artifact classification. This study is ultimately operating from a processual-plus or historical-processual worldview. That is to say, that to understand the distinguishing and overlapping characteristics of these ceramics, which leads to effective classification schemes, it is necessary to utilize multiple perspectives and methods, explore the practices of the people who made them,
and have broader cultural and societal knowledge. This deeper understanding, in other words, "will be found only through the cumulative, painstaking, data-rich, multi-scalar studies of proximate causation" (Pauketat 2001, 87). As this study shows, people, technology, and society have an effect on glaze chemistry and ceramic production. Portable X-ray fluorescence offers a window into that broader story and can deepen our knowledge of archaeological materials and their chemistry. It is a tool for revealing the similarities or differences among an assemblage of ceramics. This information can factor into the formation of classification systems that will be useful in future archaeological research. Archaeometric approaches to material culture studies, broadly speaking, are one beneficial avenue of ceramic classification research as well offer the opportunity to bridge the divide between the natural and social sciences.

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# Appendix A: Chipstone Sample Log

			Chipstone S	Sample Log		
UWM Protocols						
15KeV/25µA	Full glaze area					
180 sec runs	3 areas/3 runs					
No filter	Kaolin Kga-2 Std					
Vacuum						
Volt regulator						
Sample #	Identifier	Origin	Est. Date	Item Type	Glaze Type	Scanned Areas
STD1	Kaolinite_Start_#	USGS				Sample Case
CS1	1993.3	London	1628-1650	Charger	White tin-glaze	Flat inner base
CS2	1991.13	London	1680-1710	Porringer	White tin-glaze	Flat inner base
CS3	1997.24	London	1650	Charger	Blue lead-glaze	Flat inner base
CS4	1990.6	London	1690-1720	Charger	Blue tin-glaze	Flat inner base
CS5	2011.7	Bristol	1700-1720	Charger	Blue tin-glaze	Flat inner base
STD2	Kaolinite_End_#	USGS				Sample Case
STD3	Kaolinite_Start2_#	USGS				Sample Case
CS6	2013.1	Portuguese	1670	Charger	Blue tin-glaze	Flat inner base
CS7	2000.58	England	1600	Charger	Blue tin-glaze	Flat inner base
CS8	2006.7	Italy	1620-1640	Charger	Tin-glaze	Flat inner base
CS9	1995.7	London	1660-1680	Hand warmer	White tin-glaze	Flat surface of books
CS10	1962.16(1)	London	1670-1685	Charger	Blue tin-glaze	Flat inner base
STD4	Kaolinite_End2_#	USGS				Sample Case
STD5	Kaolinite_Start3_#	USGS				Sample Case
CS11	1962.16(2)	London	1670-1685	Charger	Blue lead glaze	Flat base
CS12	1993.15	London	1628	Bottle	White tin-glaze	Body
CS13	1992.20	London	1650-1670	Posset pot	White tin-glaze	2 body/ 1 Lid
CS14	1992.21	London	1680	Posset pot	White tin-glaze	1 handle lid/2 body
CS15	2013.2	London	1660	Charger	Green lead-glaze	Front edge
CS16	1995.16	London	1681	Charger	Blue tin-glaze	Flat of area edge
CS17	1965.10	Staffordshire	1695	Owl jug	Lead-glaze	2 top head/ 1 body
CS18	2005.13	Massachusetts	1780-1820	Storage jar	Tin-glaze	1 Top lid/2 body
CS19	1969.11	Liverpool	1750-1770	Punch bowl	White tin-glaze	2 base/1 body
STD6	Kaolinite_End3_#	USGS				Sample Case
STD7	Kaolinite_Start4_#	USGS				Sample Case
CS20	1988.24	England	1670-1710	Charger	Lead glaze	Edge on front
CS21	1990.12	Staffordshire	1680-1720	Charger	Lead glaze	Flat inner base
CS22	1993.23	Staffordshire	1677	Charger	Lead glaze	Flat inner base
CS23	1993.16	Staffordshire	1715	Charger	Lead glaze	Flat edge on front
CS24	1998.3	Midlands?	1720-1740	Dish	Lead glaze	Flat inner base
CS25	1990.17	Kent	1722-1727	Tyg	Lead glaze	Rim
CS26	1970.4	Staffordshire	1670-1690	Charger	Lead glaze	Flat edge front
CS27	1989.12	Staffordshire	1650-1680	Charger	Lead glaze	Edge on front
CS28	1999.4	Staffordshire	1690	Charger	Lead glaze	Flat inner base
STD8	Kaolinite_End4_#	USGS				Sample Case
STD9	Kaolinite_Start5_#	USGS				Sample Case
CS29	1991.8	Staffordshire	1730	Charger	Lead glaze	Flat inner base
CS30	1967.13	Staffordshire	1695	Cup	Lead glaze	Body
CS31	1993.6	Staffordshire?	1733	Puzzle jug	Lead glaze	Body
CS32	1984.3	Midlands?	1731	Cup with cover	Lead glaze	Body
CS33	1994.3	Staffordshire	1710	Cup	Lead glaze	Body
STD10	Kaolinite_End5 #	USGS				Sample Case

The Chipstone sample log with details for each artifact used in the analysis.

The Chipstone sample log with details for each artifact up	used in the an	alysis continued.
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		Chipst	one Sample	Log (Continued)	1	1
STD11	Kaolinite_Start6_#	USGS				Sample Case
CS34	1963.15	Kent	1649	Tyg	Lead glaze	Body
STD12	Kaolinite_End6_#	USGS				Sample Case
STD13	Kaolinite_Start7_#	USGS				Sample Case
CS35	2009.10	Netherlands	1690-1710	Plate	Tin-glazed	Inner base
CS36	1965.11	Netherlands	1700-1799	Jar	Delftware	Body
CS37	1996.125	Netherlands?		Plate	Delftware	Flat inner base
CS38	1952.18	Unknown		Barber's Bowl		2 inner base/1 base
CS39	1964.10	Italy	1600	Plate	Majolica	2 inner base/1 from
CS40	1966.8	London	1725	Punch bowl	Blue tin-glaze	2 body/1 base
CS41	1960.6	France (Rouen)	1700	Bleeding bowl	Faience	Body
CS42	2000.44	Staffordshire	1700-1725	Fuddling cups	Lead-glaze	Body
CS43	2001.71	Bristol	1710-1730	Plate	Delftware	Flat inner base
CS44	2001.74	Bristol	1710-1730	Plate	Delftware	Flat inner base
CS45	2001.69	Bristol	1750	Plate	Delftware	Flat inner base
STD 14	Kaolinite_End7_#	USGS				Sample Case
STD15	Kaolinite_Start8_#	USGS				Sample Case
CS46	2009.9	Bristol	1760-1775	Plate	Delftware	2 inner base/1 base
CS47	2001.63	Staffordshire	1775-1785	Plate	Lead glaze	2 inner base/1 base
CS48	2000.32	Staffordshire	1775-1785	Plate	Lead glaze	2 inner base/1 base
CS49	2001.1	Staffordshire	1780-1790	Compote	Lead glaze	Flat inner base
CS50	2000.38	Staffordshire	1780	Loving Cup	Lead glaze	Body
CS51	2000.36	Staffordshire	1810	Tankard	Lead glaze	Outer base
STD16	Kaolinite End8 #	USGS				Sample Case
STD17	Kaolinite Start9 #	USGS				Sample Case
CS52	2000 33	Derbyshire	1774-1780	Plate	Lead glaze	2 inner base/1 base
CS53	2003 35	Carlton China	1915	Shin Figurine	Lead glaze	Body
CS54	2003.38	Carlton China	1914-1915	WWI Figurine	Lead glaze	Elat Back
CS55	2003.36	Shelley China	1917	Camel Figurine	Lead glaze	Body
CS56	2003.30	Victoria China	1917	Tank Figurine	Lead glaze	Body
CS57	2003.37	Grafton China	1914-1918	WWI Figurine	Lead glaze	Body
CS58	2005.57	Staffordshire	1800	Ing	Lead glaze	Body
CS50	2000.48	Staffordshire	1800 1840	Mini Ditahar	Lead glaze	Body
CS60	2000.15	Arcadian China	101/ 1018	WWI Figurine	Lead glaze	Body
C500	Vaolinita End0 #		1914-1918	w with guillie		Sampla Casa
STD10	Kaolinite_Eliu9_#	USUS				Sample Case
0061	2006.16	USUS Staffandahina	1000 1020	Mini Ditahan	Lood alara	Dadu
CS01	2006.16	Staffordshire	1800-1830	Transf	Lead glaze	Body
CS62	2000.49	Staffordahina	1/33-1//3	Teapot	Lead glaze	Dody
CS64	1990.18	Staffordshire	1745 1765	Teapot	Lead glaze	Dody
0304	19/8.0	Stafford-1	1/43-1/03	Leapot		Dody
0303	2012.17	Staffordshire	1/82-1/83	Loving Cup	Lead glaze	Dody
0867	2012.16	Stattordshire	1/82-1/85	Teapot	Lead glaze	Body
0867	2000.14	Stattordshire	1755	Tea Bowl/Saucer	Lead glaze	Bottom of Saucer
US68	2012.15	Stattordshire	1782-1785	Portrait Mug	Lead glaze	Body
SID20	Kaolinite_End10_#	USGS				Sample Case
STD21	Kaolinite_Start11_#	USGS				Sample Case
CS69	2000.52	Staffordshire	1755	Teapot	Salt glaze	Body
CS70	1966.23	Nevers, France	1700s	Jardiniere	Salt glaze	Body
CS71	1983.6	Staffordshire	1760	Coffeepot	Salt glaze	Body
CS72	2005.1	Staffordshire	1755-1760	Teapot	Salt glaze	Body
CS73	1992.16	London	1680	Jardiniere	Tin-glaze	Body
CS74	1968.2	London?	1705	Charger	White tin-glaze	Flat inner base
CS75	2001.25	Essex	1893	Charger	Lead glaze	Flat inner base
CS76	1968.8	London	1702-1714	Charger	Tin-glaze	Flat inner base
CS77	1967.15	London	1695	Charger	Tin-glaze	Flat inner base
OTDAA	Kaalinita End11 #	USGS				Sample Case

		Chipst	one Sample	e Log (Continued)		
STD23	Kaolinite_Start12_#	USGS				Sample Case
CS78	1963.28	Netherlands	1670-1700	Charger	White tin-glaze	Flat inner base
CS79	1961.13	Bristol	1727-1740	Charger	Blue tin-glaze	Flat inner base
CS80	1997.1(1)	London	1760	Sauce Boat	Tin-glaze	Body
CS81	1997.1(2)	London	1760	Sauce Boat	Tin-glaze	Body
CS82	2000.55	Staffordshire	1760	Sauce Boat	Tin-glaze	Body
CS83	2002.21	London	1740	Plate	Tin-glaze	Flat inner base
CS84	1964.31	London	1670-1700	Apothecary Jar	Tin-glaze	Body
CS85	1964.30	London	1670-1700	Apothecary Jar	Tin-glaze	Body
CS86	1967.18	London	1670-1700	Apothecary Jar	Tin-glaze	Body
CS87	1992.18	London	1700	Plate	Tin-glaze	Flat inner base
CS88	1964.29	London	1675-1700	Lozenge Jar	Tin-glaze	Body
STD24	Kaolinite_End12_#	USGS				Sample Case
STD25	Kaolinite_Start13_#	USGS				Sample Case
CS89	1989.10(1)	Staffordshire	1760	Fruit Basket/Stand	Green lead glaze	Flat inner base stand
CS90	1989.10(2)	Staffordshire	1760	Fruit Basket/Stand	Green lead glaze	Flat inner base stand
CS91	2008.1	Staffordshire	1770	Plate	Green lead glaze	Flat inner base
CS92	2001.51	Staffordshire	1790-1810	Dish	Green lead glaze	Flat base
CS93	1989.4(2)	London	1760	Wall Pockets	Delftware	Flat base
CS94	1989.4(1)	London	1760	Wall Pockets	Delftware	Flat base
STD26	Kaolinite_End13_#	USGS				Sample Case
STD27	Kaolinite_Start14_#	USGS				Sample Case
CS95	1995.4	Staffordshire	1775	Tumbler	Lead glaze	Body
CS96	1972.7	London	1669	Armorial Cup	Delft	Body
CS97	1991.7	London	1775-1785	Tankard	Delft	Body
CS98	1964.41	London	1765	Plate	Blue tin-glaze	Flat inner base
CS99	1999.16	Glasgow	1760	Plate	Tin-glaze	Flat inner base
CS100	1975.10	Bristol	1753	Armorial Cup	Blue delft	Body
CS101	1969.20	London	1676	Plate	Delft	Flat inner base
CS102	2000.66	London	1761	Plate	Delft	Flat inner base
STD28	Kaolinite_End14_#	USGS				Sample Case

### The Chipstone sample log with details for each artifact used in the analysis continued.

### **Appendix B: Selected Photos of Chipstone Samples**

Available images of artifacts used in the analysis taken from the Chipstone Foundation archives. See Appendix D for permission letter.









CS76 CS77 CS80 CS84 IVI CS85 CS86



adloc readnum AlK CoK CuK FeK GaK MnK NiK PbL SiK SnL TiK ZnK site estyear 1 1 1822 10807 1181 36518 5221 345 3698 384402 12204 5132 817 93 L 1640																																						
adloc readnum AlK CoK CuK FeK GaK MnK NiK PbL SiK SnL TiK ZnK site 1 1 1822 10807 1181 36518 5221 345 3698 384402 12204 5132 817 93 L	1640	1640	1640	1640	1640	1640	1640	1640	1640	1690	1690	1690	1690	1690	1690	1690	1690	1690	1650	1650	1650	1650	1650	1650	1650	1650	1650	1700	1700	1700	1700	1700	1700	1700	1700	1700	1710	1710
adloc readnum AlK CoK CuK FeK GaK MnK NiK PbL SiK SnL TiK ZnK 1 1 1822 10807 1181 36518 5221 345 3698 384402 12204 5132 817 93	-	_	-	_	_	_	_	_	-	_	_	_	_	_	_	_	_	_	-	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	в	8
adloc readnum AlK CoK CuK FeK GaK MnK NiK PbL SiK SnL TIK 1 1 1822 10807 1181 36518 5221 345 3698 384402 12204 5132 817	93	655	313	202	424	271	568	0	114	109	246	301	320	313	367	241	547	174	592	731	895	1196	940	1006	510	557	681	12236	12378	12755	17978	17893	17682	24377	24693	24730	687	850
adloc readnum AlK CoK CuK FeK GaK MnK NiK PbL SiK SnL 1 1 1822 10807 1181 36518 5221 345 3698 384402 12204 5132	817	681	667	631	865	639	589	608	709	662	376	269	190	391	594	557	440	453	685	703	728	856	1133	696	537	800	680	623	642	628	840	572	660	555	511	568	1634	1535
adloc readnum AlK CoK CuK FeK GaK MnK NiK PbL SiK 1 1 1822 10807 1181 36518 5221 345 3698 384402 12204	5132	2198	5032	5448	5061	4989	5723	6067	6026	15217	15501	15101	15664	15603	15503	12746	12782	12750	3146	3646	3020	3224	2862	3233	3441	3514	3359	7362	7194	7129	8032	8061	7967	8011	7839	7657	2538	2546
adloc readnum AlK CoK CuK FeK GaK MnK NiK PbL 1 1 1 122 10807 1181 36518 5221 345 3698 384402	12204	4976	10325	11616	8236	6943	9858	9092	10182	9093	9038	8747	8519	8353	8446	8156	8349	8239	8636	8623	10683	11731	11106	11113	7968	7631	7056	7129	7249	7195	8268	8242	8156	8098	7979	8092	10823	10260
adloc readnum AlK CoK CuK FeK GaK MnK NiK 1 1 1822 10807 1181 36518 5221 345 3698	384402	250931	346082	407512	418941	424291	416780	418137	418258	303047	306558	307072	313777	319290	319541	276014	278619	280465	412699	407360	409114	391987	390733	390385	419962	420233	426887	265034	267753	269322	309284	310008	312685	327721	330124	331107	408035	411935
adloc readnum AlK CoK CuK FeK GaK MnK 1 1 1822 10807 1181 36518 5221 345	3698	2930	2723	4869	6213	6572	4309	4388	4229	1949	2416	2026	1846	1832	2092	2172	1864	2005	1782	1593	1909	2255	3765	2754	2850	3180	4282	2041	2350	2579	2387	2170	2196	2586	2385	2210	1541	1788
adloc readnum AlK CoK CuK FeK GaK 1 1 1822 10807 1181 36518 5221	345	19	298	265	332	322	444	806	651	703	669	764	892	720	533	675	469	456	16810	23612	19509	37618	45169	37660	3561	3568	3673	1272	1524	1035	1091	1173	1386	1301	1032	1040	9474	9614
adloc readnum AlK CoK CuK FeK 1 1 1822 10807 1181 36518	5221	2866	4729	5498	5345	5234	5612	5291	5808	3946	4195	4199	4201	4186	4078	3495	3369	3399	6058	5924	6107	5552	5370	5317	5825	5719	5344	2148	2284	2272	2288	2640	2781	2425	2576	2540	6138	6055
adloc readnum Alk CoK CuK 1 1 1822 10807 1181	36518	20286	26742	41140	43885	44520	42784	42075	41772	19536	19861	19403	20329	20685	20272	17997	18086	18094	17348	19250	17579	19541	24181	21405	20661	22080	22842	27101	27075	27393	32768	32940	33073	34208	34142	34805	25237	24953
adloc readnum AlK CoK 1 1 1822 10807	1181	1210	1789	1369	1533	1254	1423	1505	1556	5073	5185	5178	5218	5496	5416	4747	4798	4688	4131	3463	3848	3492	3496	3753	4721	4765	4420	30807	30877	30603	49425	49917	49805	56181	55371	54905	4010	4660
adloc readnum AlK 1 1822	10807	6107	5297	14515	17568	19251	13747	13156	12913	534	534	360	382	411	431	680	375	465	729	1259	1075	3344	7262	4259	3793	5100	8128	1668	1697	1715	1711	1914	1921	1823	1590	1713	733	712
adloc readnum	1822	2355	2036	1865	1707	1542	1754	1759	1939	1985	2267	2142	2113	2147	2193	2144	2165	2241	1800	1725	1800	1786	1722	1778	1647	1741	1680	2206	2280	2199	2097	2068	1966	1771	2102	1864	1868	1788
adloc 1	1	2	Э	1	2	3	1	2	3	1	2	æ	1	2	Э	1	2	æ	1	2	3	1	2	°.	1	2	3	1	2	3	1	2	æ	1	2	Э	1	2
5	1	1	Ļ	2	2	2	33	3	3	1	7	1	2	2	2	3	33	3	1	1	7	2	2	2	Э	3	3	1	1	1	2	2	2	3	3	3	1	1
desig CS1	CS1	CS2	CS3	CS4	CS5	CS5																																
uniqueID CS1.1.1	CS1.1.1	CS1.1.2	CS1.1.3	CS1.2.1	CS1.2.2	CS1.2.3	CS1.3.1	CS1.3.2	CS1.3.3	CS2.1.1	CS2.1.2	CS2.1.3	CS2.2.1	CS2.2.2	CS2.2.3	CS2.3.1	CS2.3.2	CS2.3.3	CS3.1.1	CS3.1.2	CS3.1.3	CS3.2.1	CS3.2.2	CS3.2.3	CS3.3.1	CS3.3.2	CS3.3.3	CS4.1.1	CS4.1.2	CS4.1.3	CS4.2.1	CS4.2.2	CS4.2.3	CS4.3.1	CS4.3.2	CS4.3.3	CS5.1.1	CS5.1.2

# **Appendix C: Raw Net Intensity Data for Chipstone Materials**

1710	1710	1710	1710	1710	1710	1670	1670	1670	1670	1670	1670	1670	1670	1670	1630	1630	1630	1630	1630	1630	1630	1630	1630	1670	1670	1670	1670	1670	1670	1670	1670	1670	1670	1670	1670	1670	1670	1670	1670
в	в	в	в	в	в	٩	Ч	Ч	٩	٦	٦	Р	Р	٦	-	-	-	-	-	-	-	-	-	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_
2969	3092	2726	680	882	715	254	365	466	489	443	226	434	241	405	342	292	232	645	472	0	486	505	187	271	206	155	147	321	258	412	273	433	299	301	334	1025	966	749	117
1628	1445	1309	1268	1518	1197	1119	1227	1257	5481	5194	5265	6573	6744	6707	1647	1958	1636	1008	1084	1002	1552	1570	1427	697	489	676	569	450	464	382	468	518	169	577	429	401	333	346	474
2866	2647	2698	3355	3475	3384	1418	1511	1483	1956	2036	2047	1213	1224	1202	2909	2924	2973	2967	3032	3188	3804	3960	3893	14983	15083	14905	15521	15641	15578	16409	16134	16335	12128	12302	12449	14500	14414	14465	11628
8542	8753	8900	10018	10328	10301	1019	1075	1111	644	538	581	501	512	480	9226	9664	9912	10391	10254	10404	14936	14971	14868	6157	6376	6079	8265	8308	8493	9075	9036	9019	10569	10748	10464	6466	6391	6437	7929
388170	391472	393509	405094	407925	408278	375211	410517	409727	393301	392681	394625	336555	340075	341185	361581	367622	368035	380806	381630	382239	383356	384606	386918	383973	385741	386868	372494	372799	372970	377588	378892	380511	362252	363383	364401	317538	320329	320209	332680
7823	7585	8045	1361	1744	1604	6287	6686	7278	4545	5048	5174	2245	2403	2470	1531	1428	1504	1095	959	1172	1632	1397	1417	1091	1475	1552	1715	1455	1409	1419	1784	1625	1123	1614	1618	957	1133	1293	1820
672	567	255	406	554	659	2583	2690	2866	2128	2048	1924	22525	22349	22827	2247	2289	2036	1283	1312	1040	589	492	455	554	532	598	521	335	676	982	862	1025	433	450	495	475	501	469	706
4987	5034	5010	6122	5807	6386	4963	5789	5431	5118	5523	5034	4446	4488	4529	5071	5005	4792	5287	5587	4880	5603	5823	5374	5167	5221	5311	5010	4812	4964	4944	5175	5320	4604	4772	4889	3721	3962	3829	4332
27246	27455	27502	30352	30364	30004	35754	38462	38735	32212	32422	32310	19698	20567	20321	34213	33658	34416	35897	36562	36318	27855	27928	27852	25070	24615	24870	24764	25011	25301	25039	25299	25353	24146	24092	23691	25762	25590	26052	20979
2338	2289	2441	4095	4483	4232	590	991	715	808	658	069	1529	986	1286	52933	54059	53985	75530	75144	76360	3680	3711	3811	3658	4009	4090	3398	3110	3425	3448	3237	3659	46679	46078	45939	152414	152239	152501	6639
12943	12627	12977	893	1025	883	22320	24139	24315	16526	16369	16638	1838	2136	1967	631	572	503	701	646	691	645	761	507	569	637	769	476	570	1034	1258	1457	1760	882	1025	992	392	514	679	593
1936	1874	1757	1895	1828	1850	1481	1706	1630	1775	1666	1779	1886	1977	1894	2052	2051	2066	1983	1871	2055	2357	2327	2431	1709	1741	1830	1930	1865	1958	1860	1895	1852	1964	1891	1848	1762	1750	1773	1956
1	2	3	1	2	æ	1	2	æ	1	2	3	1	2	3	1	2	Э	1	2	æ	1	2	3	1	2	Э	1	2	33	1	2	æ	1	2	33	1	2	3	1
2	2	2	Э	3	ю	1	-	-	2	2	2	3	ю	e	1	1	1	2	2	2	œ	Э	3	1	1	1	2	2	2	S	e	ю	1	1	1	2	2	2	e
CS5	CS5	CS5	CS5	CS5	CS5	CS6	CS8	CS9	CS 10	CS 10	CS10	CS10	CS10	CS 10	CS10																								
CS5.2.1	CS5.2.2	CS5.2.3	CS5.3.1	CS5.3.2	CS5.3.3	CS6.1.1	CS6.1.2	CS6.1.3	CS6.2.1	CS6.2.2	CS6.2.3	CS6.3.1	CS6.3.2	CS6.3.3	CS8.1.1	CS8.1.2	CS8.1.3	CS8.2.1	CS8.2.2	CS8.2.3	CS8.3.1	CS8.3.2	CS8.3.3	CS9.1.1	CS9.1.2	CS9.1.3	CS9.2.1	CS9.2.2	CS9.2.3	CS9.3.1	CS9.3.2	CS9.3.3	CS10.1.1	CS10.1.2	CS10.1.3	CS10.2.1	CS10.2.2	CS10.2.3	CS10.3.1

1670	1670	1670	1670	1670	1670	1670	1670	1670	1670	1670	1628	1628	1628	1628	1628	1628	1628	1628	1628	1660	1660	1660	1660	1660	1660	1660	1660	1660	1680	1680	1680	1680	1680	1680	1680	1680	1680	1660	1660
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276	159	300	496	286	11	0	293	444	454	393	249	59	114	86	351	162	103	75	335	454	341	326	205	232	428	392	173	235	269	344	428	2673	2821	2728	690	609	587	2663	2828
440	493	722	601	610	571	467	444	475	334	600	471	383	495	442	538	669	523	429	435	341	347	484	396	328	289	471	630	437	471	567	477	645	802	671	459	444	498	760	707
11728	11672	4932	4644	4869	5573	5498	5328	4532	441	4511	9553	9710	9601	12121	12135	11923	10135	6767	10298	18334	18223	18197	16562	16488	16810	15382	15477	15428	9638	9807	9375	9823	9987	9894	8397	8711	8780	3339	3518
7929	7755	5967	6174	6006	7296	7308	7616	7756	7769	7599	16909	16689	17057	19666	19947	19901	7428	7356	7531	7552	7231	7287	9423	9722	9579	11056	11277	11031	15677	15528	15476	13057	13139	12967	6482	6596	6355	8459	8240
335440	335509	438620	439177	440993	438090	441011	440615	422981	424414	426411	393602	393987	395093	382474	383773	383981	393733	397274	396290	384985	386921	388298	380709	384837	383737	363527	368090	368646	369684	371876	372043	382946	386845	385786	392769	394321	395792	395745	398638
2099	1927	1892	1513	1430	1510	1544	1654	1557	1673	1476	9678	9961	9813	4911	4793	4510	10811	10840	10350	1378	1400	1342	1140	1011	1300	1605	1658	1615	18691	18490	18710	1413	1649	1535	1387	1461	1286	1168	1334
663	286	190	715	610	308	299	369	137	274	110	394	328	260	407	216	222	666	403	294	613	547	336	266	577	501	519	529	242	24702	25157	24541	1328	1712	1862	354	404	529	519	541
4461	4256	6374	6623	6324	6637	6497	6893	6407	6122	6243	5062	5009	4927	5135	5464	5224	4625	4801	4916	5317	5147	5204	5649	5234	5446	5141	5428	5115	4692	4909	4551	5076	5137	5268	5076	5017	5333	4687	4698
21593	20925	31958	32319	32192	29256	29434	29775	29452	29788	29468	44964	45280	44923	33249	33414	33129	36523	36849	36463	23558	23312	22885	23217	23379	22900	23817	23825	23668	40755	40864	40765	25174	25004	24901	26776	26579	26399	29389	29874
6508	6605	4842	4702	4617	5269	5198	5628	5057	5561	4768	1251	1014	1132	1482	1293	1238	1021	1135	930	2644	2837	2194	2340	2334	2240	2402	2577	2601	1711	1937	1997	3258	3695	3162	35684	35361	35392	84035	83272
942	368	1009	1055	874	795	1187	819	716	621	999	19154	19174	19398	8862	8719	8571	21031	21010	21206	604	701	539	735	643	801	481	802	718	18498	18948	18931	861	1039	919	884	620	552	1353	1967
1916	1949	1309	1471	1304	1427	1362	1481	1389	1403	1468	1664	1829	1866	2232	2267	2263	1585	1519	1574	1781	1560	1772	1530	1673	1611	1745	1834	1677	1856	1854	1953	1951	1987	1775	1642	1609	1671	1686	1568
2	3	1	2	33	7	2	33	7	2	Э	-	2	æ	-	2	æ	Ч	2	3	H	2	ю	7	2	Э	1	2	e	1	2	33	Ч	2	c	1	2	ŝ	1	2
e	æ	1	1	1	2	2	2	æ	£	£	7	1	1	2	2	2	£	£	3	7	1	1	2	2	2	3	ŝ	e	1	1	1	2	2	2	ŝ	ŝ	ŝ	1	1
CS10	CS10	CS11	CS12	CS13	CS13	CS13	CS13	CS13	CS13	CS13	CS13	CS13	CS14	CS15	CS15																								
CS10.3.2	CS10.3.3	CS11.1.1	CS11.1.2	CS11.1.3	CS11.2.1	CS11.2.2	CS11.2.3	CS11.3.1	CS11.3.2	CS11.3.3	CS12.1.1	CS12.1.2	CS12.1.3	CS12.2.1	CS12.2.2	CS12.2.3	CS12.3.1	CS12.3.2	o CS12.3.3	<b>J</b> CS13.1.1	CS13.1.2	CS13.1.3	CS13.2.1	CS13.2.2	CS13.2.3	CS13.3.1	CS13.3.2	CS13.3.3	CS14.1.1	CS14.1.2	CS14.1.3	CS14.2.1	CS14.2.2	CS14.2.3	CS14.3.1	CS14.3.2	CS14.3.3	CS15.1.1	CS15.1.2

1660	1660	1660	1660	1660	1660	1660	1681	1681	1681	1681	1681	1681	1681	1681	1681	1695	1695	1695	1695	1695	1695	1695	1695	1695	1690	1690	1690	1690	1690	1690	1690	1690	1690	1677	1677	1677	1677	1677	1677
_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	S	S	S	S	S	s	s	S	S	S	S	s	s	S	S	S	S	S	s	s	s	s	s	S
2742	2315	2021	1933	373	407	457	3333	3491	3703	3957	3761	3416	4100	3254	3425	467	749	441	869	650	779	1106	1055	1008	2330	2640	2554	2978	2661	2735	2796	2811	2251	676	640	915	647	751	389
635	714	736	550	729	732	700	470	422	625	620	355	776	691	452	632	5815	5478	5744	4234	4161	4221	3718	3640	3523	3890	3569	3608	4477	4265	4315	4018	4225	4147	5550	5496	5212	4471	4577	4498
3278	3374	3503	3514	2709	2725	2656	7499	7515	7686	3744	3431	3339	5402	5322	5507	283	316	365	99	182	67	91	84	148	316	246	190	403	492	400	342	334	421	299	224	235	242	341	201
8400	6524	6646	6698	7476	7549	7422	9843	9682	9775	8041	8097	8254	9956	9889	9831	7552	7670	7462	5382	5132	5231	4750	4778	4784	5112	5038	4906	5528	5806	5918	5176	5283	5397	7513	7531	7581	5810	5677	5480
399255	403049	405352	406276	431124	434984	433767	384052	388423	388229	377136	378834	377940	394573	395703	396437	432979	434878	434356	448921	452044	453966	445881	452062	452872	452190	456811	458651	418593	420883	421790	452284	454938	456442	458149	459297	460387	446347	449730	449373
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366	437	711	699	657	401	720	2728	2272	2001	4113	4301	3774	3629	3339	3724	538	239	361	61	154	7	295	501	305	360	368	90	707	821	569	323	564	234	167	408	369	180	377	158
4686	4937	5089	4861	6377	5758	6079	4026	4299	4105	3321	3425	3771	4069	3675	3801	6884	6798	6860	6828	7249	6672	6899	6591	6769	6498	6646	6908	6254	6060	6124	6595	6794	6727	6837	7022	7335	7018	6982	6883
29546	27517	27554	27445	28437	28097	28407	40316	40944	40583	62473	62275	61500	51885	52169	52200	34184	34177	33682	32188	31730	32001	46106	46451	46428	22537	22773	22389	31414	30990	31469	27050	27198	27228	28236	27563	27721	26360	26207	25974
83076	69712	86069	68879	8238	8279	8443	13444	12952	12997	6170	5899	5973	10156	10283	9697	1434	1274	1291	1621	1642	1165	1480	1297	1343	1336	1717	1366	1568	1321	1023	1446	1980	1489	2006	1931	2092	1826	1559	1332
1446	2036	1811	1912	6325	6495	6478	15561	15985	15392	40869	39974	39727	28115	27845	27731	1179	811	853	809	781	720	1019	975	1141	540	655	416	676	690	816	558	814	678	617	978	643	644	069	687
1717	1577	1540	1473	1538	1541	1408	1533	1793	1572	1483	1615	1590	1644	1640	1658	2267	1936	2140	1910	1854	2160	1645	1806	1962	1882	1736	1761	2075	1956	1962	1905	1806	1732	2148	2137	2095	2094	2075	1933
e	1	2	Э	4	2	e	1	2	3	1	2	3	1	2	e	H	2	e	H	2	Э	H	2	e	1	2	œ	1	2	3	1	2	3	1	2	e	1	2	Э
-	2	2	2	æ	œ	æ	1	1	1	2	2	2	33	33	e	H	Ч	Ч	2	2	2	æ	œ	œ	1	1	1	2	2	2	e	33	3	1	1	1	2	2	2
CS15	CS16	CS17	CS17	CS17	CS17	CS17	CS17	CS17	CS17	CS17	CS21	CS22	CS22	CS22	CS22	CS22	CS22																						
CS15.1.3	CS15.2.1	CS15.2.2	CS15.2.3	CS15.3.1	CS15.3.2	CS15.3.3	CS16.1.1	CS16.1.2	CS16.1.3	CS16.2.1	CS16.2.2	CS16.2.3	CS16.3.1	CS16.3.2	CS16.3.3	CS17.1.1	CS17.1.2	CS17.1.3	o CS17.2.1	CS17.2.2	CS17.2.3	CS17.3.1	CS17.3.2	CS17.3.3	CS21.1.1	CS21.1.2	CS21.1.3	CS21.2.1	CS21.2.2	CS21.2.3	CS21.3.1	CS21.3.2	CS21.3.3	CS22.1.1	CS22.1.2	CS22.1.3	CS22.2.1	CS22.2.2	CS22.2.3

1677	1677	1677	1715	1715	1715	1715	1715	1715	1715	1715	1715	1680	1680	1680	1680	1680	1680	1680	1680	1680	1665	1665	1665	1665	1665	1665	1665	1665	1665	1690	1690	1690	1690	1690	1690	1690	1690	1690	1730
S	S	S	S	S	S	S	S	S	s	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	s	s	S	S	S	S	S	s	s	S	S	S	S
896	860	1341	1677	1855	1846	1070	964	926	1697	1328	1719	1512	1658	1310	1669	2001	2134	2019	1613	2021	7701	7677	7010	9809	9833	9579	8055	8233	8631	7841	7895	7609	5266	5401	5476	5873	5496	5686	11200
4748	4768	4700	5043	5015	5347	5500	5263	5102	8110	7764	7716	3826	3876	3954	4165	3978	3972	4072	4076	4107	3198	3254	3349	3373	3443	3340	2819	2834	2816	4905	4879	5176	3786	3657	3805	4792	4344	4492	5773
255	224	244	340	356	293	329	272	410	322	369	395	412	386	287	222	360	261	314	312	349	233	146	156	189	154	213	300	241	151	223	250	304	196	210	194	255	272	216	138
5607	5347	5560	8378	8464	8245	8582	8646	8653	8024	8271	8226	5270	5195	5072	6438	6399	6181	5782	5688	5776	4472	4622	4500	5470	4158	3991	4271	4213	4384	4885	4646	4716	4976	5063	4949	5045	5022	5163	5531
434157	435906	437400	429574	430742	431703	434582	436185	436960	389695	390847	393131	414252	418239	420235	429230	431622	433490	413685	416958	416424	439904	441284	443357	448992	452645	454042	430500	434138	434133	411862	413093	414738	454286	458099	457048	416020	418461	420737	434464
1379	1477	1778	1223	1089	1396	1477	1386	1374	1201	1383	1472	1328	1132	1079	1198	1095	980	1206	923	1091	1321	944	1101	1428	1027	1521	1234	1296	1172	1331	1704	1597	1554	1495	1547	1564	1389	1702	1458
629	444	359	514	224	182	212	415	132	564	560	286	454	148	238	317	252	574	681	629	406	355	361	470	388	385	433	1524	1398	1536	417	557	855	572	225	556	378	299	572	201
6760	6944	6594	6430	6421	6099	6458	6747	6588	5852	5807	5779	6543	6521	6706	6185	6899	6325	5985	6085	6136	6191	6600	6248	6553	6472	6340	5939	5869	6105	6322	6056	6108	6870	6224	6747	6433	6044	6456	6139
28972	29528	29212	55660	54537	54384	34901	34401	34717	50242	50044	49588	59796	59133	58925	71247	70925	66582	72966	72769	73276	50559	50227	50984	38748	41911	42160	48902	48953	49022	27324	27866	27904	22282	22395	22167	25375	25212	25145	37313
1962	1751	2047	1508	1790	1465	1502	1819	1657	1541	1600	1978	1951	1699	1700	1704	1697	1763	1652	1893	1458	1594	1762	1512	1250	1848	1359	1459	1384	1669	1957	1780	1738	1841	2133	1998	2151	2111	2265	3068
598	762	960	1190	1011	1098	868	884	848	1036	1194	1057	1213	898	821	1170	1187	1120	1364	1460	1667	980	1059	943	777	965	752	1079	942	992	636	490	580	479	614	597	678	701	724	854
1924	1909	1989	2369	2294	2384	2388	2499	2519	2333	2296	2250	2046	2086	2011	2146	2165	2149	2091	2046	2053	1674	1775	1738	1937	1691	1628	1782	1846	1800	2171	2134	1941	2114	1828	1889	2000	1903	2169	1700
1	2	3	Ļ	2	3	Ļ	2	Э	۲	2	Э	1	2	e	L	2	æ	Ļ	2	æ	Ļ	2	33	1	2	3	1	2	3	1	2	Э	1	2	33	1	2	œ	Ļ
e	œ	3	1	1	1	2	2	2	ю	e	Э	1	1	Ļ	2	2	2	Э	e	e	1	1	1	2	2	2	ŝ	ŝ	3	1	1	1	2	2	2	33	ŝ	ŝ	1
CS22	CS22	CS22	CS23	CS26	CS26	CS27	CS28	CS29																															
CS22.3.1	CS22.3.2	CS22.3.3	CS23.1.1	CS23.1.2	CS23.1.3	CS23.2.1	CS23.2.2	CS23.2.3	CS23.3.1	CS23.3.2	CS23.3.3	CS26.1.1	CS26.1.2	CS26.1.3	CS26.2.1	CS26.2.2	CS26.2.3	CS26.3.1	5 CS26.3.2	CS26.3.3	CS27.1.1	CS27.1.2	CS27.1.3	CS27.2.1	CS27.2.2	CS27.2.3	CS27.3.1	CS27.3.2	CS27.3.3	CS28.1.1	CS28.1.2	CS28.1.3	CS28.2.1	CS28.2.2	CS28.2.3	CS28.3.1	CS28.3.2	CS28.3.3	CS29.1.1

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1730	1730	1730	1730	1730	1730	1730	1730	1695	1695	1695	1695	1695	1695	1695	1695	1695	1733	1733	1733	1733	1733	1733	1733	1733	1733	1710	1710	1710	1710	1710	1710	1710	1710	1710	1700	1700	1700	1700	1700
S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	s	s	S	S	S	S	s	s	S	S	S	S	S	S	z	z	z	z	z
503	1597	888	5290	858	3387	3384	3190	7624	7245	953	3757	<b>1517</b>	I856	571	320	822	797	018	120	374	905	746	455	240	732	258	261	068	854	495	629	2492	830	254	109	504	127	650	564
10	10	υ,	Ű	υ,	ω	~	~	27	27	27	33	37	34	20	21	20		~	~				~	~		~	~	~	-	-	~		-	(1					
5682	5988	6442	6501	6232	5065	5338	5200	6193	0609	5750	6587	6527	6763	0906	8531	8770	5441	5134	5114	5565	5800	5724	5747	5831	5894	5615	5533	5570	6257	6187	6247	6316	6311	6259	434	489	399	180	268
166	250	290	275	195	242	271	256	278	170	160	500	427	388	765	582	602	231	335	275	236	260	290	405	278	380	363	272	253	355	359	329	380	430	224	11971	11891	11931	15593	15675
4960	4803	4079	4067	4103	4884	4998	5260	3982	3999	4157	4362	4298	4243	4466	4634	4572	4928	4824	4839	4080	3798	3755	3779	3921	3734	4307	4148	4059	3508	3363	3370	3688	3713	3765	8566	8559	8491	9291	9318
436201	436101	458060	457904	460424	444053	444126	446558	438672	441791	442588	445065	448211	449552	437829	439237	438461	460621	462358	463027	467804	466909	468490	456475	460117	459096	461796	463431	465079	462356	462208	462541	468205	468242	470458	374978	378840	380320	370778	371926
232	250	051	106	353	406	074	498	940	079	943	173	123	279	316	321	323	192	988	908	253	381	212	010	1036	910	176	1067	084	248	239	368	249	123	191	308	616	284	270	206
	~	-	-	-	-	-			-			-	-			~							~	~		-	~	~	-	-	~		-	~	11	1	11	~	
546	613	217	205	97	449	129	586	590	589	732	786	864	883	1273	1209	1258	507	493	358	841	942	878	305	506	559	1003	1069	1070	818	566	754	967	556	721	774	752	939	643	962
6133	6425	6430	6792	6524	6925	6637	6296	6116	5770	6424	6026	5990	5893	6038	6351	6407	7155	6956	6930	7223	7065	7500	7158	6944	7537	7111	7250	7128	6808	7253	6862	7036	6771	7458	5354	5308	5395	5067	4857
37572	37484	51997	51755	51674	35561	35243	35377	58583	57543	57933	30533	29965	30350	37750	37684	38064	55489	55615	55436	37416	37676	37697	66071	65575	65135	50064	49241	49011	33874	33311	33261	36387	35700	36330	34450	34585	34620	19712	20215
3116	2971	2927	2827	3054	3122	2710	3180	1572	1923	1777	1696	1976	1637	910	1362	1328	1559	1887	1556	2045	1722	1946	1514	1705	1652	2132	1800	1557	1935	1586	2136	1697	1267	1472	2565	3075	2644	3691	3618
807	933	1043	916	1014	766	736	543	707	917	829	778	578	296	556	661	485	1083	1110	1089	772	663	762	1143	1092	1042	950	856	1095	697	510	565	685	661	750	18218	17821	18436	794	639
1618	1536	1382	1287	1260	1311	1467	1581	1430	1333	1284	1361	1297	1251	1229	1336	1405	1284	1273	1370	1362	1296	1381	1199	1403	1239	1366	1208	1307	1342	1302	1247	1187	1291	1255	1364	1291	1318	1404	1462
2	e	Ч	2	e	Ч	2	e	1	2	e	1	2	e	-	2	e	-	2	e	-	2	e	1	2	e	1	2	e	Ч	2	m	1	2	m	1	2	e	Η	2
Ч	1	2	2	2	3	С	С	1	1	1	2	2	2	С	З	С	H	Ч	H	2	2	2	e	3	С	1	1	1	2	2	2	œ	3	3	1	1	1	2	2
CS29	CS30	CS30	CS30	CS30	CS30	CS30	CS30	CS30	CS30	CS31	CS31	CS31	CS31	CS31	CS31	CS31	CS31	CS31	CS33	CS35	CS35	CS35	CS35	CS35															
CS29.1.2	CS29.1.3	CS29.2.1	CS29.2.2	CS29.2.3	CS29.3.1	CS29.3.2	CS29.3.3	CS30.1.1	CS30.1.2	CS30.1.3	CS30.2.1	CS30.2.2	CS30.2.3	CS30.3.1	CS30.3.2	CS30.3.3	CS31.1.1	CS31.1.2	5 CS31.1.3	CS31.2.1	CS31.2.2	CS31.2.3	CS31.3.1	CS31.3.2	CS31.3.3	CS33.1.1	CS33.1.2	CS33.1.3	CS33.2.1	CS33.2.2	CS33.2.3	CS33.3.1	CS33.3.2	CS33.3.3	CS35.1.1	CS35.1.2	CS35.1.3	CS35.2.1	CS35.2.2

1700	1700	1700	1700	1750	1750	1750	1750	1750	1750	1750	1750	1750	1750	1750	1750	1750	1750	1750	1750	1750	1750	1600	1600	1600	1600	1600	1600	1600	1600	1600	1725	1725	1725	1725	1725	1725	1725	1725	1725
z	z	z	z	z	z	z	z	z	z	z	z	z	z	z	z	z	z	z	z	z	z	-	-	-	-	-	-	-	-	-	_	_	_	_	_	_	_	_	_
781	597	925	1067	605	480	550	893	1208	1369	576	946	1055	51002	51736	51904	49048	48891	48999	31877	31482	31718	516	523	488	363	455	247	531	693	612	666	847	620	609	494	441	890	522	581
471	629	529	600	652	785	805	114	177	476	697	447	340	602	653	408	220	514	301	322	163	352	226	327	277	418	324	354	459	299	542	1626	1663	1807	1930	1685	1912	1900	1852	1831
15649	13840	13604	13658	3663	3633	3794	10888	10868	10856	9582	9096	9879	2639	2481	2611	2357	2238	2144	3720	3871	3917	11474	11339	11175	12132	12311	12225	12173	12218	12176	9098	9216	9071	7413	7669	7810	6322	6384	6525
9215	7919	7933	8052	7105	7054	7182	8573	8569	8536	8256	8610	8519	5655	5472	5487	5281	5299	5113	5932	6051	6052	7760	8121	7925	7585	7790	7834	7798	7698	7847	9279	9058	9005	10644	10672	10505	10381	10332	10263
371715	357844	358364	359055	428344	428898	429065	407376	408992	408661	412788	413388	415806	400725	404772	403490	398036	400155	401297	405786	408857	409811	394441	395040	396231	405311	408943	408481	403411	406133	407425	388627	389252	390887	403276	404963	405574	410510	411466	412706
1307	1920	1786	2118	7958	7965	7951	1811	1496	1778	2349	2195	2275	748	757	636	1413	1370	1647	1325	1368	1103	1437	1489	1312	1132	1276	1060	880	1294	1136	1086	1175	1590	1589	1350	1193	1481	1287	1523
1061	1450	1011	955	2101	2199	2349	508	547	420	472	538	481	327	314	529	85	69	181	171	184	281	322	675	510	315	429	602	413	233	411	726	515	809	820	724	745	475	868	717
5073	4538	5043	4780	6143	6092	6127	5748	5858	5589	5420	6057	5878	5613	5340	5611	5423	5545	5426	5655	5754	5852	5407	6187	6034	6234	6243	6132	5991	5973	5981	5344	5556	5694	5819	5799	5355	6002	5950	6058
20268	34408	34563	34886	22994	23371	23234	14342	14372	14396	13587	13474	13378	55106	55131	55512	73367	72354	73077	49723	48923	49338	20935	20672	20222	21083	21190	21012	22099	22298	21723	23402	23566	23289	22818	23084	22572	24588	24735	23977
4053	2603	2632	3027	2851	2798	3135	3597	3565	4139	3312	3675	3893	547	815	342	513	393	360	459	715	316	2588	2728	2200	2390	2640	2500	2138	2822	2441	9459	9394	9700	8003	7574	7311	7878	7839	8055
827	1813	1793	1762	11433	11096	11105	701	831	850	929	984	916	4763	4387	4589	6871	6932	6935	9835	9778	9704	507	508	515	529	316	587	670	769	731	943	477	618	459	785	568	552	674	499
1441	1478	1588	1511	1464	1259	1281	1389	1481	1536	1423	1483	1442	1176	1179	1281	1220	1248	1100	1188	1382	1218	1606	1646	1400	1319	1375	1315	1340	1408	1310	1595	1664	1546	1613	1661	1798	1725	1457	1572
3	1	2	3	1	2	3	1	2	3	1	2	3	1	2	С	Ч	2	3	H	2	Э	1	2	c	1	2	œ	1	2	3	1	2	3	1	2	3	1	2	æ
2	3	3	3	1	1	1	2	2	2	Э	3	3	7	1	Ļ	2	2	2	æ	æ	Э	1	1	1	2	2	2	33	ŝ	3	7	1	1	2	2	2	œ	c	Э
CS35	CS35	CS35	CS35	CS36	CS37	CS37	CS37	CS39	CS40																														
CS35.2.3	CS35.3.1	CS35.3.2	CS35.3.3	CS36.1.1	CS36.1.2	CS36.1.3	CS36.2.1	CS36.2.2	CS36.2.3	CS36.3.1	CS36.3.2	CS36.3.3	CS37.1.1	CS37.1.2	CS37.1.3	CS37.2.1	CS37.2.2	CS37.2.3	, CS37.3.1	CS37.3.2	CS37.3.3	CS39.1.1	CS39.1.2	CS39.1.3	CS39.2.1	CS39.2.2	CS39.2.3	CS39.3.1	CS39.3.2	CS39.3.3	CS40.1.1	CS40.1.2	CS40.1.3	CS40.2.1	CS40.2.2	CS40.2.3	CS40.3.1	CS40.3.2	CS40.3.3

1700	1700	1700	1700	1700	1700	1700	1700	1700	1710	1710	1710	1710	1710	1710	1710	1710	1710	1720	1720	1720	1720	1720	1720	1720	1720	1720	1720	1720	1720	1720	1720	1720	1720	1720	1720	1750	1750	1750	1750
FR	S	S	S	S	S	S	S	S	s	в	в	в	в	в	в	в	8	в	в	в	в	в	в	в	в	в	в	в	в	в	8								
1249	943	1222	902	836	722	665	459	604	3578	3972	3991	3099	3064	2819	3708	3640	4026	632	390	759	1096	763	829	1198	1062	1303	1049	1145	935	1425	1269	910	1207	1434	1463	835	1060	1173	1074
207	83	180	22	82	154	125	88	0	5049	4824	4912	4900	4690	4648	5486	5080	5280	1400	1720	1558	1781	1669	1769	1441	1521	1640	2077	1865	2081	1744	1739	1551	1560	1803	1807	827	890	973	992
15947	16217	16136	18133	18523	18443	18377	18299	18529	538	565	464	465	329	383	458	438	474	5076	4958	4912	4893	4525	4640	6665	6772	6766	3803	3708	3671	7420	7299	7263	4688	4815	4826	22452	22347	22805	22629
9074	8940	9088	8758	8818	8596	8440	8194	8287	6641	6719	6535	6993	6943	6817	6961	7134	6924	11058	11206	11253	11157	11019	11011	11088	11239	11319	9020	9343	9035	9260	9580	9252	10551	10729	10737	9494	9685	9631	9919
405467	409455	409404	405390	407999	408925	408526	411158	412503	391137	391509	393154	386487	388259	388436	390657	391417	390714	387716	393942	392762	393264	393183	394841	379593	381614	381897	421202	422167	422821	401463	402406	402968	403225	405900	406494	337678	338851	338440	340666
1276	1394	1304	1272	1064	1032	1062	1108	937	623	965	895	673	680	879	624	654	994	11521	11321	11162	1978	1752	1799	1766	1396	1766	1653	1513	1739	1547	1456	1806	1893	1724	1969	1702	1446	1562	1420
2894	2862	3069	121	313	41	43	102	103	125887	125738	125819	129969	129902	130118	130109	130028	130114	882	1361	746	784	839	704	730	837	646	702	676	365	599	412	734	570	825	543	819	809	661	889
5912	5939	5808	5414	5432	5641	5500	5510	5450	5542	5654	5503	5338	5517	5450	5384	5381	5370	5169	5273	5035	5333	5753	5961	5451	5473	5674	6238	5733	6061	5768	5803	5783	6208	6037	5990	4579	4263	4582	4517
11024	10802	10508	10485	10317	7666	10250	10297	10581	54436	55141	54020	52172	51788	52353	48996	49076	48974	32615	32502	32971	25745	25296	25397	25641	25506	25239	30947	31335	31636	29522	29813	29604	31121	31052	30604	23278	22981	23300	23407
6857	7105	6817	7132	7030	7103	8163	8264	8233	2211	2449	2496	2184	2029	2602	2285	1885	2298	3687	3772	3786	5058	4847	4622	5139	5046	5117	4359	4266	4620	4648	4211	4676	4473	4456	4298	5553	5827	6062	5834
10008	9891	10004	1309	915	823	1196	930	784	334	603	574	523	269	509	237	œ	789	11999	11710	11709	657	758	632	870	575	855	1325	1127	1242	1061	1365	1240	972	1072	1023	390	500	405	692
1569	1653	1411	1629	1494	1634	1633	1580	1604	1494	1405	1422	1355	1351	1458	1376	1577	1524	1672	1814	1645	1723	1876	1802	1695	1666	1689	1653	1664	1665	1597	1691	1647	1577	1634	1687	1559	1744	1648	1862
1	2	æ	1	2	S	1	2	ε	1	2	Э	1	2	ε	7	2	Э	1	2	ε	1	2	S	1	2	3	1	2	ŝ	1	2	ε	1	2	ŝ	1	2	c	1
1	1	1	2	2	2	S	Э	33	1	1	1	2	2	2	e	e	ю	1	-	-	2	2	2	33	e	3	1	1	1	2	2	2	33	33	33	1	1	1	2
CS41	CS42	CS43	CS43	CS43	CS43	CS43	CS43	CS43	CS43	CS43	CS44	CS45	CS45	CS45	CS45																								
CS41.1.1	CS41.1.2	CS41.1.3	CS41.2.1	CS41.2.2	CS41.2.3	CS41.3.1	CS41.3.2	CS41.3.3	CS42.1.1	CS42.1.2	CS42.1.3	CS42.2.1	CS42.2.2	CS42.2.3	CS42.3.1	CS42.3.2	CS42.3.3	CS43.1.1	CS43.1.2	L CS43.1.3	CS43.2.1	CS43.2.2	CS43.2.3	CS43.3.1	CS43.3.2	CS43.3.3	CS44.1.1	CS44.1.2	CS44.1.3	CS44.2.1	CS44.2.2	CS44.2.3	CS44.3.1	CS44.3.2	CS44.3.3	CS45.1.1	CS45.1.2	CS45.1.3	CS45.2.1

1750	1750	1750	1750	1750	1770	1770	1770	1770	1770	1770	1770	1770	1770	1770	1770	1770	1770	1770	1770	1770	1770	1770	1770	1770	1770	1770	1770	1770	1770	1770	1770	1785	1785	1785	1785	1785	1785	1785	1785
в	в	в	в	в	в	в	в	в	в	в	в	в	в	S	S	S	S	S	S	S	S	S	S	S	S	S	s	s	S	S	S	S	S	S	S	S	S	S	S
855	1233	1179	1182	986	535	681	196	414	416	477	461	432	509	240	429	- 1	264	- 1	243	141	263	228	290	76	353	381	321	587	540	383	401	345	448	418	559	305	441	538	389
931	874	1110	888	1290	58	143	430	235	345	357	251	253	0	3828	3670	3697	3767	3731	3788	3408	3450	3446	3405	3429	3507	3519	3309	3457	3489	3487	3334	1387	1183	1258	1201	1037	1337	922	992
22985	22473	22898	22973	23019	28651	28261	29146	28789	28586	28555	26431	26411	26405	999	615	694	796	737	680	410	561	599	154	160	163	210	147	136	129	62	38	1867	1898	1804	1870	1628	1921	1634	1875
9826	9668	10009	10192	10266	64954	64655	64685	65000	64536	65103	66257	65899	65763	55970	55967	55994	60108	60209	60358	54216	53715	54475	45111	45596	44897	46756	46713	46129	45389	45005	45130	65722	65683	65176	67575	67242	66756	67541	66822
342341	343150	340017	340459	341416	288967	290103	289560	291587	291589	292456	289290	290898	290961	359970	360414	360854	348259	349769	350814	359697	360822	362002	367931	368132	368489	365526	367751	366585	364365	365218	364835	355881	358168	359515	356734	357972	359395	359801	361450
1601	1599	1612	1545	1641	1686	2060	2104	1751	2018	1774	1739	1598	1676	1195	1365	1006	982	1130	922	773	833	1049	911	811	1032	992	869	1120	1105	1091	956	1159	1615	1462	1522	1292	1426	1552	1426
967	731	928	534	006	1074	809	945	1128	1176	1052	991	976	766	450	263	320	263	408	232	320	19	161	138	242	285	290	155	343	1	82	175	378	532	478	577	450	698	654	483
4306	5024	4484	4536	4582	6444	6144	6466	6233	6351	6327	6491	6513	6589	9233	9564	9211	9442	9392	9581	9181	9290	9213	9310	9131	9450	9620	9235	9273	9224	9210	9086	9253	9033	9218	9386	8926	9233	9192	8828
23321	23072	23336	23709	23446	22342	22432	22325	22156	22105	22497	22941	22775	22110	13148	13071	13454	15012	14590	14774	13451	13780	13819	9658	9679	9485	10479	10280	10725	10055	10105	9991	6688	6714	6758	6811	6798	6701	6794	7149
5674	5735	5651	5478	5461	4194	4210	4043	4144	4055	4261	3934	3708	3622	1793	2092	1847	1489	1566	1497	1741	2012	2094	2551	2242	2505	2439	2214	2217	2612	2354	2432	2103	1955	2245	2234	2115	2016	2187	2296
485	519	410	520	427	2175	2045	2174	2139	1912	2041	2312	2453	2218	664	734	1100	600	1040	794	724	765	711	389	681	408	740	406	725	721	635	518	1147	1203	1158	1268	1203	1081	1289	1344
1694	1872	1511	1824	1725	17629	17994	17809	17912	18193	17977	23113	23303	23219	25781	25667	25475	29905	29961	29453	26080	25887	25813	17977	18245	18430	19504	19203	18613	19992	19920	20080	28738	28836	28429	29609	29713	29227	25607	25278
2	œ	1	2	œ	1	2	С	Ļ	2	c	Ļ	2	£	۲	2	£	Ļ	2	c	Ļ	2	œ	Ļ	2	ю	1	2	œ	1	2	œ	Ļ	2	3	1	2	e	1	2
2	2	3	œ	3	1	1	1	2	2	2	œ	3	ε	1	1	7	2	2	2	e	3	æ	7	1	1	2	2	2	c.	S	e	1	7	1	2	2	2	œ	m
CS45	CS45	CS45	CS45	CS45	CS46	CS47	CS47	CS47	CS47	CS47	CS47	CS47	CS47	CS47	CS48	CS49																							
CS45.2.2	CS45.2.3	CS45.3.1	CS45.3.2	CS45.3.3	CS46.1.1	CS46.1.2	CS46.1.3	CS46.2.1	CS46.2.2	CS46.2.3	CS46.3.1	CS46.3.2	CS46.3.3	CS47.1.1	CS47.1.2	CS47.1.3	CS47.2.1	CS47.2.2	, CS47.2.3	CS47.3.1	CS47.3.2	CS47.3.3	CS48.1.1	CS48.1.2	CS48.1.3	CS48.2.1	CS48.2.2	CS48.2.3	CS48.3.1	CS48.3.2	CS48.3.3	CS49.1.1	CS49.1.2	CS49.1.3	CS49.2.1	CS49.2.2	CS49.2.3	CS49.3.1	CS49.3.2

1785	1780	1780	1780	1780	1780	1780	1780	1780	1780	1810	1810	1810	1810	1810	1810	1810	1810	1810	1915	1915	1915	1915	1915	1915	1915	1915	1915	1915	1915	1915	1915	1915	1915	1915	1915	1915	1917	1917	1917
S	S	S	S	S	S	S	S	S	S	S	s	S	S	S	S	S	S	s	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S
447	247	546	322	374	223	431	278	486	155	113	-4	201	464	182	257	175	240	157	987	687	680	905	829	877	434	1160	744	210	381	260	636	358	182	667	395	429	2039	2033	1927
1180	2640	2597	2849	2778	2577	2781	2666	2758	2668	2204	2040	2102	2037	1911	2122	2305	2294	2414	579	535	682	490	600	347	488	660	365	319	374	264	426	474	619	510	582	318	993	986	928
1916	1128	1159	1047	1052	1114	1140	1495	1512	1495	2215	2148	2105	2324	2151	2151	1896	2086	2172	14854	14534	14893	15148	14535	14639	14780	14851	14641	19673	19972	19521	20224	20557	20325	20009	20015	20152	14527	14388	14522
66319	51097	50818	50931	50382	49689	49479	53292	53380	53011	43242	42960	42769	39987	39744	40500	40714	40976	40778	122753	123248	122032	123028	123676	123169	116576	116938	116493	90038	90480	89486	88177	88029	87165	91077	90638	90646	134410	133440	134018
361629	360769	361352	361276	362291	363810	363634	356581	358850	357443	364333	364859	364913	375471	374749	375884	365513	365041	365444	212656	213160	213076	198221	200532	200138	238551	238587	240226	277169	277484	278930	283151	283289	284952	275697	277572	277372	106398	107607	107009
1422	952	1291	1363	950	1116	1109	1060	1021	1152	1366	1460	1546	1509	1572	1640	1541	1439	1469	470	486	605	751	579	376	394	865	538	1004	913	931	935	736	760	926	638	763	555	864	844
542	538	305	338	303	379	318	668	326	222	103	268	206	277	428	1	116	1	255	1513	1434	1548	1881	1341	1436	1163	1035	1163	662	836	959	910	929	1194	1211	1091	1287	2128	1831	1967
9004	9496	9736	9476	8983	9164	9281	9296	9371	9369	9102	9103	9306	9164	9304	9243	9248	9300	9175	6322	6438	6339	5747	6107	5898	6942	6921	6654	7489	7729	7489	7803	7884	7667	7743	7569	7523	4264	3930	3690
6614	13628	13598	13906	13578	13369	13491	14323	14482	14727	6111	6118	6422	5882	6225	5888	5772	5933	5717	24635	24628	25267	26123	25730	25920	22584	22816	22949	15254	15284	15531	15260	15258	15033	15719	15854	15965	31537	31735	32282
2403	1362	1919	1735	1604	1571	1838	1375	1631	1674	1191	1218	1158	1242	1289	1284	1566	1506	1296	2381	2344	2283	2372	2558	1977	2373	3036	2572	1828	1762	1665	2113	1766	1703	2088	1824	2112	2121	2069	2107
1422	2303	2036	1945	1733	1947	1904	2014	1970	2137	1874	2142	2267	1723	1942	2076	2103	2081	2256	2192	2105	2268	2573	1967	2140	1630	2039	1875	1016	1014	887	1155	1061	924	1285	1046	993	3127	2979	3048
25379	24274	23933	23646	23493	23236	23334	24990	24495	25366	17724	17602	17461	14383	14228	13788	15971	16735	16176	98548	98240	98672	105566	104349	104757	92298	92020	92334	50747	50596	50708	48580	49928	49138	50981	50552	50821	94663	95434	95915
m	1	2	S	1	2	3	1	2	e	1	2	Э	1	2	3	1	2	e	1	2	3	1	2	Э	1	2	c	1	2	m	1	2	e	1	2	S	1	2	e
e	1	1	1	2	2	2	e	e	e	1	-	1	2	2	2	3	œ	e	1	1	1	2	2	2	33	33	S	1	1	1	2	2	2	Э	ŝ	S	1	1	₽
CS49	CS50	CS51	CS53	CS54	CS55	CS55	CS 55																																
CS49.3.3	CS50.1.1	CS50.1.2	CS50.1.3	CS50.2.1	CS50.2.2	CS50.2.3	CS50.3.1	CS50.3.2	CS50.3.3	CS51.1.1	CS51.1.2	CS51.1.3	CS51.2.1	CS51.2.2	CS51.2.3	CS51.3.1	CS51.3.2	CS51.3.3	CS53.1.1	CS53.1.2	CS53.1.3	CS53.2.1	CS53.2.2	CS53.2.3	CS53.3.1	CS53.3.2	CS53.3.3	CS54.1.1	CS54.1.2	CS54.1.3	CS54.2.1	CS54.2.2	CS54.2.3	CS54.3.1	CS54.3.2	CS54.3.3	CS55.1.1	CS55.1.2	CS55.1.3

1917	1917	1917	1917	1917	1917	1916	1916	1916	1916	1916	1916	1916	1916	1916	1800	1800	1800	1800	1800	1800	1800	1800	1800	1820	1820	1820	1820	1820	1820	1820	1820	1820	1916	1916	1916	1916	1916	1916	1916
S	S	S	S	S	S	S	S	s	S	S	s	S	S	s	s	S	S	S	S	S	S	S	S	s	S	S	S	s	S	S	S	S	S	s	s	S	s	s	S
893	1176	1002	1012	660	803	1093	1466	1013	14145	9155	6668	3891	2818	2307	157	172	238	0	287	235	342	295	177	403	527	611	706	253	565	513	400	340	1397	1322	1199	2018	1876	1661	2102
857	808	602	557	777	747	560	584	550	140	266	577	1179	1132	1240	2245	2191	2215	2127	2273	2372	2156	2277	2319	3293	3494	3396	3471	3732	3677	4046	4194	4053	348	344	387	347	422	451	420
10335	10279	10113	7252	7044	7394	4394	4721	4689	2851	2814	2583	2501	2127	2054	620	639	821	637	612	581	969	627	611	204	138	318	128	192	153	346	309	371	10837	10782	10816	14525	14660	14387	14489
110348	109982	110256	109547	109116	109258	87660	87757	88292	52257	58545	58523	45569	46004	45390	46024	45954	45797	46418	46427	46547	46495	46680	46644	37848	38099	37599	37329	37290	37258	38554	38330	38439	90144	89793	90345	92283	92033	92075	91793
221565	223938	222654	254034	256258	256020	307802	309389	309457	286910	289652	290833	322856	324078	324801	358643	359330	360549	360556	361106	361112	357859	358538	359925	366458	366708	367578	361342	362013	362728	360220	360783	361024	289460	290530	289927	254871	255550	255214	253546
704	641	703	622	723	574	762	936	896	5546	5094	5113	3621	3599	3574	1455	1474	1552	1154	1752	1599	1235	1441	1121	799	746	629	697	628	865	831	822	572	834	1019	1163	809	586	722	804
1292	1357	1531	751	775	871	567	640	893	13268	13540	13152	9636	9197	9426	618	511	183	496	405	321	339	320	278	205	3	101	46	172	177	374	499	250	814	880	755	974	1123	1216	944
6838	6533	6477	7533	7457	7356	8717	8842	8704	7629	7767	7332	8518	8224	8142	9529	9791	9585	8963	9418	9469	9322	8981	9351	9207	8910	9095	9235	9076	9216	9182	9250	9304	8213	8354	8055	7896	7667	7586	7724
23506	23444	23884	18377	17891	17937	11378	11197	11631	23102	23493	23652	15453	14657	15011	5282	5337	5117	5439	5206	5400	5774	6158	6012	27199	27380	27294	27813	27017	27405	33087	32730	32846	13998	14073	14696	15901	16224	16048	16333
2397	2151	2197	2194	2209	1970	2582	3083	2806	1805	1667	1557	2045	1953	1804	2235	2273	2415	2526	2610	2621	2320	2051	2262	951	882	1032	1432	1024	1068	1326	899	1040	1318	1533	1336	1834	1625	1528	1397
1980	1675	2210	1172	1008	1431	573	717	847	78294	75483	75379	51195	49281	49599	1057	1238	1066	1108	1279	1177	888	1085	960	1946	1586	1610	1830	1563	1884	2288	2340	2020	708	1030	1299	1238	1122	1210	1201
69082	69691	69795	70095	70258	69628	54169	53561	53652	18275	22190	22199	16293	16779	16494	20387	20006	19672	19613	19439	19417	20405	20194	19984	17395	17586	17429	17986	18082	17850	18824	18554	18541	51529	51368	52041	60973	60720	60813	60607
1	2	e	1	2	e	1	2	e	1	2	e	1	2	e	1	2	e	1	2	e	1	2	e	1	2	e	1	2	ŝ	1	2	e	1	2	e	1	2	e	1
2	2	2	е	e	С	1	1	1	2	2	2	С	3	œ	1	1	1	2	2	2	3	3	3	1	1	1	2	2	2	3	ю	С	1	1	1	2	2	2	С
CS55	CS55	CS55	CS55	CS55	CS55	CS57	CS58	CS59	CS60																														
CS55.2.1	CS55.2.2	CS55.2.3	CS55.3.1	CS55.3.2	CS55.3.3	CS57.1.1	CS57.1.2	CS57.1.3	CS57.2.1	CS57.2.2	CS57.2.3	CS57.3.1	CS57.3.2	CS57.3.3	CS58.1.1	CS58.1.2	CS58.1.3	CS58.2.1	CS58.2.2	CS58.2.3	CS58.3.1	CS58.3.2	CS58.3.3	CS59.1.1	CS59.1.2	CS59.1.3	CS59.2.1	CS59.2.2	CS59.2.3	CS59.3.1	CS59.3.2	CS59.3.3	CS60.1.1	CS60.1.2	CS60.1.3	CS60.2.1	CS60.2.2	CS60.2.3	CS60.3.1

1916	1916	1815	1815	1815	1815	1815	1815	1815	1815	1815	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1755	1755	1755	1755	1755	1755	1755	1755	1755	1785	1785
S	S	S	S	S	S	S	S	s	s	S	s	S	S	S	s	S	S	S	S	S	S	S	S	s	S	S	s	s	S	S	S	S	S	s	s	S	S	S	S
2073	2101	1053	1316	1226	1172	1291	1406	1597	1155	1007	2174	2447	2418	1625	1468	1810	12774	12411	12160	1293	1148	917	1122	1050	1349	1448	1429	1482	1681	1701	1692	1491	1795	1768	2033	1701	1737	839	1115
464	316	3585	3623	3385	3591	3586	3453	3307	3724	3524	4050	3660	3972	4033	4026	3943	3186	2850	3027	4645	4979	4512	5156	4616	4572	5007	4899	4855	6066	6247	5991	5894	6018	5834	5994	5800	6134	4095	4277
14334	14399	91	145	114	124	62	49	171	32	36	2487	2405	2378	2020	1775	1844	1529	1304	1309	204	219	52	287	310	289	451	459	432	1116	1037	935	1078	986	1111	922	693	685	251	276
92705	91614	46695	46826	46644	47104	46821	47067	46818	46720	46968	21750	21898	21927	24039	23885	24075	14959	15185	14890	39146	39179	38603	38185	37814	37605	41532	41605	41583	43613	43741	43784	44739	44464	44555	45631	45255	45599	47920	47592
256599	255955	337422	338897	339749	328156	327964	327839	332971	332348	332554	315809	317581	316911	315435	317262	315498	284000	284015	283991	339979	340832	343187	338101	337886	339156	333188	333393	334071	287348	287997	288633	286811	287918	288000	289666	290635	290076	344760	345413
882	908	580	317	417	200	263	235	319	76	381	381	257	132	331	۲	237	109	155	329	447	999	484	342	260	379	443	330	390	406	443	324	410	160	108	294	308	468	347	349
918	1236	1329	1	800	824	1713	1581	1924	1518	1692	117442	116429	115908	120176	118785	119349	98654	97481	97118	19536	19098	18938	20341	20247	21133	24414	23989	24316	103088	102846	102416	102169	102127	101622	104097	103565	104071	1292	1304
7971	7940	8445	8222	8191	8514	8230	8312	8628	8678	8705	5746	5717	5805	5936	5913	6264	3405	3044	3226	8373	8062	8120	8232	8064	8364	7921	7746	7784	6137	6122	6319	6423	6629	6133	6370	5957	6254	8034	8437
16366	16118	96258	95443	95346	100363	100279	99643	93421	93429	93191	72106	72635	71343	73354	72688	72881	64838	64906	64313	26069	67974	68701	70345	70080	70842	77261	76923	77179	121917	120773	120896	119479	119501	119062	122914	122350	122850	84167	84374
1648	1737	1289	1202	1317	1390	1102	1253	1378	1280	1185	25900	26385	26379	15150	14509	14832	152227	152341	150916	2586	2807	2510	2116	2084	2174	2005	1964	2082	3725	3641	3487	3582	3481	3554	3800	3493	3345	1736	2050
1185	1175	6593	6260	6466	7222	7002	7145	6595	6111	6639	2714	2740	2213	2725	2672	2623	2061	1838	2103	4325	4348	4411	4300	4238	4534	4669	4715	4948	6167	6067	6236	6043	6177	6106	5830	6235	6446	5627	5295
59568	60287	19500	19232	18834	21507	21411	21897	21110	21547	20946	6441	6570	6339	7231	7237	7109	3627	3734	3828	15677	15411	15435	15874	15797	15482	17604	17335	17270	18616	18354	18540	18903	19112	18848	18029	18017	18225	19557	19226
2	ε	1	2	ε	1	2	ю	1	2	ε	1	2	æ	7	2	ε	1	2	З	1	2	ŝ	1	2	ε	1	2	ŝ	1	2	æ	1	2	c	1	2	c	1	2
e	3	1	Ч	1	2	2	2	Э	æ	Э	Ţ	7	7	2	2	2	Э	3	3	7	Ţ	1	2	2	2	3	c	33	1	1	Ч	2	2	2	e	3	S	1	H
CS60	CS60	CS61	CS62	CS63	CS64	CS65	CS65																																
CS60.3.2	CS60.3.3	CS61.1.1	CS61.1.2	CS61.1.3	CS61.2.1	CS61.2.2	CS61.2.3	CS61.3.1	CS61.3.2	CS61.3.3	CS62.1.1	CS62.1.2	CS62.1.3	CS62.2.1	CS62.2.2	CS62.2.3	CS62.3.1	CS62.3.2	, CS62.3.3	CS63.1.1	CS63.1.2	CS63.1.3	CS63.2.1	CS63.2.2	CS63.2.3	CS63.3.1	CS63.3.2	CS63.3.3	CS64.1.1	CS64.1.2	CS64.1.3	CS64.2.1	CS64.2.2	CS64.2.3	CS64.3.1	CS64.3.2	CS64.3.3	CS65.1.1	CS65.1.2

1785	1785	1785	1785	1785	1785	1785	1785	1785	1785	1785	1785	1785	1785	1785	1785	1755	1755	1755	1755	1755	1755	1755	1755	1755	1785	1785	1785	1785	1785	1785	1785	1785	1785	1755	1755	1755	1755	1755	1755
S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	s	S	S	s	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S
1016	976	972	1067	1394	966	1117	2135	2134	2418	1878	1452	1891	1846	1810	2083	1450	1013	1367	1120	1488	1376	1105	1393	1231	194	198	207	233	263	378	322	425	435	4543	4782	4665	3988	3769	3888
4199	4315	4169	4181	4623	4613	4516	4122	4145	4104	3757	3916	3957	4271	4015	3999	5172	4722	4803	4752	4678	4909	5026	4938	4886	3766	3463	3538	3500	3554	3647	3445	3674	3596	18659	18779	19045	16416	16468	16480
273	307	394	216	357	301	504	1535	1463	1502	1839	1679	1770	1777	1863	1947	1315	1339	1361	1616	1546	1807	1487	1468	1270	2530	2381	2435	1339	1377	1357	2561	2891	2750	4866	5092	5182	4876	4656	4839
47423	48272	47610	47807	48282	48121	48329	41022	41542	41538	40567	40087	40070	42381	42322	42459	37173	37430	37314	37303	37389	37241	36552	36738	36595	67550	67305	67388	59059	58732	58885	69576	68868	69092	119033	118483	119013	115993	115709	114825
346046	338836	339085	338854	335225	335277	335512	313553	313342	314267	320794	320541	320530	306481	307297	306906	297250	298122	298481	300401	301701	302525	297016	297648	297872	323394	324641	325463	349523	350437	351272	326737	327383	328675	229296	230612	229872	239879	240586	240619
270	409	224	317	324	309	278	108	233	239	346	255	238	454	336	256	89	239	553	339	289	526	806	512	293	2278	2160	1965	1896	1690	1816	2031	2029	2168	23466	23203	23246	23695	23601	23525
1294	1521	1552	1728	1923	1747	1960	14544	14460	14557	14205	14064	14117	17338	17100	16738	98213	98190	97736	94345	94073	93883	97822	97435	97808	551	206	484	282	191	539	613	581	271	3651	3733	4369	3900	3722	4248
8127	8536	8586	8262	8112	7934	8212	7785	7632	8062	7385	7825	7637	7175	7340	7521	6637	6384	6575	6257	6595	6494	6366	6446	6179	9364	8888	9095	9270	8668	9214	8718	8755	8654	5072	5010	5077	5210	5325	5284
84662	82664	82052	82152	91407	90439	90344	125269	125216	125122	118079	118035	118251	130850	130224	131325	91745	91608	91275	87264	87027	86376	91296	91515	91054	21935	21774	22339	19420	19009	19059	22186	22006	22375	75416	75372	75250	71546	71755	71690
1924	1784	2035	1973	1868	1710	1864	2270	2560	2538	2480	2446	2376	2281	2411	2128	6016	5985	5977	5781	6263	6174	6288	6151	6162	1443	1433	1724	1500	1635	1511	1544	1787	1810	1572	2015	1747	1990	1641	1938
5322	5706	5675	5760	6235	6123	6101	9298	9520	9439	8783	8711	8765	10212	10030	10072	4465	4824	4739	4438	4198	4410	4837	4402	4516	4870	5124	5123	4350	3783	3894	4878	4751	5028	68709	69261	69337	71002	70834	70416
19177	22074	22076	22102	22707	22496	22401	17298	17258	17893	16537	16388	16990	17726	17591	17905	14814	15062	14864	14904	14905	14268	15156	15169	15005	33614	33736	33549	27455	27550	27851	31146	31220	31579	62241	62231	62265	62783	63022	63028
Э	1	2	ю	1	2	ю	1	2	Э	1	2	Э	7	2	e	1	2	m	1	2	m	1	2	Э	1	2	ε	1	2	ю	7	2	ε	1	2	ю	1	2	Э
Ţ	2	2	2	3	3	с	1	۲	Ļ	2	2	2	e	e	ю	H	H	H	2	2	2	m	e	Э	H	Ч	1	2	2	2	£	e	3	1	1	Ч	2	2	2
CS65	CS66	CS67	CS68	CS69	CS69	CS69	CS69	CS69	CS69																														
CS65.1.3	CS65.2.1	CS65.2.2	CS65.2.3	CS65.3.1	CS65.3.2	CS65.3.3	CS66.1.1	CS66.1.2	CS66.1.3	CS66.2.1	CS66.2.2	CS66.2.3	CS66.3.1	CS66.3.2	CS66.3.3	CS67.1.1	CS67.1.2	CS67.1.3	CS67.2.1	CS67.2.2	CS67.2.3	CS67.3.1	CS67.3.2	CS67.3.3	CS68.1.1	CS68.1.2	CS68.1.3	CS68.2.1	CS68.2.2	CS68.2.3	CS68.3.1	CS68.3.2	CS68.3.3	CS69.1.1	CS69.1.2	CS69.1.3	CS69.2.1	CS69.2.2	CS69.2.3

1755	1755	1755	1750	1750	1750	1750	1750	1750	1750	1750	1750	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1680	1680	1680	1680	1680	1680	1680	1680	1680	1705
S	S	S	FN	ΓN	Γ	FN	Ч	N	Ч	Ч	Z	s	S	s	s	S	s	s	s	S	S	S	S	S	S	S	S	s	s	_	_	_	_	_	_	_	_	_	_
4570	4535	4387	1647	1581	1900	1702	1612	1253	1544	1313	1648	5176	5817	5585	5067	5294	4954	5078	4643	4699	9279	10018	10219	15720	15940	15542	7777	7667	8318	1136	848	868	913	1033	927	817	544	702	761
17066	17038	16942	194	630	566	501	742	367	455	356	446	89795	89295	89637	10078	10290	9904	9348	9507	9305	8509	8524	8306	7816	7716	7729	6640	6561	6528	110	195	321	289	185	310	346	154	204	86
4718	4542	4723	7672	7864	7890	7745	7742	7887	10636	10632	10216	451	407	401	1067	1202	1272	1859	1923	1742	2565	2690	2732	9093	9038	9062	1656	1825	1734	12847	12539	12084	10195	10433	10204	18167	18144	18164	26531
117961	117062	117358	69794	68817	68629	70097	69832	69420	76523	75974	76368	1045	1098	1003	943	789	765	2084	2106	2187	4945	5109	5077	118746	118706	118925	52726	51818	51802	84145	84349	83953	84852	83398	83785	86554	86504	86531	78747
237974	237208	237193	328081	328364	328626	330986	330661	331781	315403	316781	317562	247087	248767	248783	238016	240368	240064	260932	262416	263348	240637	241044	242017	113120	113708	113363	290458	290861	291816	276398	276384	275773	284827	284620	285053	282121	282724	283453	273550
22984	22533	22729	15018	14780	14907	14875	14753	14963	16581	17071	16644	14445	14589	14676	20674	21078	20791	21207	20749	20605	40224	40602	40274	30488	30390	30523	42315	42710	42817	14299	14809	14398	15307	15613	15609	0006	9232	9511	2654
4322	4408	3957	1097	1298	1432	1326	1300	1237	1993	1432	1787	5613	5726	5458	9442	8991	9279	9784	10229	9757	8863	9546	8905	24423	24805	25454	4097	3574	4204	1512	1552	1204	986	1076	1096	649	749	732	1114
5287	5328	5198	6652	6771	6980	6597	6459	7026	5874	5877	6076	2339	2683	2291	2456	2286	2383	2511	2572	2725	1317	1568	1399	2510	2445	2383	3143	3524	3582	5891	5767	6310	5838	5730	5960	5994	5945	6025	5921
76323	75646	75490	46415	46313	45966	45814	46167	46310	52146	52198	51853	119425	119476	119169	159080	158932	158570	172445	172330	172240	201220	201815	202180	271615	271653	271152	154978	155235	155462	51997	52192	51949	53045	53440	53180	30358	30255	30702	33380
2073	1906	1609	2935	3148	3391	3226	3264	3256	3236	3638	3356	994	634	800	478	746	516	442	493	43	567	305	361	5065	5352	4752	1450	1545	1594	3188	2902	2839	3262	3318	3286	2672	2706	2758	2625
67810	67712	67831	39857	38609	39080	38937	38949	38917	45079	45089	44522	47629	47676	48160	70154	70393	70944	72926	72459	72895	89400	88903	88243	104836	105404	105679	98038	97531	98404	53406	53068	53546	55574	55875	55875	32086	31761	31843	4906
63604	64680	64807	23818	24448	24358	23029	22502	22822	26172	26636	26364	1062	1184	1109	1193	1271	1152	682	762	804	1902	2053	1822	56269	56524	56637	5827	5942	5802	31689	32180	32829	31811	31760	31173	31815	32364	31754	21998
1	2	3	1	2	e	1	2	Э	1	2	m	1	2	e	1	2	c	1	2	e	1	2	c	1	2	3	1	2	33	1	2	3	1	2	33	1	2	Э	-
e	3	С	1	1	7	2	2	2	£	c	m	1	7	1	2	2	2	m	£	e	1	1	1	2	2	2	œ	œ	œ	1	1	1	2	2	2	œ	С	С	-
CS69	CS69	CS69	CS70	CS71	CS71	CS72	CS73	CS74																															
CS69.3.1	CS69.3.2	CS69.3.3	CS70.1.1	CS70.1.2	CS70.1.3	CS70.2.1	CS70.2.2	CS70.2.3	CS70.3.1	CS70.3.2	CS70.3.3	CS71.1.1	CS71.1.2	CS71.1.3	CS71.2.1	CS71.2.2	CS71.2.3	CS71.3.1	, CS71.3.2	CS71.3.3	CS72.1.1	CS72.1.2	CS72.1.3	CS72.2.1	CS72.2.2	CS72.2.3	CS72.3.1	CS72.3.2	CS72.3.3	CS73.1.1	CS73.1.2	CS73.1.3	CS73.2.1	CS73.2.2	CS73.2.3	CS73.3.1	CS73.3.2	CS73.3.3	CS74.1.1

1705	1705	1705	1705	1705	1705	1705	1705	1708	1708	1708	1708	1708	1708	1708	1708	1708	1695	1695	1695	1695	1695	1695	1695	1695	1695	1685	1685	1685	1685	1685	1685	1685	1685	1685	1735	1735	1735	1735	1735
_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	z	z	z	z	z	z	z	z	z	8	в	8	в	в
698	780	757	921	885	457	703	665	697	508	1006	518	439	483	721	720	700	602	887	747	417	431	471	293	611	426	5910	5596	5701	46149	46204	46589	973	1073	806	904	1129	948	1472	1352
142	158	170	285	249	270	531	114	101	65	22	281	92	31	136	181	62	1175	1350	1102	273	564	815	304	221	204	423	188	Э	650	418	369	485	268	268	1578	1780	1936	1916	1612
26591	26805	26945	26822	26522	24483	25229	25058	24345	24506	24596	21441	21479	21709	28279	28199	28330	21218	21345	21218	21952	22149	22484	23556	23441	23429	20549	20657	20492	15060	15051	14973	13662	13301	13289	9283	9119	9455	10762	10528
78342	79284	78057	77429	77900	76827	76349	76789	64301	63756	63259	60591	60528	60061	63291	62989	63349	39558	39460	39507	47625	47320	46820	51069	51718	51348	63661	63843	63679	66215	66357	66435	66567	65682	65390	62133	62392	62146	65169	65071
275203	276717	269225	270258	271133	273620	273599	274933	309905	313504	313046	313887	316011	315346	310062	311456	310804	324909	326755	326299	329912	332188	331483	334168	335560	336229	297821	299512	299431	266232	267173	267958	313849	315110	314625	331883	331540	332602	329692	329842
2205	2217	5271	5021	4732	8606	9173	9366	6498	6635	6532	12966	13586	13403	655	517	852	667	723	618	1624	2027	1846	797	891	1085	15595	15417	14839	9489	9244	9281	19755	19923	19735	7685	7490	7551	1411	1347
1172	1110	1152	1023	1122	906	1028	771	1004	730	864	1297	1209	1627	1629	1352	1446	4030	3919	4014	7674	7838	7654	1711	1770	1932	1276	1553	1416	16298	15828	15789	985	898	841	3960	3843	4045	1046	1181
6014	5766	5747	5645	5731	5681	5629	5786	6680	6731	6782	6311	6324	6387	6636	6574	6443	5941	5688	5803	6466	6344	6341	6545	6627	6575	4733	4913	4763	4080	4172	4154	6525	6357	6471	6839	6755	7023	6877	7258
32902	33361	41113	40952	40807	43413	43437	43377	26351	26616	26299	42700	42630	43034	21612	21043	21111	47615	47859	47459	40050	40574	40810	25296	24893	25142	53829	53670	53612	76649	75735	75122	51789	51819	51651	30843	31537	31381	27141	26423
2932	2850	3039	2781	2914	2381	2683	2943	2210	2296	2475	2307	2406	2502	2597	2521	2506	2213	2719	2300	2117	2197	2151	2390	2384	2256	12670	13221	12475	36794	37324	36954	2933	2684	2387	8447	8310	8244	9358	9298
5174	5010	8480	8479	8346	13740	13615	13552	9558	9585	9194	21271	21254	20676	1429	1141	1466	2455	2740	2508	6638	6418	6782	1151	1747	1257	23930	23681	23581	18398	18104	18120	27834	27682	27647	8289	8763	8750	1832	1767
22383	22044	19671	20056	19896	20294	19851	20633	19160	18945	18761	16476	16450	16685	16431	16178	16806	5938	6061	5999	8581	8241	8450	8952	8668	8890	15553	15659	15552	18331	18368	18200	18915	19173	18998	19468	19073	19407	21038	21315
2	3	1	2	3	1	2	З	7	2	e	H	2	e	1	2	e	H	2	æ	Ч	2	3	Ч	2	3	1	2	3	1	2	ю	Ч	2	ю	1	2	c	1	2
Ч	1	2	2	2	3	33	Э	Ļ	f	H	2	2	2	œ	æ	œ	H	-	f	2	2	2	œ	œ	33	1	Ч	Ч	2	2	2	æ	œ	æ	1	1	1	2	2
CS74	CS76	CS 76	CS 76	CS76	CS 76	CS76	CS76	CS76	CS76	CS77	CS77	CS77	CS77	CS77	CS77	CS77	CS77	CS77	CS78	CS79	CS79	CS79	CS 79	CS 79															
CS74.1.2	CS74.1.3	CS74.2.1	CS74.2.2	CS74.2.3	CS74.3.1	CS74.3.2	CS74.3.3	CS76.1.1	CS76.1.2	CS76.1.3	CS76.2.1	CS76.2.2	CS76.2.3	CS76.3.1	CS76.3.2	CS76.3.3	CS77.1.1	CS77.1.2	, CS77.1.3	CS77.2.1	CS77.2.2	CS77.2.3	CS77.3.1	CS77.3.2	CS77.3.3	CS78.1.1	CS78.1.2	CS78.1.3	CS78.2.1	CS78.2.2	CS78.2.3	CS78.3.1	CS78.3.2	CS78.3.3	CS79.1.1	CS79.1.2	CS79.1.3	CS79.2.1	CS79.2.2

1735	1735	1735	1735	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1740	1740	1740	1740	1740	1740	1740	1740	1740	1685	1685	1685
в	8	в	в	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	S	S	S	S	S	S	_	_	_	_	_	_	_	_	_	_	_	_
1466	1017	1140	1074	1946	2053	2165	5231	5615	5152	3582	3494	3358	2829	3301	3192	6067	5751	6137	3832	4629	4005	545	371	235	313	109	470	1682	1666	1708	1833	1619	1707	1720	1868	1679	-1	383	446
1571	1089	870	941	972	973	1008	561	455	537	824	930	939	1115	1001	973	589	823	677	069	691	949	1233	1097	1129	1043	928	1114	730	767	716	548	222	401	668	332	469	204	70	235
10463	17067	16921	16614	5815	5922	5901	14801	14896	14683	10894	10969	11050	6488	6211	6383	16823	16960	16631	12578	12334	12224	12065	12319	12061	10410	10248	10252	19495	19625	20050	31256	31028	31001	31289	31152	31361	25058	24735	24591
65022	62806	62295	63110	55283	55132	54747	87396	86944	87044	44909	44508	44256	59232	58629	58418	62055	61768	62185	58804	58911	58328	49134	49521	48903	49928	49575	49431	65527	65979	65779	65651	65962	65359	65338	65474	65626	72650	72226	72642
329788	314710	315239	316983	300007	301902	302604	302289	303142	302964	327547	330655	328562	315970	315164	316932	312927	314280	314548	311546	312610	312338	380568	381624	381201	382309	383172	384766	306386	306372	307251	287675	289596	289170	288283	289763	289014	312620	313583	312493
1152	7062	6910	6755	66216	65812	64838	2582	2550	2365	18248	18703	18179	37087	37174	37436	1792	1699	1857	20472	20471	20616	1005	1252	1260	2840	2913	3319	5559	5585	5379	1203	1217	939	984	1124	1264	863	584	795
1080	3556	3541	3470	1149	1594	1390	758	1224	829	912	834	1181	1070	1391	1621	1150	1168	955	1274	1031	1193	458	559	554	625	737	685	1084	1022	1211	1257	1228	1321	942	1402	1070	640	1051	978
7144	6277	6330	6340	5102	4804	4945	6250	6240	6245	5622	5567	5784	5281	5518	5509	6305	6274	6342	5487	5683	5639	8683	7865	8133	8088	8141	8244	5776	6082	6097	6087	5649	5991	5925	5983	5937	7075	0069	6895
27075	37824	37840	38024	75351	75108	74786	38592	38740	38690	45583	45486	45727	66471	66815	66645	36617	36485	36790	47804	47341	47699	8954	9158	9154	10219	10205	10505	34971	34910	34803	26916	26664	26792	26840	26725	26874	28976	29261	29081
9443	8191	7891	7942	9984	9661	9266	11116	10968	10496	10163	10843	10151	10080	10098	10147	13338	13140	13546	11795	12024	11828	1439	1429	1022	1561	1417	1791	5592	5350	5861	5801	5467	5393	5657	5522	5593	1946	1609	1800
1741	7701	7814	8027	66664	66661	66030	4649	4865	4755	22615	21583	22275	41197	41392	40673	3368	3499	3249	24497	24207	24324	323	568	445	2874	3086	3301	7426	7346	7106	1781	1744	1683	1732	1981	1934	2020	1945	2164
21267	17064	17213	17015	12494	12618	12522	32569	32921	33028	10675	10611	10481	16263	16770	16469	19980	19822	19928	16628	16876	16351	14272	14138	14383	12768	12658	12573	15919	16217	15950	16096	15954	16009	17807	17997	17807	22912	22849	22799
m	1	2	e	1	2	S	1	2	e	1	2	3	1	2	e	1	2	e	1	2	£	1	2	e	1	2	Э	1	2	3	1	2	3	1	2	e	1	2	m
2	3	33	e	7	1	1	2	2	2	Э	3	3	7	Ч	1	2	2	2	e	e	£	1	7	Ļ	2	2	2	1	1	1	2	2	2	e	3	e	Ļ	Ч	Ч
CS79	CS79	CS79	CS79	CS80	CS81	CS81	CS82	CS82	CS82	CS82	CS82	CS82	CS83	CS84	CS84	CS84																							
CS79.2.3	CS79.3.1	CS79.3.2	CS79.3.3	CS80.1.1	CS80.1.2	CS80.1.3	CS80.2.1	CS80.2.2	CS80.2.3	CS80.3.1	CS80.3.2	CS80.3.3	CS81.1.1	CS81.1.2	CS81.1.3	CS81.2.1	CS81.2.2	CS81.2.3	CS81.3.1	<sup>T</sup> CS81.3.2	CS81.3.3	CS82.1.1	CS82.1.2	CS82.1.3	CS82.2.1	CS82.2.2	CS82.2.3	CS83.1.1	CS83.1.2	CS83.1.3	CS83.2.1	CS83.2.2	CS83.2.3	CS83.3.1	CS83.3.2	CS83.3.3	CS84.1.1	CS84.1.2	CS84.1.3

1685	1685	1685	1685	1685	1685	1685	1685	1685	1685	1685	1685	1685	1685	1685	1685	1685	1685	1685	1685	1685	1685	1685	1685	1700	1700	1700	1700	1700	1700	1700	1700	1700	1685	1685	1685	1685	1685	1685	1685
_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_
531	518	384	744	689	443	338	505	389	442	361	417	486	460	787	309	354	343	189	699	667	255	387	189	3158	3268	3108	3192	3440	2731	3271	3265	3162	493	581	558	349	432	514	707
148	155	180	189	233	133	166	362	138	310	193	192	188	75	57	26	159	8	136	188	2	7	154	277	16	144	-27	64	107	26	-17	0	214	6	342	93	256	363	242	270
25176	25185	25446	24934	24755	24551	27180	26885	26819	26813	26605	26658	28418	28587	28737	27108	26715	26885	25893	26394	25769	26453	26041	26101	30606	30448	30737	30392	30225	29953	30728	30692	30389	23411	23226	23181	23867	23772	23826	24357
70662	70530	70364	69565	69234	69286	74438	74066	73938	74474	74454	75246	72400	72150	72109	69289	68255	68818	69740	69381	69642	69353	69862	68860	64903	64801	64884	65725	65416	65825	65507	65870	65188	71489	70835	70248	69190	69064	69369	69091
314013	315040	314596	318186	319680	318930	300145	301887	301935	298094	300838	299807	303010	304022	302861	304019	305168	305567	303369	304916	304572	307116	307534	307294	294875	296282	296208	295379	296239	296007	296422	298208	296574	303770	305739	304655	307826	308354	306868	307865
724	574	530	619	934	629	675	843	474	865	750	542	457	743	820	889	494	687	678	599	815	627	626	471	605	872	828	757	670	843	746	768	666	713	771	685	581	646	795	592
1428	1477	1351	1264	1063	1052	928	1075	643	891	1033	820	846	1063	1134	1564	1362	1164	1378	1430	1299	1400	1449	1257	1087	887	549	740	979	1077	767	1157	1039	2180	1694	2047	1675	1803	2028	1931
6994	6945	7028	6772	6823	7046	6651	6531	6448	6535	6510	6566	6546	6530	6551	6518	6874	6811	6913	6737	6655	6429	6527	6789	5703	5857	5724	5626	5848	5687	5888	5625	5723	6725	6947	0069	6658	7095	6876	6815
29419	29819	29831	28580	28519	28794	28448	28053	28322	28677	28928	28662	27929	28217	27793	22428	22357	22021	21540	21645	21597	22935	22410	22912	23825	23610	23651	23802	23796	23364	24079	23904	23365	29982	29321	29427	29615	29627	29277	29518
2063	2336	2058	2219	2191	2002	2568	2913	3022	3194	3084	3159	2779	2818	3062	2246	2145	2167	2235	2330	2376	2386	2416	2141	10464	10636	10520	10441	10784	10443	11235	11427	11384	2189	2034	2208	2319	2147	2145	2193
1922	1791	2126	1788	2093	2072	2029	2165	1816	2355	2298	1885	1678	2142	1886	1527	1506	1226	1477	1429	1210	1382	1389	1157	1643	1968	2028	1773	1537	1887	1803	2066	2033	1823	2319	1923	1790	2165	1796	2024
19202	19528	19376	20386	20307	20683	22642	22500	22782	23471	23553	23133	20654	20920	21320	20598	20607	20679	20333	20184	20344	19195	19584	19299	17684	17500	17202	17566	17401	17277	17793	17575	17352	22660	22956	22832	21209	21694	21540	21090
1	2	œ	1	2	ю	1	2	ŝ	1	2	ŝ	1	2	œ	1	2	S	1	2	ю	1	2	ю	1	2	3	1	2	æ	1	2	Э	1	2	Э	1	2	£	1
2	2	2	£	3	e	1	1	1	2	2	2	£	e	c	7	Ч	1	2	2	2	e	e	e	7	1	1	2	2	2	e	e	œ	Ч	1	7	2	2	2	e
CS84	CS84	CS84	CS84	CS84	CS84	CS85	CS 85	CS85	CS86	CS87	CS88																												
CS84.2.1	CS84.2.2	CS84.2.3	CS84.3.1	CS84.3.2	CS84.3.3	CS85.1.1	CS85.1.2	CS85.1.3	CS85.2.1	CS85.2.2	CS85.2.3	CS85.3.1	CS85.3.2	CS85.3.3	CS86.1.1	CS86.1.2	CS86.1.3	CS86.2.1	CS86.2.2	CS86.2.3	CS86.3.1	CS86.3.2	CS86.3.3	CS87.1.1	CS87.1.2	CS87.1.3	CS87.2.1	CS87.2.2	CS87.2.3	CS87.3.1	CS87.3.2	CS87.3.3	CS88.1.1	CS88.1.2	CS88.1.3	CS88.2.1	CS88.2.2	CS88.2.3	CS88.3.1

1685	1685	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1770	1770	1770	1770	1770	1770	1770	1770	1770	1800	1800	1800	1800	1800	1800	1800	1800	1800	1760	1760
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501	575	5018	5115	5232	5413	4956	5380	4621	5167	4604	4633	4506	4656	4566	4334	4557	4712	4773	4559	4513	4629	4570	4100	3798	4266	4586	4859	4502	3726	3584	3803	3531	3676	3886	3970	4422	3924	1185	1340
203	381	3131	3230	3209	3190	3259	3096	3178	2936	3228	2712	2729	2661	2568	2438	2489	2930	2723	2974	2087	2410	2201	2093	2205	1892	2159	1848	2076	2095	2133	1993	1895	2034	2140	1884	1482	1493	-34	0
24308	24395	472	513	392	508	468	558	718	746	619	89	79	125	64	36	65	113	141	81	435	326	437	450	422	516	304	379	347	421	353	379	447	418	445	476	364	272	29108	28624
68941	68744	30635	30621	30377	29265	29384	29809	29753	30029	29946	30285	30441	30196	34313	33450	33773	28334	29105	28594	43194	43419	43316	44179	44385	43831	45732	45612	45513	38454	38133	38687	38741	38451	38435	46389	45488	45846	61178	60118
309135	307918	321616	322206	320859	320851	322292	321321	326186	326720	327025	318668	319250	318778	322204	321298	321848	318787	318629	319487	324247	325856	326334	332752	334156	333066	325778	328094	326767	336110	336960	335995	339340	339902	339200	332385	334135	333990	306961	308753
626	736	496	165	263	381	362	613	540	344	410	345	247	463	444	203	402	260	352	318	531	265	629	693	503	597	320	290	490	619	546	807	685	612	503	737	318	505	1191	1189
1718	2073	157	168	347	H	280	83	204	105	06	H	234	151	£	42	62	H	97	255	194	272	1	227	161	30	159	60	68	384	365	352	191	492	91	238	214	171	895	955
7019	7063	5518	5681	5742	5652	5527	5785	5650	5649	5685	5838	5793	5622	5880	5906	5828	5618	5745	5679	5921	5972	6183	6113	6178	6112	5786	5775	5993	6447	6262	6402	6194	6217	6091	6307	6399	6324	6673	6316
29815	29576	10279	10077	10072	10342	10284	10308	10618	10553	11081	8531	8506	8429	8026	8007	8007	8231	8584	8248	10904	10575	10850	10812	10497	10793	10227	9866	9962	7814	7973	7963	7922	8111	7988	7815	7624	7727	18492	18769
2246	2206	179701	178210	178533	175403	175190	175143	163372	163691	163080	180714	179790	179935	178661	178397	177705	183675	185242	184565	172732	172921	172254	166443	166218	166333	177238	177416	177783	142619	143067	142397	139632	138809	139074	138419	137727	137434	6275	6409
1981	2095	795	647	637	973	843	803	734	879	870	587	597	481	664	469	582	548	664	661	1045	760	837	1133	735	669	620	768	664	1302	1458	1725	1590	1632	1105	1575	1165	1354	1654	1623
21260	21435	8689	8995	8742	8522	8233	8958	8765	8861	8651	8630	8588	8448	9799	9448	9554	7816	7927	7732	12220	12363	12433	11618	11526	11399	13076	12920	12820	12093	12325	11998	11969	11850	11980	16176	16312	15779	15855	15692
2	Э	1	2	c	7	2	e	1	2	m	1	2	c	7	2	e	1	2	c	7	2	c	1	2	e	1	2	ŝ	1	2	e	1	2	ß	1	2	c	1	2
c	Э	7	1	1	2	2	2	m	œ	c	1	1	1	2	2	2	e	c	œ	7	1	1	2	2	2	3	е	3	1	1	1	2	2	2	3	£	c	1	1
CS88	CS88	CS89	CS90	CS91	CS91	CS91	CS91	CS91	CS91	CS91	CS91	CS91	CS92	CS93	CS93																								
CS88.3.2	CS88.3.3	CS89.1.1	CS89.1.2	CS89.1.3	CS89.2.1	CS89.2.2	CS89.2.3	CS89.3.1	CS89.3.2	CS89.3.3	CS90.1.1	CS90.1.2	CS90.1.3	CS90.2.1	CS90.2.2	CS90.2.3	CS90.3.1	CS90.3.2	CS90.3.3	L CS91.1.1	CS91.1.2	CS91.1.3	CS91.2.1	CS91.2.2	CS91.2.3	CS91.3.1	CS91.3.2	CS91.3.3	CS92.1.1	CS92.1.2	CS92.1.3	CS92.2.1	CS92.2.2	CS92.2.3	CS92.3.1	CS92.3.2	CS92.3.3	CS93.1.1	CS93.1.2

1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1760	1775	1775	1775	1775	1775	1775	1775	1775	1775	1669	1669	1669	1669	1669	1669	1669	1669	1669	1780	1780	1780	1780	1780	1780
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1281	1323	1069	1228	1194	1407	1201	1355	1382	797	1283	1289	1043	847	1154	1216	220	274	332	0	414	284	124	199	122	308	233	369	325	334	389	518	550	726	3743	4096	4201	3895	3969	4155
m	-55	151	72	2	209	9-	-32	71	84	11	-33	-27	-34	41	76	1595	1622	1265	1441	1400	1459	25264	24786	25200	25	0	1	86	-20	25	100	-32	40	1493	1461	1566	1503	1330	1491
28979	29249	29374	29076	28629	28028	27988	28697	28499	28304	29123	28565	29005	28405	28454	28434	143	202	135	48	166	196	87	97	129	28907	28986	28763	27377	27762	27231	29481	29723	29607	5377	5150	5217	4289	4345	4330
60873	60834	60307	60245	60704	60473	60252	57845	57360	57794	56776	57306	56659	55934	56439	56270	2817	2619	2644	1964	1911	1911	1787	1763	1750	61316	61614	61440	61511	60808	60848	61097	60730	60932	5810	5636	5738	31251	30819	31007
309057	308439	308907	309212	307488	309465	308791	309216	310050	311579	311003	311765	310090	311601	312671	312457	495086	498150	498565	501642	503122	502818	489937	491715	491758	308532	309950	310864	310686	311104	310898	311164	311619	312710	425640	426411	426850	402213	403208	403457
821	1083	809	770	1027	096	1100	666	947	729	1135	935	896	938	1029	1096	1450	1373	1315	1533	1554	1367	1358	1310	1472	687	862	700	922	745	964	834	982	1062	18671	18885	18813	10816	10859	10825
785	840	653	922	883	973	1065	1070	1034	950	1225	1062	750	974	006	1071	Ļ	1	59	256	119	1	18	38	2	766	995	1218	1486	1054	1058	981	921	853	1708	1422	1347	1526	1142	1157
6339	6243	6359	6190	5786	6603	6273	6321	6405	6291	6417	6404	6439	6194	6535	6389	8466	8410	8518	8304	7977	8257	7780	7740	7703	6976	6655	6928	6887	6980	6792	6703	6687	6674	4304	4651	4584	5855	6348	5956
18795	18716	18582	18706	18947	18407	18638	18024	17710	17981	17713	17907	17531	17640	17733	17874	9922	9737	9443	9589	9432	9414	9213	9569	9762	18839	18730	19077	19621	19196	18751	18853	18848	18909	48549	48541	47858	38087	38197	38030
6434	6074	5702	6205	6811	6861	6817	6422	6444	5761	6229	6153	6114	6249	6604	6351	2275	1921	2606	2135	2206	2328	1696	2044	1940	1773	1750	1946	1762	2078	1620	2054	2254	2195	12320	12319	12590	12919	12850	13309
1427	1656	1471	1313	1801	1620	1405	1409	1763	1712	1698	1600	1439	1388	1341	1540	532	343	491	502	548	345	533	383	399	1112	918	1257	1641	1170	1152	1105	1339	1385	25690	25916	26176	15600	15138	15469
15411	15270	15154	15133	14592	14694	14572	14852	14890	14639	13822	13612	13659	12546	12399	12863	1780	1688	1848	1745	1748	1743	1745	1678	1763	16794	16286	16423	17230	16989	17441	14972	15271	15258	1609	1579	1770	4434	4337	4501
m	1	2	e	1	2	e	1	2	e	1	2	e	7	2	Э	7	2	Э	7	2	Э	1	2	ю	1	2	S	1	2	e	1	2	e	1	2	ŝ	1	2	m
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CS93	CS94	CS95	CS96	CS97	CS97	CS97	CS97	CS97	CS97																														
CS93.1.3	CS93.2.1	CS93.2.2	CS93.2.3	CS93.3.1	CS93.3.2	CS93.3.3	CS94.1.1	CS94.1.2	CS94.1.3	CS94.2.1	CS94.2.2	CS94.2.3	CS94.3.1	CS94.3.2	CS94.3.3	CS95.1.1	CS95.1.2	CS95.1.3	CS95.2.1	CS95.2.2	CS95.2.3	CS95.3.1	CS95.3.2	CS95.3.3	CS96.1.1	CS96.1.2	CS96.1.3	CS96.2.1	CS96.2.2	CS96.2.3	CS96.3.1	CS96.3.2	CS96.3.3	CS97.1.1	CS97.1.2	CS97.1.3	CS97.2.1	CS97.2.2	CS97.2.3

1780	1780	1780	1765	1765	1765	1765	1765	1765	1765	1765	1765	1760	1760	1760	1760	1760	1760	1760	1760	1760	1753	1753	1753	1753	1753	1753	1753	1753	1753	1676	1676	1676	1676	1676	1676	1676	1676	1676	1761
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3776	4179	4123	6705	6415	6544	6792	6441	6561	6605	6763	6878	4029	3930	3220	3873	4208	3764	4209	3756	4075	166	443	446	459	389	209	383	481	462	9157	9256	8979	6362	6548	5829	1813	2168	1933	3022
1555	1643	1584	523	432	424	550	222	496	305	287	307	111	37	139	-28	-45	-24	99	78	-26	755	869	641	947	903	1247	902	931	728	655	790	811	774	678	715	1657	1535	1398	606
4659	4652	4462	22449	22353	22378	22172	21864	21850	22322	22087	21897	24537	24892	24772	25013	25271	25232	24384	24458	24482	14478	14301	14251	9488	9437	9611	14756	14559	14482	19187	19065	19261	19001	19124	19094	18706	18220	18213	26313
59877	59822	59498	69620	69397	69644	69742	69415	69384	69284	68907	68703	64525	63869	64391	64617	64940	64483	64660	64531	65085	65535	65593	65490	60784	60228	60665	65511	64241	64701	6779	6810	6947	24511	24783	24515	5562	5472	5627	10716
343815	345668	344494	299851	300767	302786	300196	300606	301848	300237	300453	301151	306567	307972	308364	307730	308855	309186	305326	307859	306652	292893	294148	293820	300301	300091	301201	293835	295157	295527	389913	392144	392437	356616	359134	360320	390210	393503	394226	362821
9366	9570	9657	913	608	601	521	406	595	693	590	633	706	606	1087	898	1094	752	1056	933	1015	32674	32596	32529	51753	52591	52349	29046	29978	30093	858	870	906	824	866	682	726	875	894	662
1327	1271	1416	3923	4342	4203	4382	4391	4303	4189	4440	4426	661	817	744	899	652	961	559	563	581	1125	1345	1438	1367	1346	1249	973	1443	1074	1021	006	805	1300	1017	986	815	923	1063	1204
6571	6376	6386	5509	5508	5693	5770	5734	5758	5633	5577	5790	6219	6140	6142	6093	6116	6233	6215	6101	6169	6280	6108	6299	6432	5964	5967	6000	6468	6110	5265	5477	5535	5730	5438	5461	5475	5700	5869	4791
36005	35487	36085	34941	35363	34860	34274	34522	34131	35158	35004	35102	21078	20949	21284	21271	21016	21001	21021	21581	21718	52875	52628	52643	61306	62192	61934	49709	49837	50068	31302	32107	31908	29563	29177	29446	31038	30972	30988	38607
12455	12490	12748	15581	15078	15361	15018	15251	15113	15726	16457	16269	8156	7998	7535	8675	9279	8317	7990	8166	8168	2609	3182	2684	3148	3755	3336	2790	3232	3106	2748	3076	2884	8004	7769	7477	2939	2811	2872	8224
14982	14560	14665	2575	2423	2523	2413	2450	2322	2590	2799	2649	1384	1467	1659	1559	1632	1614	1778	1525	1745	31784	31601	31802	4447	44493	44600	27972	28419	28165	830	1123	1210	066	1112	976	1092	971	794	1077
18577	18455	18230	21137	21306	21419	20306	20450	20208	21486	21202	21163	15516	15862	15953	16318	16245	16290	16938	16917	17386	19582	19380	19219	17301	17372	17346	18296	17942	18220	1099	1193	1255	2286	2286	2470	1049	934	1148	1980
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CS97	CS97	CS97	CS98	CS99	CS 100	CS100	CS 100	CS100	CS100	CS 100	CS100	CS100	CS 100	CS101	CS101	CS101	CS101	CS101	CS101	CS 101	CS101	CS101	CS102																
CS97.3.1	CS97.3.2	CS97.3.3	CS98.1.1	CS98.1.2	CS98.1.3	CS98.2.1	CS98.2.2	CS98.2.3	CS98.3.1	CS98.3.2	CS98.3.3	CS99.1.1	CS99.1.2	CS99.1.3	CS99.2.1	CS99.2.2	CS99.2.3	CS99.3.1	CS99.3.2	CS99.3.3	CS100.1.1	CS100.1.2	CS100.1.3	CS100.2.1	CS100.2.2	CS100.2.3	CS100.3.1	CS100.3.2	CS100.3.3	CS101.1.1	CS101.1.2	CS101.1.3	CS101.2.1	CS101.2.2	CS101.2.3	CS101.3.1	CS101.3.2	CS101.3.3	CS102.1.1
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naw net intensity data for the artifacts used in the statistical analysis continue	u.																																						

1761	1761	1761	1761	1761	1761	1761	1761
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3140	3077	3265	2764	2957	3093	3107	3056
661	796	593	725	535	496	819	747
26207	26127	25462	25402	25858	22450	22512	22796
10650	10735	6015	5981	5991	2659	2823	2974
365035	366295	377956	380063	378906	383700	384595	385112
1283	915	1131	1121	1047	1386	1411	1317
1364	1070	1232	1572	1185	1397	975	1152
5560	4962	4951	4748	4826	4590	4830	5014
38145	38560	28075	27689	27900	27333	27294	27125
8654	8312	8420	8558	8343	8232	8073	8161
1247	987	884	1073	948	1106	760	1047
2013	2130	1856	1883	1970	1802	1957	1967
2	ŝ	1	2	33	1	2	e
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CS102							
CS102.1.2	CS102.1.3	CS102.2.1	CS102.2.2	CS102.2.3	CS102.3.1	CS102.3.2	CS102.3.3

## **Appendix D: Permissions**

Permission letter to reprint images in Appendix B.

Academic Office Building Michigan Technological University 1400 Townsend Drive Houghton, MI 49931

April 13, 2015

Jon Prown **Chipstone Foundation** 7820 N Club Cir Milwaukee, WI 53217

Dear Jon Prown:

I am completing a Master's thesis at Michigan Technological University entitled " BEAUTIFUL FORMS AND COMPOSITIONS ARE NOT MADE BY CHANCE: EXPLORING THE EFFICACY OF PORTABLE X-RAY FLUORESCENCE TO SORT AND SOURCE ENGLISH LEAD GLAZED CERAMICS." I would like your permission to reprint in my thesis images of ceramics held by the Chipstone Foundation in the section titled "Appendix B" of the document. These images depict the samples analyzed during my research.

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If these arrangements meet with your approval, please sign this letter where indicated below and return to me the physical letter via mail and a scanned digital copy via email. Thank you very much.

Sincerely,

Steven J. Sarich

PERMISSION GRANTED FOR THE USE REQUESTED ABOVE:



Date: \_\_\_\_\_\_/14/11-